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Data-driven algorithms to estimate Maize Sap Flow Transpiration based on climatic and soil moisture data

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Abstract

Purpose Accurate estimation of crop transpiration is essential for optimizing irrigation management and improving water-use efficiency in precision agriculture. However, direct measurement of transpiration is often invasive, costly, and difficult to maintain at large scales. This study proposes a data-driven framework to estimate maize (*Zea mays* L.) sap flow driven by transpiration using widely available climatic and soil moisture data combined with machine learning techniques.

Methods Field experiments were conducted during the 2023 and 2024 growing seasons in central Italy under irrigated silage maize. Meteorological variables, soil water content, and crop growth indicators were used as inputs, while sap flow measurements served as reference outputs. Several machine learning models were evaluated, including Linear Regression, Support Vector Regression (SVR), Decision Tree Regressor, and Multi-Layer Perceptron Regressor (MLPR), using both Point Estimation and Temporal Estimation strategies. Temporal approaches incorporated short-term historical information through feature concatenation and previous-average windows.

Results Results demonstrate that non-linear models, particularly MLPR and SVR, consistently outperform linear and tree-based approaches. The inclusion of short temporal windows (45 minutes to 2 hours) significantly improves predictive accuracy, enhancing reconstruction of the diurnal transpiration pattern. Feature concatenation proved more effective than averaging strategies in capturing soil-plant-atmosphere interactions. Model performance remained robust across two contrasting growing seasons, confirming good generalization capability under interannual variability and data discontinuities.

Conclusion The proposed framework provides a reliable and minimally invasive solution for real-time estimation of maize transpiration, supporting precision irrigation management. These findings highlight the potential of machine learning models as practical decision-support tools for sustainable agricultural water management.

Keywords Sap flow prediction; Deep learning; environmental data; soil water content

Introduction

Optimising water management in agriculture represents a key challenge to ensure the sustainability of agricultural practices, maximise crop productivity and mitigate the effects of

40 climate change. Reducing natural resource consumption and improving crop adaptation to
41 extreme conditions such as drought and high temperatures are crucial objectives.

42 Maize (*Zea mays* L.), one of the most widely cultivated cereal crops worldwide, is particularly
43 sensitive to water availability, making the use of advanced methodologies for monitoring
44 transpiration and water demand essential. Its water requirements, which depend on many
45 factors including growth stage, climatic conditions, and soil type, generally range between 500
46 and 800 mm over the entire crop cycle under optimal conditions.

47 Transpiration (T), which represents the main component of crop water consumption, can be
48 directly estimated through sap flow measurements, which quantify the movement of water
49 within the plant stem. This estimation provides a direct indication of the crop's actual water
50 use, supporting more accurate and efficient water-resource management in agriculture
51 (Giménez et al., 2013; Jones, 2004; Vadez et al., 2024). Accurate sap flow assessment is
52 particularly important because plant transpiration greatly influences terrestrial water cycle
53 processes, accounting for about 80-90% of total evapotranspiration (Jasechko et al., 2013; Wei
54 et al., 2017). However, transpiration is controlled by complex and non-linear interactions
55 among multiple factors, particularly crop traits and meteorological data (Asbjornsen et al.,
56 2011), making its direct measurement and modelling inherently challenging.

57 Several methods have been developed to quantify plant water use, including sap-flow
58 techniques, indirect and micrometeorological measurements, as well as empirical, physically
59 based, and machine-learning models.

60 Direct methods rely basically on thermodynamic, magnetodynamic (nuclear magnetic
61 resonance) and electrodynamic principles. Among these, heat-transfer techniques are the
62 most widely adopted (Granier, 1985; Cermák et al., 2004; Nadezhdina, 1999; Kumar et al.,
63 2022; Steppe et al., 2010) and are commonly applied in a wide range of plant species and
64 numerous research domains to investigate plant hydraulics, improve water management,
65 assess crop water stress, and support irrigation planning. The advantage lies in obtaining
66 continuous transpiration measurements with high temporal resolution. However, in almost all
67 cases, these methods are rather invasive, expensive, time-consuming, and require frequent
68 maintenance (Bush et al., 2010; Ren et al., 2017; Steppe et al., 2015; Wullschlegel et al., 2011).
69 To overcome these limitations, several empirical and physical models have been proposed to
70 estimate transpiration. Examples include the SIMDualKc model, the modified Jarvis-Stewart
71 MJS, Multiple linear regression MLR and the Shuttleworth–Wallace S-W (Jiang et al., 2016; Liu
72 et al., 2022; Rosa et al., 2016; Tu et al., 2019; Whitley et al., 2008). However, these models
73 require extensive parameterization and large amounts of site-specific data, which restricts
74 their general applicability.

75 In recent years, data-driven approaches based on machine learning (ML) and deep learning
76 (DL) have emerged as powerful tools for modelling complex agronomic processes (Benos et al.,
77 2021; Kamarudin et al., 2021; Mana et al., 2024). Their strength lies in their ability to capture
78 the complex relationships between environmental and physiological parameters that regulate
79 these processes. For instance, Convolutional Neural Networks (CNNs) have become a
80 standard for crop disease identification and crop identification, as shown by Agarwal 2020,
81 Banerjee et al. 2024, Coulibaly 2019, Waldchen et al. 2018, and Zhong et al. 2019, who
82 achieved high diagnostic and classification accuracy. In the context of yield prediction, various
83 ML models have been successfully implemented to forecast productivity (Barbosa et al., 2020;
84 Chang et al., 2023; Maya Gopal et al., 2019), while in livestock management, clustering and

85 data processing algorithms like K-Nearest Neighbors (KNN) and Principal Component Analysis
86 (PCA) have been applied to track animal behaviour and health (Borgonovo, 2020; Riaboff,
87 2020).

88 In the specific field of water management (Pagano et al., 2023; Sun et al., 2019; Yadav et al.,
89 2024), techniques are often tailored to the nature of the data: Support Vector Machines (SVMs)
90 and Ensemble methods have shown excellent results in estimating transpiration and
91 evapotranspiration (Amir et al., 2021; Yamaç and Todorovic, 2020), while architectures like
92 RNNs, LSTM, and GRU have been introduced to handle the temporal dependencies of plant
93 physiological responses (Fan et al., 2021). The most predicted parameters are crop
94 evapotranspiration E_{Tc} , reference evapotranspiration E_{T0} and transpiration T , especially in
95 forests and crops with mainly high economic value or water-intensive management (Bellido-
96 Jimenez et al., 2023; Li et al., 2023; Yamaç and Todorovic, 2020). However, applications to long-
97 term sap flow prediction in herbaceous crops such as maize or tomato remain still limited. Amir
98 et al. (2021) predicted tomato sap flow based on climate, irrigation and sap flow datasets,
99 applying different ML algorithms; their results showed that random forest (RF) achieved the
100 highest accuracy, with good performance of linear regression (LR) and elastic net regression
101 (ENR). Similarly, Fan et al. (2021) estimated daily maize transpiration using four ML models:
102 SVM, extreme gradient boosting (XGBoost), ANN, and deep neural networks (DNN) models.
103 Their analysis incorporated different combinations of input variables, including weather
104 parameters, soil water content (SWC), leaf area index (LAI), and sap flow. Results indicated that
105 the DNN model provided the most accurate transpiration estimation when all input data were
106 used.

107 Successful ML model development depends on the availability of high resolution, robust and
108 comprehensive datasets acquired continuously over appropriate spatial and temporal scales.
109 Such data richness is essential to provide algorithms with the variability required for effective
110 learning and to ensure rigorous training and validation. Climatic data such as temperature,
111 humidity, precipitation, solar radiation are commonly employed as input to predict
112 evapotranspiration and transpiration (Ferreira et al., 2020; Xing et al., 2022; Zhanget al., 2025a).
113 Nevertheless, these data are most effective when integrated into eco-physiological
114 frameworks describing soil–plant–atmosphere interactions (Chen et al., 2020; Feng et al.,
115 2017; Tang et al., 2018). This step enables climatic data to be converted into target variables,
116 such as actual evapotranspiration or water fluxes, suitable for machine learning predictions.

117 Complementary data sources, such as satellite remote sensing and micrometeorological
118 systems, can further enhance ML prediction accuracy by providing valuable information on
119 crop water and physiological status and enriching the dataset’s dimensionality and spatial
120 representativeness. Vegetation indices (e.g., NDVI) and thermal parameters offer spatially
121 continuous insights into vegetation condition and water stress (Bounoua et al., 2024; Virnodkar
122 et al., 2020; Gómez et al., 2019; Schwalbert et al., 2020), while eddy covariance and Bowen
123 ratio systems provide direct measurements of energy and water fluxes within the soil-plant-
124 atmosphere continuum (SPAC) supporting model calibration and validation (Dou and Yang,
125 2018; Fang et al., 2020; Zenone et al., 2022; Zhang et al., 2025b). However, their high cost,
126 operational complexity and maintenance have restricted practical applications. In this context,
127 proximal sensors for direct monitoring of plant water transport, such as sap flow sensors,
128 represent an attractive tool. They provide high-temporal resolution data at relatively low cost
129 suitable for characterizing plant responses to water stress and water uptake dynamics (Amir
130 and Butt, 2025; Li et al., 2022; Zhang et al., 2023). When properly calibrated and integrated with

131 other environmental datasets— including satellite, climate, and micrometeorological data—
132 these measurements can substantially enhance the predictive capability of ML models. The
133 combination of multi-scale data sources enables the development of robust and adaptive
134 models tailored to local agroecological conditions, thereby supporting precision irrigation
135 management and providing actionable decision support to farmers.

136 The goal of this research activity was to develop data-driven models to derive maize
137 transpiration from easily measurable and widely available data, such as climate and soil
138 moisture, for the smart and sustainable real-time management of irrigation practices. The
139 study focused on irrigated silage maize cultivated at the 'Fondazione per l'Istruzione Agraria'
140 farm (Casalina, Perugia, Italy) within two experimental areas managed using Variable Rate
141 technology. Climate and soil water content data served as reference independent variables to
142 train the ML algorithms, while sap flow as the dependent variable, along with crop development
143 indicators such as growing degree days and days after sowing to account for the crop
144 vegetative phase. A key innovative aspect of this work lies in the combined use of multiple
145 machine learning models—ranging from linear and kernel-based approaches (Elastic Net
146 regression, Support Vector Regression) to tree-based methods (Decision Tree Regressor) and
147 multi-layer neural models (MLPR)—together with temporal estimation frameworks that
148 explicitly encode short-term historical dependencies through feature concatenation or
149 aggregated lag windows. This modelling architecture enables the capture of nonlinear soil-
150 plant-atmosphere interactions and diurnal transpiration dynamics that cannot be reproduced
151 by classical point-based predictors. To assess model generalisation, two independent
152 seasonal datasets (2023 and 2024 growing seasons) were used, allowing both intra- and
153 interannual evaluations under varying environmental conditions.

154 **Materials and methods**

155 **Study area**

156 The experimental activity was conducted in 2023 and 2024 in two experimental plots located
157 in central Italy within the 'Fondazione per l'Istruzione Agraria' farm (Casalina, Perugia, Italy). The
158 total area of the parcel analyzed in 2023 was about 30 hectares, 600 m long and 500 m wide
159 (coordinates: 42°56'08.3" N, 12°23'18.0" E), while that examined in 2024 was about 18
160 hectares, with an average length of 570 m and an average width of 310 m (coordinates:
161 42°55'52.8" N, 12°22'44.7" E) (Fig. 1). In both fields, a smaller study area was delineated for
162 sensor installation and focused monitoring (blue dots in Fig. 1). According to previous
163 analyses, the 2023 experimental plot was characterized by a loam soil texture (Santaga et al.,
164 2021), whereas the 2024 plot presented a silty loam texture. Both sites were characterized by a
165 nearly flat topography, with an average slope close to 0%. In both years, corn (*Zea mays* L.) for
166 silage (varieties LG 31,415 in 2023 and MAS576N in 2024) was sown as second crop after pea,
167 in the last decade of June using a precision seed drill, with a planting density of 7.5-8.5 plants
168 per square meter and a row spacing of 75 cm. Harvesting for both years took place in early
169 October. Irrigation was provided by self-propelled hose reel sprinklers, with a 7-day irrigation
170 interval that can be adjusted depending on weather conditions.

171

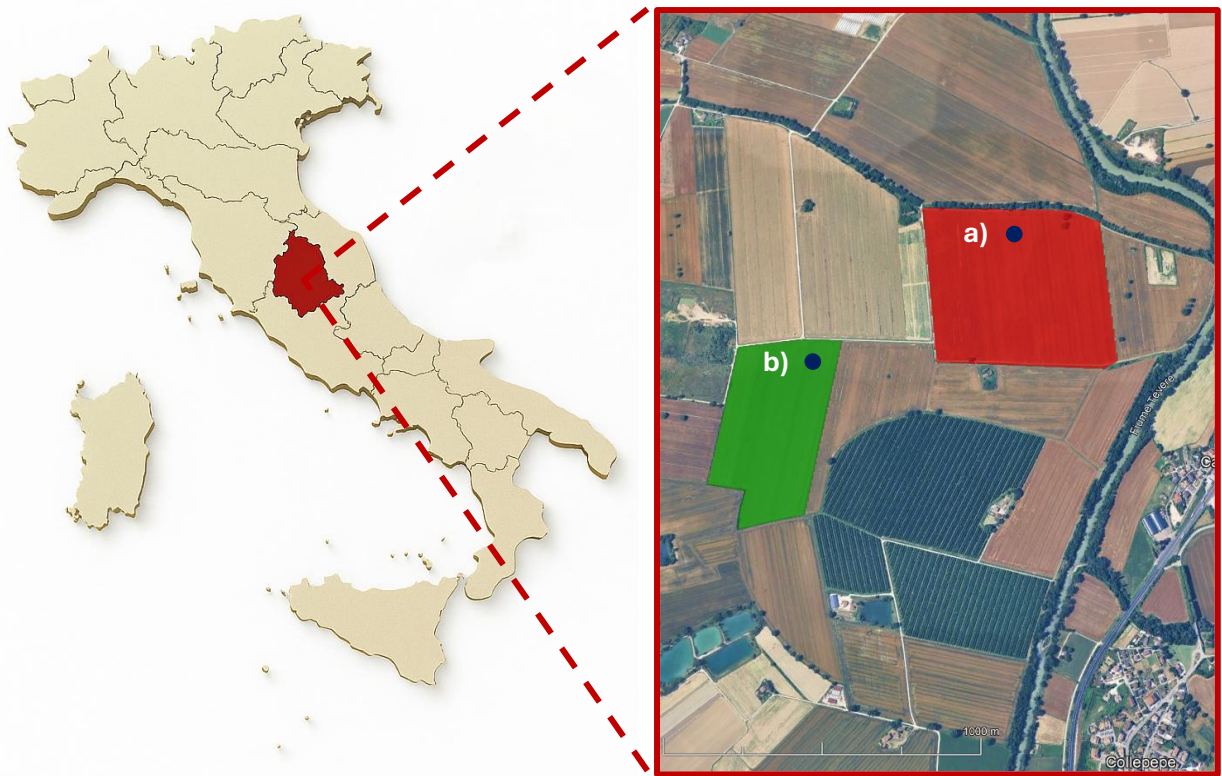


Fig. 1 Framing of the plots (in green) and detail of the study area (in blue) monitored a) in 2023 and b) in 2024

Data collection and dataset consistency

The environmental and physiological variables monitored during the experimental trials are summarized in Table 1 and Table 2, which respectively report external and internal data: descriptions, measurement units, and sampling frequencies.

All the data have been collected during the 2023 and 2024 maize growing seasons, different sensors were installed to monitor external variables, including local climatic conditions and soil water content, along with internal parameters i.e. sap flow (Fig. 2).

Meteorological data were obtained from an automatic weather station near the experimental site. Temperature, relative humidity, wind speed, global and net radiation, and the FAO Penman-Monteith ET₀ (Allen et al., 1998) were recorded every 15 minutes.

Precipitation (P) and irrigation (Irr) were collected using a tipping-bucket rain gauge (Spectrum Technologies Inc., Aurora, USA) installed at a height of approximately 2.5 m above the ground, and the datum is the cumulative values in 30 minutes time interval resulting in 2 samples/hour.

Soil water content was monitored by FDR probes (Sentek Drill&Drop Bluetooth, Sentek Technologies, Australia) with sensors at depths of 5-15-25-35-45-55 cm and stored at 60-minute intervals. In July 2023, 4 FDR probes were positioned between two plants along a corn row, spaced about 2-5 meters apart (Fig. 2a). To monitor soil moisture variability between rows, at the end of June 2024 6 probes were installed 10 and 20 cm away from the row, keeping a distance between the probes of 5-10 meters (Fig. 2b). The volumetric water content in the first 60 cm of soil was computed for each probe. Due to the high spatial variability of soil conditions and the intrinsic sensitivity of FDR probes, a max-min normalization was applied to each probe over its entire operating period. This procedure ensures that the probe-specific variability does not introduce bias into the computation of the final averaged soil water content. The normalized data were then averaged to obtain a single value, SWC_avg.

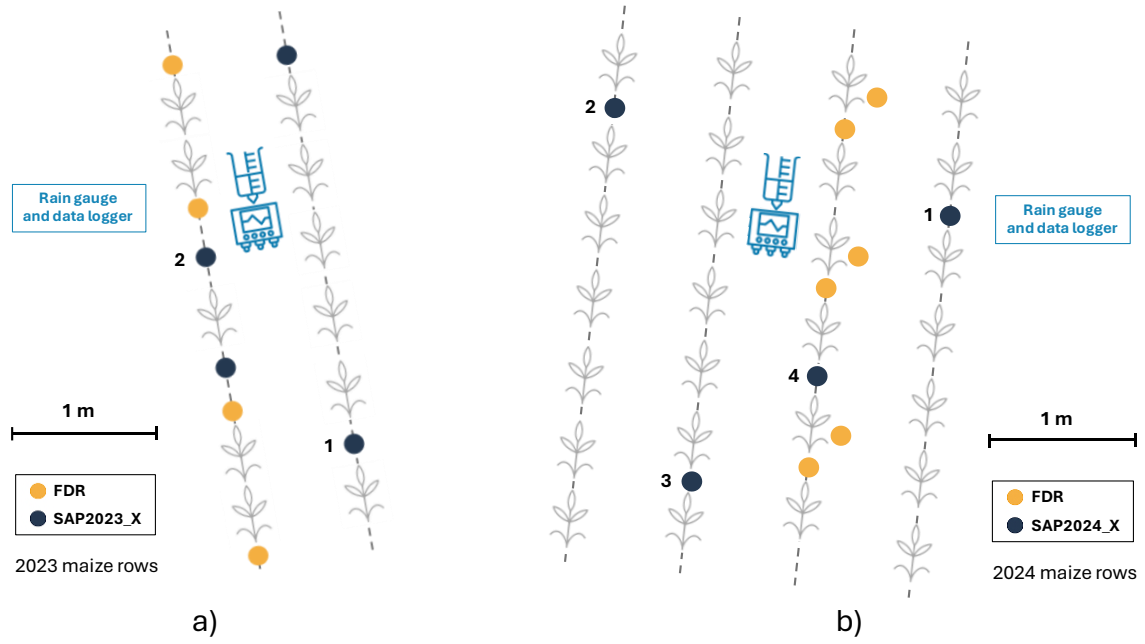


Fig. 2 Experimental plan for the two years monitoring: a) year 2023, 4 Dynagage sap flow sensors and 4 FDR probes positioned between two plants along a row, spaced 2-5 metres apart; b) year 2024, 4 sap flow sensors and 6 FDR probes 10 and 20 cm apart from the row, spaced 5-10 metres

Crop transpiration fluxes were continuously monitored during the irrigation season (August-September), using sap flow heat balance sensors (SAP) produced by Dynamax Inc. (Houston, Texas, USA). This type of sensor is based on heat balance theory and involves applying a constant amount of heat to a small section of the stem by means of a heating strip in the surrounding gauge body (Kišš and Manina, 2019; Lascano et al., 2016). The sensors directly measure the amount of heat carried by the sap through the stem, which is converted into real-time sap flow rate F ($\text{g}\cdot\text{s}^{-1}$) using the equation:

$$F = \frac{(P_{in} - Q_v - Q_r)}{C_p \cdot dT} = \frac{\left[P_{in} - K_{ST} \cdot A \cdot \left(\frac{dT_u + dT_d}{dx} \right) - K_{sh} \cdot CH \right]}{C_p \cdot dT}$$

where P_{in} is the power of heater (W), Q_v is vertical conduction, Q_r is radial heat conduction, C_p is specific heat of water ($4.186 \text{ J}\cdot\text{g}^{-1}\cdot\text{°C}^{-1}$) and dT is temperature increase of sap (°C), K_{ST} is the thermal conductivity of the stem ($\text{W}\cdot\text{m}^{-1}\cdot\text{°C}^{-1}$), A is the stem cross-sectional area (m^2), dT_u/dx and dT_d/dx ($\text{°C}\cdot\text{m}^{-1}$) are the temperature gradients in the up and down directions, respectively, dx is the spacing between the thermocouple junctions (m), K_{SH} is the sheath conductivity ($\text{W}\cdot\text{mV}^{-1}$), CH is the radial-heat thermopile voltage (mV).

Specifically, four sensors, suitable for plants with a stem diameter of approximately 35 mm, were installed on healthy, representative plants (Fig. 2). In both 2023 and 2024, the probes were deployed in August, during peak vegetation cover and the onset of flowering, when crop water demand is highest. The sensors were positioned 20–30 cm above the ground, between two internodes, following the manufacturer's recommended procedure. The installation procedure required the setting of certain parameters including the type of sensor and the cross-sectional areas of the stem used. The voltage was set at 4.4-5.4 V, with a power between 0.20 and 0.73 W and a temperature range of 0.1 - 13 °C . No stem damage due to heat occurred during the monitoring period. Sap flow measures (g/h) were sampled every 1 minute and averaged over 15-minute time intervals from August through September i.e. frequency 4 samples/hour (Table

1). Due to datalogger malfunctions and technical issues affecting the acquisition system, in the 2023 season, only two sensors (SAP23_1, SAP23_2) were included in the dataset, while for the 2024 season, four sensors (SAP24_1, SAP24_2, SAP24_3, SAP24_4) provided valuable data to be integrated in the dataset. The final sap flow dataset consistency is based on 1371 effective measurements for 2023 and 1472 samples for 2024. Missing values were handled using various gap-filling and interpolation techniques, as described in Section “Temporal Alignment and Gap Filling”. Two more parameters were added to consider the growth phase of the crop:

- Growing degree-day (GDD): this index expresses the relationship between air temperatures and phenological development of the crop (Liu et al., 2025) and is calculated as the sum of the differences between the average daily temperature (TA_avg) and the vegetative zero (Tz) of the species considered (8°C for maize).
- Days since sowing (DSS): sequential number representing the days elapsed since the sowing date.

As mentioned before, the monitored data and soil-crop dataset structure are presented in Tables 1 and 2, along with the measurement units and time resolution. Table 1 presents the weather data and crop growth variables, while Table 2 lists the soil water content and sap flow data.

Table 1 Meteorological and soil water content variables (external)

Variables	Description	Unit	Sampling
TA_min	Minimum air temperature	°C	4/hour
TA_avg	Average air temperature	°C	4/hour
TA_max	Maximum air temperature	°C	4/hour
RH_avg	Average Relative humidity	%	4/hour
Rg_avg	Average Global radiation	W/m ²	4/hour
Rn_avg	Average Net radiation	W/m ²	4/hour
Wind_avg	Average Wind speed	m/s	4/hour
ET0	Reference evapotranspiration	mm	4/hour
Irr and P	Cumulative irrigation and precipitation from rain gauge	mm	2/hour
DSS	Days elapsed since the sowing date	-	1/day
GDD	Growing degree-day	°C/d	1/day
SWC_avg	Average of normalized soil water content from FDR probes in the 60 cm soil depth	-	1/hour

248 **Table 2** Crop variables (internal)

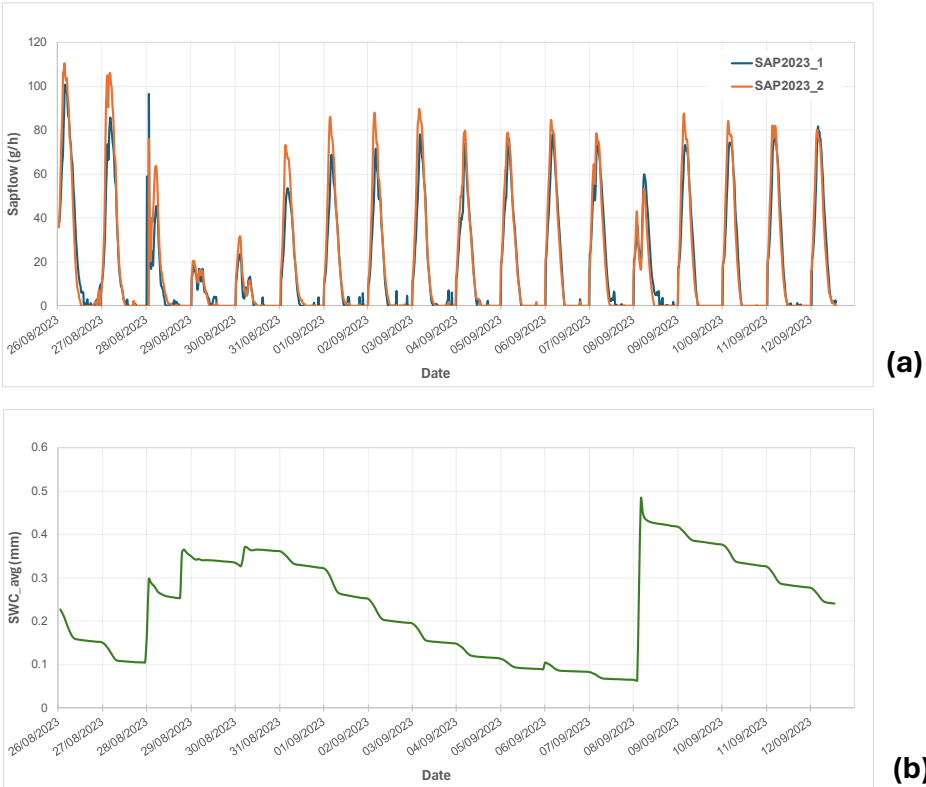
Variables	Description	Unit	Sampling
SAP23_X	Sapflow mass discharge from sensor X in 2023 (X = 1, 2)	g/h	4/hour
SAP24_X	Sapflow mass discharge from sensor X in 2024 (X=1, ..., 4)	g/h	4/hour

249 The collected meteorological, soil and crop data were organised into two separate datasets,
250 one for 2023 and one for 2024, which served as the basis for developing the datasets employed
251 in the implementation of the data-driven model.

252 Figure 3 shows the behaviour of some of the most significant variables included in the dataset
253 relative to 2023: Sapflow SAP, averaged soil moisture (SWC_avg), ET0, Irr and P. As expected,
254 the dynamics exhibit a close correlation and synchronicity between sap flow and ET0: as
255 evapotranspiration increases, sap flow increases.

256 Soil water content, on the other hand, exhibits a dynamic relationship T and ET0. SWC reaches
257 its maximum when T and ET0 are at their daily lowest values, typically at night, and
258 progressively declines throughout the daytime following a characteristic stepwise pattern. The
259 diurnal variation of SWC (Δ SWC) primarily reflects transpiration-driven soil water depletion,
260 highlighting the temporal coupling between soil water availability and crop water uptake over
261 the day–night cycle.

262 The data-driven models to be developed must be able to recognise the recurring patterns
263 between the climate variables and the plant’s transpiration response (i.e. sap flow) and the
264 relationships between T and irrigation/rainfall and consequently SWC, in order to be able to
265 estimate the plant’s water demand from real-time input data.



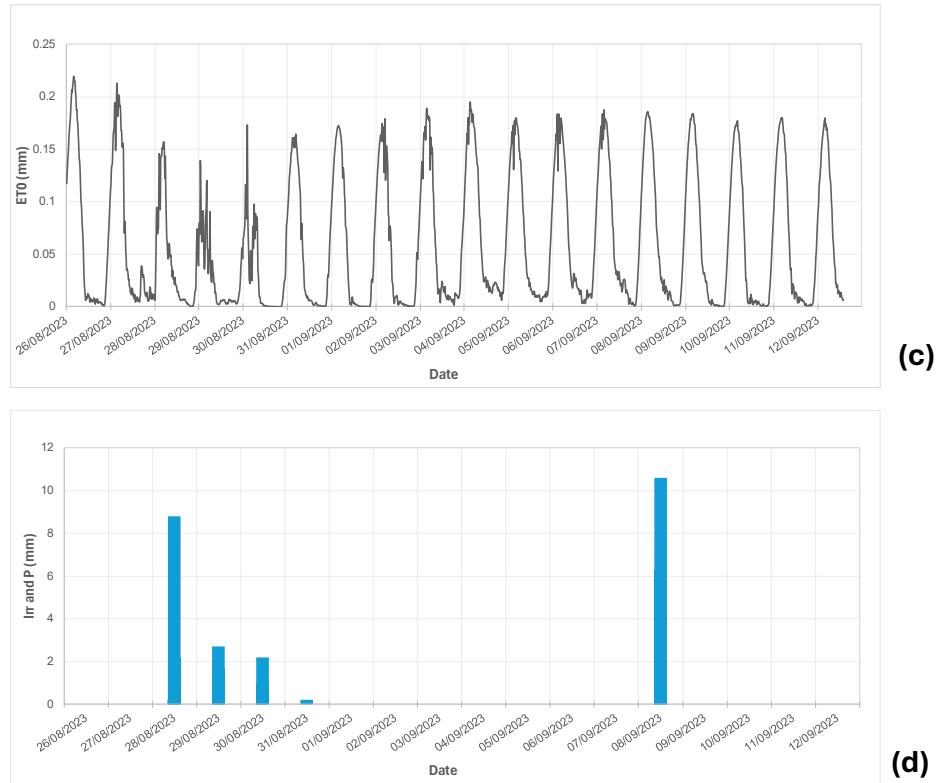


Fig. 3 Time behaviour of plant water consumption, sapflow, a), volumetric soil water content b), reference evapotranspiration, ET0 c) and Irrigation and precipitation d) during 2023

Data-driven estimation models

The following sections describe the data-driven estimation models adopted in the experiments. Two model types were considered: Point Estimation (PE) models, which predict the output based solely on the current input sample, and Temporal Estimation (TE) models, which additionally incorporate information from the previous N time steps to enhance prediction accuracy.

For each monitored year (2023 and 2024), the objective was to estimate the sap-flow variable `SAP_avg` based on concurrent meteorological (Table 1) and soil moisture (Table 2) data. `SAP_avg` is defined as the mean value obtained from all functioning sensors at each time step. As detailed in section “*Temporal Alignment and Gap Filling*”, the reference time step used in the analysis is 15 minutes.

Point Estimate (PE)

The Point Estimate (PE) strategy aims to predict the average sap flow value (`SAP_avg`) using only the current measurements of climatic and soil variables, while explicitly ignoring any information from previous time steps. In this configuration, the model focuses on instantaneous conditions (those observed within the most recent 15-minute sampling window) without accounting for temporal dependencies or lagged effects.

As summarized in Table 3, the input features include only the current external variables, whereas no averaged or concatenated features are introduced.

289 Different PE models were exploited to select the best predictive model for SAP_avg, comparing
 290 various ML algorithms:

- 291 • Linear Regression - LR
- 292 • Support Vector Regression - SVR
- 293 • Decision Tree Regressor - DTR
- 294 • Multi-Layer Perceptron Regressor – MLPR

295 Temporal Estimate (TE)

296 Strategies are investigated to capture temporal dependencies within the data. In contrast to PE,
 297 where models relied only on current sensor readings to estimate target values, the present
 298 analysis extends the input by incorporating information from past observations. This approach
 299 enables to assess whether previous measurements can be effectively exploited to improve the
 300 accuracy of the current SAP_avg prediction.

301 Two different approaches have been used to account for past observations: the current sample
 302 and Previous Averages (TE-PA) and the current sample and Features Concatenation (TE-FC).
 303 TE-PA has been built by concatenating each observation with the average of the N previous
 304 ones. The parameter N is computed by specifying a temporal interval., such as 45 minutes, or
 305 2, 6 hours, which corresponds to a specific sample number: since the data are recorded at 15-
 306 minute intervals, each additional 15 minutes in the temporal window increases N by one unit.
 307 Consequently, for temporal windows of 45 minutes, 2 hours, and 6 hours, N assumes values of
 308 3, 8, and 24, respectively.

309 The TE-FC strategy was implemented by concatenating each observation with the previous N
 310 ones.

311 Table 3 provides a comprehensive summary of the input and output features considered in the
 312 models, outlining the variables used for model training and prediction.

313 **Table 3** Features for the Point Estimate (PE) and the Temporal Estimate (TE) models

MODELS	Input features (single sample)	Averaged/concatenated features	Output quantity
PE	time, SWC_avg, TA_avg, RH_avg, Rn_avg, Wind_avg, Eto, Irr and P, GDD, DSS	----	SAP_avg
TE	time, SWC_avg, TA_avg, RH_avg, Rn_avg, Wind_avg, Eto, Irr and P, GDD, DSS	SWC_avg, TA_avg, RH_avg, Rn_avg, Wind_avg, Eto, Irr and P	SAP_avg

314 Model Assessment and Details

315 Model assessment is performed by using the RMSE and R²-Score metric defined as:

$$316 \quad RMSE = \sqrt{\frac{1}{n} \cdot \sum_{k=1}^N (y_k - \hat{y}_k)^2}$$

$$317 \quad R^2 = 1 - \frac{\sum_{k=1}^N (y_k - \hat{y}_k)^2}{\sum_{k=1}^N (y_k - \bar{y})^2}$$

318 in which y_k and $\hat{y}_k$ are the observed and the predicted value for sample k , and $\bar{y}$ is the mean of
319 all SAP_avg values.

320 All experiments were implemented in Pandas for data manipulation and preprocessing, and
321 Python, using the scikit-learn library for model development and hyperparameter tuning.

322 **Dataset management and feature engineering**

323 This section outlines the data preprocessing steps, including time resolution alignment and gap
324 filling.

325 **Temporal Alignment and Gap Filling**

326 As reported in Table 1, measures are sampled at different frequencies, spanning to 1
327 sample/day to 4 samples/hour. To ensure data consistency, a fixed 15-minutes time resolution
328 has been selected. This section outlines the main steps taken to align the several sampling
329 frequencies.

- 330 • *Meteorological Alignment*: since rainfall and irrigation data were recorded as
331 cumulative values every 30 minutes, while other weather variables were sampled every
332 15 minutes, a splitting procedure was applied. Each 30-minute cumulative value was
333 divided equally: half was assigned to the current 15-minute record and the other half to
334 the preceding 15-minute slot.
- 335 • *Soil Moisture Interpolation*: the SWC_avg, originally recorded every 60 minutes, was
336 linearly interpolated to match the 15-minute sampling frequency of the climatic and
337 sap flow data. This step was essential to provide the models with a continuous
338 representation of soil water availability.
- 339 • *Target Variable Synchronization*: sap flow measurements, initially collected every
340 minute, were averaged over 15-minute intervals to align with the climatic reference time
341 step.

342 After merging the weather and soil-crop datasets using date-time keys, missing values due to
343 malfunctioning in SAP sensors were handled. In 2023 dataset a multi-step imputation strategy
344 was applied. Initially, missing values occurring at night—identified by negative net radiation
345 ($Rn_avg < 0$)—were set to zero. For daytime gaps, values were imputed using the average
346 recorded at the corresponding time across different days. Regular data gaps were observed
347 due to sensor-specific logging cycles. Since these empties remained after the previous steps,
348 they were handled according to their temporal extent:

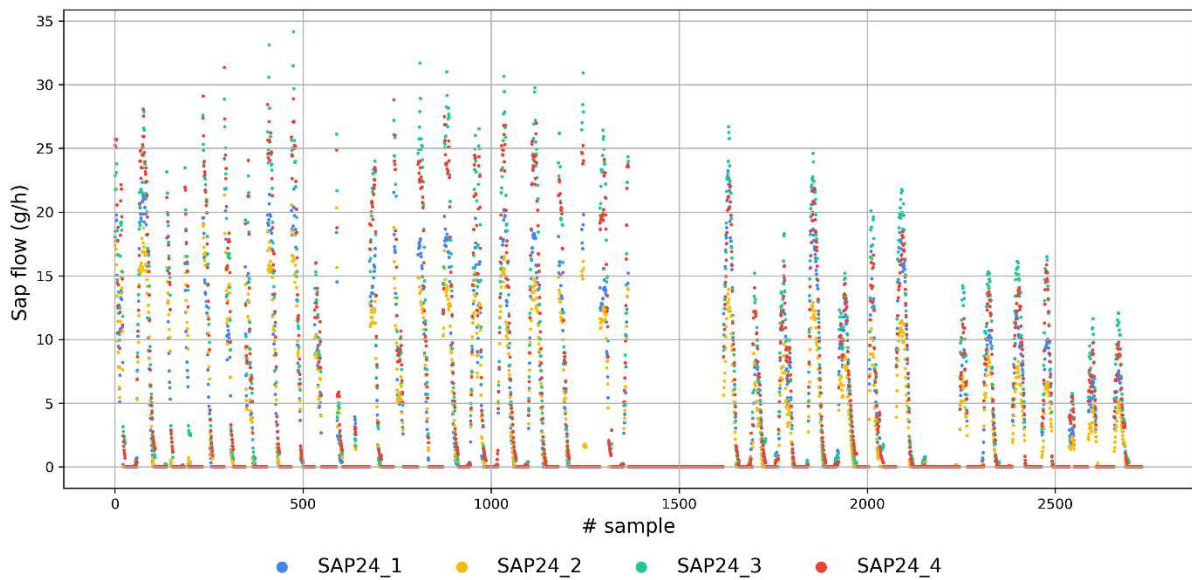
- 349 • For SAP23_1 (single isolated missing value), the gap was filled using the average of the
350 immediately preceding and subsequent measurements.
- 351 • For SAP23_2 (three consecutive missing samples), linear interpolation was applied.

352 As illustrated in Fig. 4, the 2024 sap flow measurements exhibit a considerable number of
353 missing (NaN) values, predominantly clustered around sample index 1500, likely due to sensor
354 malfunction or incorrect activity. Unlike the 2023 dataset, for which missing values were filled
355 using data from previous or subsequent days, the extent and distribution of missing entries in
356 2024 made the same procedure unfeasible. Therefore, linear interpolation was adopted before

357 integrating the sap flow data with the meteorological dataset. After the merge, the remaining
 358 missing values corresponding to periods with negative Rn_avg were set to zero, while the
 359 residual NaN values, not temporally aligned or too sparse to be reliably filled, were discarded
 360 from the analysis.

361 For visualization purposes, the x-axis of the 2024 plots reports the sample index instead of the
 362 corresponding days. This choice was made to preserve readability, since the presence of a large
 363 number of missing (NaN) values, subsequently removed during preprocessing, would have
 364 resulted in irregular time spacing and a distorted representation of the temporal scale.
 365 Consequently, only the sample number is shown on the x-axis, while the y-axis represents the
 366 measured or estimated sap flow values (SAP_avg).

367 After pre-processing and gap filling, the complete dataset consistency is 1696 samples for
 368 2023, while 2731 samples for 2024.



369
 370 **Fig. 4** Sap flow data measured by the four sensors in 2024

371 Time Encoding and Features Normalization

372 The collected data is marked with a timestamp: hour and minute of each measurement. To
 373 enable the ML models to effectively learn the diurnal periodicity of transpiration, the time of
 374 day was transformed using cyclic encoding. Treating time as a linear numerical feature would
 375 create a false discontinuity: 23:45 and 00:00 would be treated as numerically distant.
 376 Therefore, the timestamp was decomposed into its sine and cosine components. This
 377 transformation ensures that the models perceive the proximity between the end of one day and
 378 the beginning of the next.

379 The time is split into hours $\in [0, 23]$ and minutes $\in \{00, 15, 30, 45\}$. To aggregate them, minutes
 380 are first converted into fractional hours and then combined with the hour component:

$$381 \quad tempTime = 4 * (hours + (minutes / 60))$$

382 This produces 96 unique values (24 hours $\times$ 4 intervals). To preserve the circular nature of time
 383 over the day, a cyclic encoding was then applied:

$$newTime_x = 2\pi\sin(tempTime / 95)$$

$$newTime_y = 2\pi\cos(tempTime / 95)$$

A min-max normalization was applied to rescale all input features to the range $[-1, +1]$ ensuring consistency with the sine and cosine encodings used for time feature. This transformation preserves the relative distribution of each feature while aligning all inputs to a common scale.

Data partitioning for 2023

The complete 2023 dataset spans just over 18 days. The first 14 days were assigned to the training set, while the remaining 4 days were designated as the test set. Additionally, three days from the training set were reserved for hyperparameter validation; this configuration is referred to as *split1*. As illustrated in Fig. 5, which depicts the SAP_avg values of *split1*, three days within the training set (corresponding to the third, the fourth, and the fifth peaks) exhibit markedly different behaviour compared to other days.

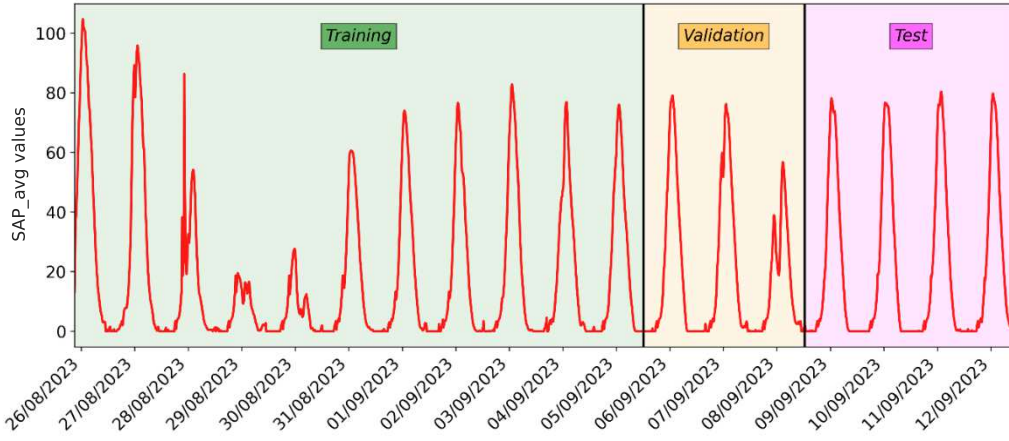


Fig. 5 Train (green), Validation (yellow), and Test (purple) sets (*split1*) in 2023

To account for these anomalies, two additional data splits were built, *i.e.*, *split2*, and *split3*: in *split2* the test set contains the three days with irregular sap flow values (Fig. 6a), whereas the test set for *split3* includes only half of those irregular measurements, with the remaining part of the set containing regular values (Fig. 6b). These three splits have been designed to evaluate the impact of those irregular patterns on model performance and to assess their generalization capabilities.

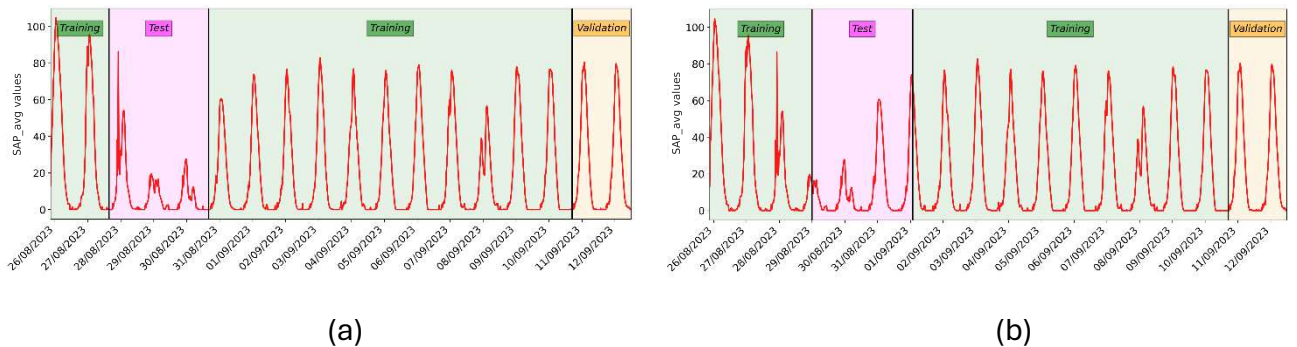
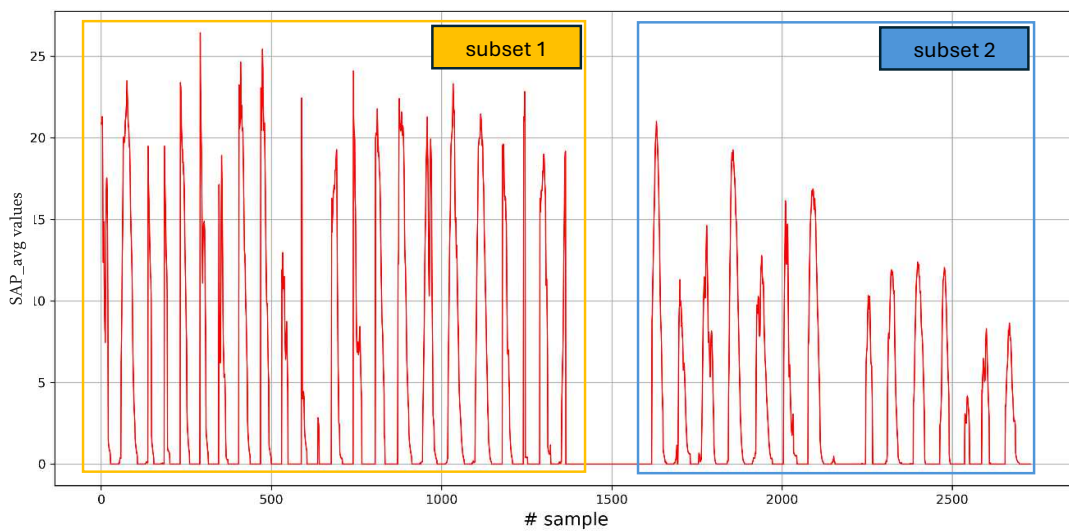


Fig. 6 Train (green), Validation (yellow), and Test (purple) sets for *split2* (a) and *split3* (b) in 2023

408 Data partitioning for 2024

409 The dataset collected in 2024 was used to assess the generalisation capability of the model
410 across different growing seasons, in additional experiments. These analyses are crucial for
411 evaluating the model's robustness when trained and tested on data acquired under potentially
412 different conditions and spanning an extended plant life cycle.

413 The 2024 dataset spans a longer temporal period compared to 2023, as evidenced by the mean
414 sap flow values depicted in Fig. 7. As already discussed in Section “Temporal Alignment and
415 Gap Filling”, the sap flow (SAP_avg) measurements in 2024 contain a significant number of
416 missing (NaN) values. To address this issue, the dataset was partitioned into two subsets:
417 *Subset 1*, which spans from the beginning to approximately index 1400, and *Subset 2*, which
418 ranges from around index 1600 to the end.



419

420 **Fig. 7** Mean sap flow values of the four SAP24 sensors

421 Despite the application of the gap-filling procedure described before and the partitioning
422 strategy, a considerable number of NaN values remained. Due to the incomplete temporal
423 continuity, temporal estimation (TE) experiments, which require incorporating the previous N
424 samples into the prediction process, could not be performed. Consequently, the analysis was
425 restricted to the point estimation (PE) task and two different experiments were implemented:

- 426 • *Exp1*: PE models were trained on the 2023 dataset and tested on the 2024 dataset, to
427 directly assess cross-year generalization.
- 428 • *Exp2*: PE models were trained on a combined dataset consisting of 2023 and Subset 1
429 of 2024, and then tested on Subset 2 of 2024, simulating adaptation to partially known
430 2024 conditions.

431 Hyperparameters Tuning

432 After completing the data preprocessing, the hyperparameter tuning procedure was performed
433 prior to model evaluation. This step is essential to identify the optimal configuration of model
434 parameters that influence its learning behaviour. Proper tuning ensures that each algorithm
435 operates under the most suitable conditions, thereby enhancing model performance, stability,

436 and generalization capability. The optimization was carried out through a GridSearchCV
 437 (Bishop, 2006) procedure, which systematically explores multiple parameter combinations to
 438 select the configuration yielding the best predictive accuracy. Table 4 reports the optimal
 439 hyperparameter values obtained through cross-validation on the 2023 dataset for PE case,
 440 which are provided here as a representative example. Analogous were performed on PE and TE
 441 strategies and on the 2024 dataset. It should be noted that, for the LR model, an Elastic Net
 442 (Zou and Hastie, 2005) formulation was adopted to allow L1 and L2 regularization.

443 **Table 4** Best hyperparameters for the 2023 PE case

Hyperparameter	Description	Best Value
LR (Elastic Net)		
α (alpha)	Regularization strength: higher values mean stronger regularization	0.1
L1_ratio	Controls the mix between L1 (Lasso) and L2 (Ridge) penalties	0.9
DTR		
criterion	Function to measure the quality of a split	poisson
max_depth	Maximum depth of the tree	None
max_features	Number of features to consider when looking for the best split	sqrt
min_samples_leaf	Minimum number of samples required to be at a leaf node	1
min_samples_split	Minimum number of samples required to split an internal node	10
SVR		
C	Regularization parameter; controls trade-off between smoothness and accuracy	10
kernel	Specifies the kernel type to be used in the algorithm	rbf
MLPR		
activation	Activation function for the hidden layer	logistic
α (alpha)	L2 penalty (regularization term)	1e-5
hidden_layer_sizes	Neurons per layer	(50, 50)
learning_rate_init	Initial learning rate used during training	0.01
max_iter	Max number of iterations	500
solver	Optimization algorithm	adam

444 **Results**

445 In accordance with the considerations outlined above, the following sections present the
446 results obtained from the application of the two modelling approaches for the 2023 and 2024
447 datasets, highlighting their predictive performance and the main differences observed between
448 the two monitoring periods.

449 **Results of PE approach for 2023 data**

450 This section summarizes the quantitative results of each PE model and provide a qualitative
451 evaluation regarding the best performing one. Performance metrics reported in Table 5 include
452 the R²-score on both training and test set, as well as the RMSE (Bishop, 2006).

453 **Table 5** Results of best PE models. The best model for each split is shown in bold.

	Model	RMSE		R ² -score	
		train	test	train	test
split1	LR	10.057	11.246	0.835	0.822
	DTR	2.824	13.379	0.987	0.748
	SVR	5.958	6.568	0.942	0.939
	MLPR	2.910	7.861	0.986	0.913
split2	LR	8.662	9.721	0.894	0.385
	DTR	2.858	8.160	0.989	0.567
	SVR	14.401	9.934	0.708	0.357
	MLPR	3.392	7.318	0.984	0.651
split3	LR	8.985	9.103	0.885	0.590
	DTR	2.307	10.482	0.992	0.456
	SVR	4.946	6.081	0.965	0.817
	MLPR	4.151	5.524	0.976	0.849

454

455 Based on the results in Table 5, MLPR and SVR consistently emerge as the best performing
456 models across all dataset splits. In each scenario, at least one of the two achieves the best
457 performance in both RMSE and R²-score, often outperforming the others by a clear margin.

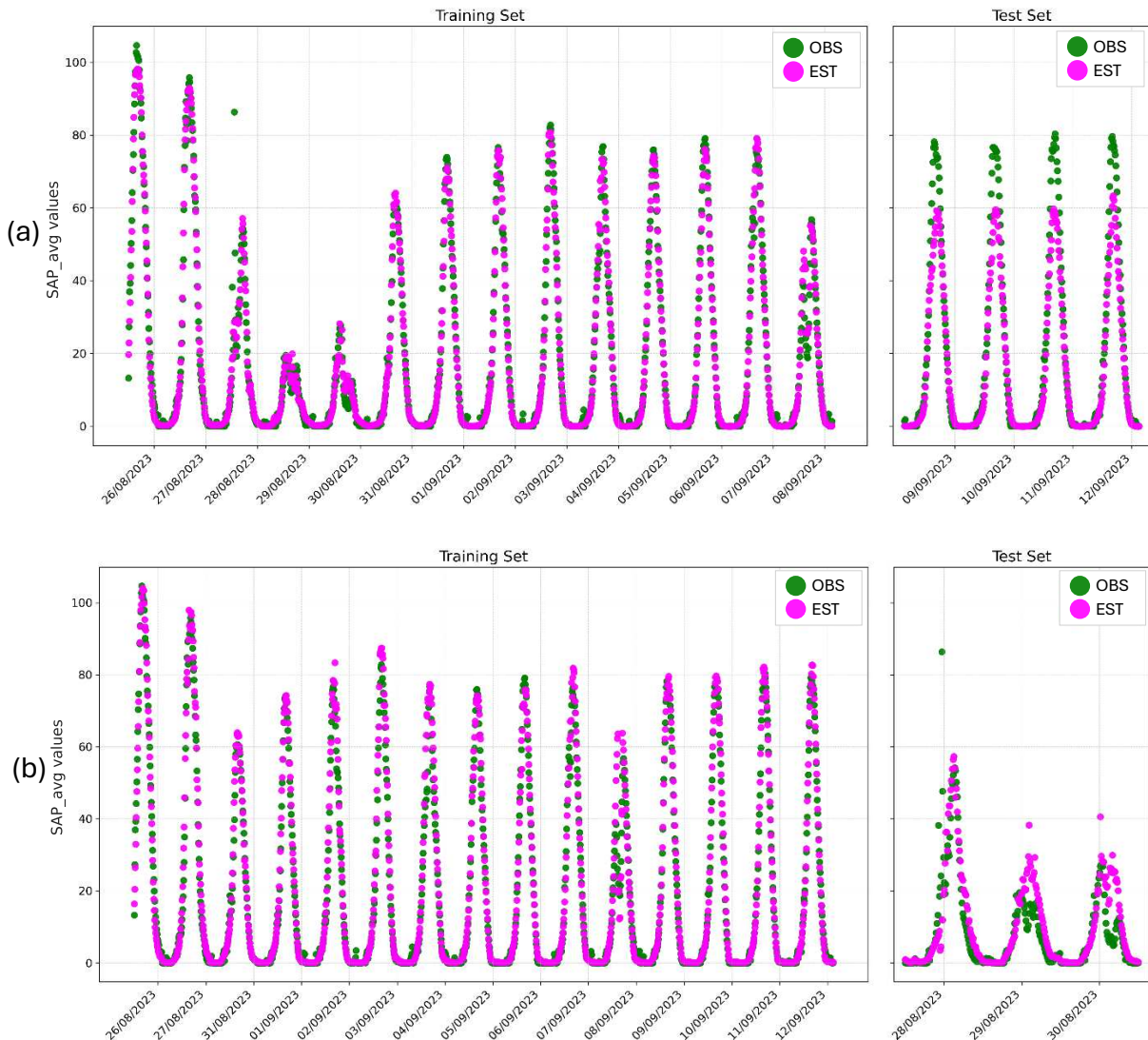
458 In split1, both models demonstrate excellent predictive capabilities, while traditional models
459 like LR and DTR show either poor generalization or overfitting. This trend continues in split2,
460 where MLPR proves to be the most robust, especially in handling unseen or irregular data
461 patterns. Even in split3, where the test set contains both regular and irregular sap flow values,
462 MLPR and SVR provide the best performance, confirming their adaptability and stability.

463 Given their consistently superior results, SVR and MLPR are selected as the best-performing
464 models for sap flow estimation, showing the highest potential for generalizing across diverse
465 conditions.

466 Although SVR and MLPR yield comparable results, MLPR achieves overall a better performance.
467 For this reason, the following graphs shows only the qualitative results of MLPR.

468 Figure 8 compares the MLPR predictions (EST) with the observed values (OBS) for the three
469 dataset splits. In split1 (Fig. 8a), the model reproduces the temporal pattern of the test set well,
470 except for a few peak values that are slightly underestimated. In split2 and split3 (Figs. 8b–c),
471 the performance degrades due to a general overestimation of several SAP_avg values around
472 midday, which is expected given the greater irregularity of these test sets. It is also worth noting
473 that split2 reports a lower R^2 than split1 despite achieving a slightly lower RMSE. This behaviour,
474 which may appear counter-intuitive, is explained by the markedly reduced variability of
475 SAP_avg in the split2 test set (approximately 0–30 g/h for two days out of three, compared to 0–
476 80 g/h in split1). Because R^2 depends on the variance of the observed data, when the ground
477 truth fluctuates less, the same absolute prediction error represents a larger portion of the total
478 variance, resulting in lower R^2 values even if the RMSE improves.

479 Split3 represents an intermediate situation: its test set contains both regular and irregular sap-
480 flow patterns, with a variability that is higher than in split2 but still smaller than in split1.
481 Consequently, its R^2 values typically fall between those of split1 and split2, reflecting this
482 intermediate level of signal variability and difficulty.



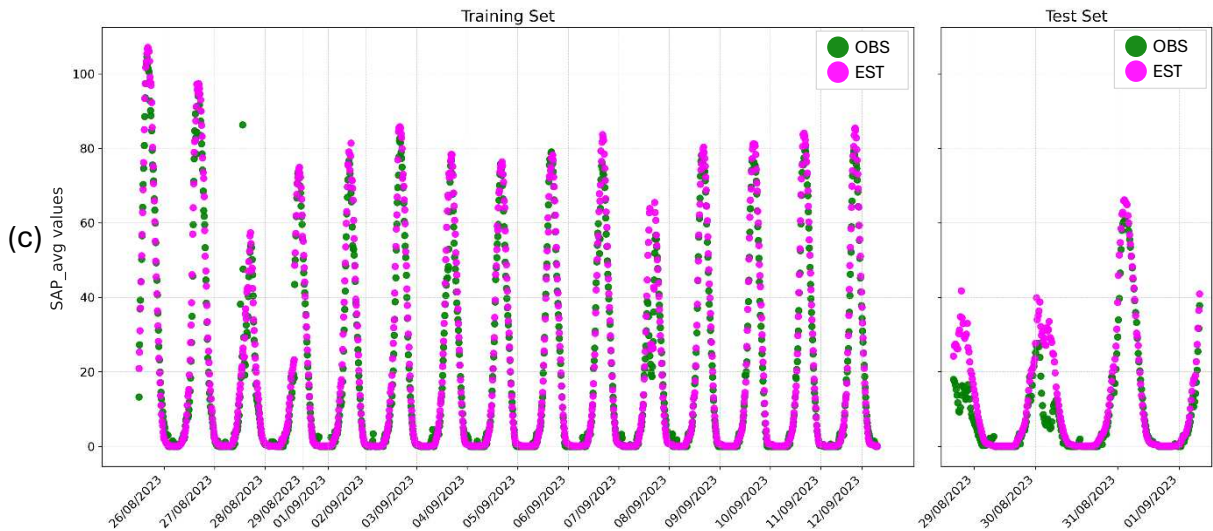


Fig. 8 SAP_avg estimated values, EST, by MLPR model compared against observed values, OBS, for split1 (a), split2 (b) and split3 (c)

Results of TE approach for 2023 data

The following subsections present quantitative and qualitative results for the three time intervals considered in the TE model (45 minutes, 2 hours, and 6 hours). Specifically, table 6 reports the RMSE and R^2 -score scores for the SVR and MLPR models, which proved to be the best in the PE approach, while LR and DTR were discarded due to their poor performance (as described in the previous sections). Additionally, three graphs (one for each split) compare the observed values with those estimated using the MLPR model for the three temporal windows. For each split and time interval, results are depicted both for the approach based on concatenating the average of the previous samples (TE-PA) and for the direct concatenation of the features (TE-FC).

Overall, the results obtained across the three temporal windows reveal a clear split-dependent behaviour. Split1 generally provides good predictive performance, but it is not consistently the best case, especially when longer temporal windows are used. Split2 systematically emerges as the most challenging configuration: its low variability and irregular dynamics lead to the highest RMSE values and the lowest R^2 scores across all TE-PA and TE-FC experiments, regardless the window size. In contrast, split3 often achieves the best results, particularly for longer windows and when feature concatenation (TE-FC) is applied. In this setting, the model benefits from the additional temporal context by more effectively reconstructing the overall daily pattern, which results in substantial improvements in R^2 and, in several cases, reductions in RMSE. Increasing the temporal window does not produce a uniform trend: short windows (45 minutes and 2 hours) typically offer the most stable and reliable improvements, whereas longer windows (6 hours) may either enhance or degrade performance depending on the split. This reflects the trade-off between providing meaningful temporal context and introducing overly smoothed or outdated information. Finally, TE-FC generally outperforms TE-PA in terms of R^2 , especially with wider windows, indicating a stronger ability to recover the shape of the transpiration signal, although this does not always translate into a corresponding reduction in RMSE.

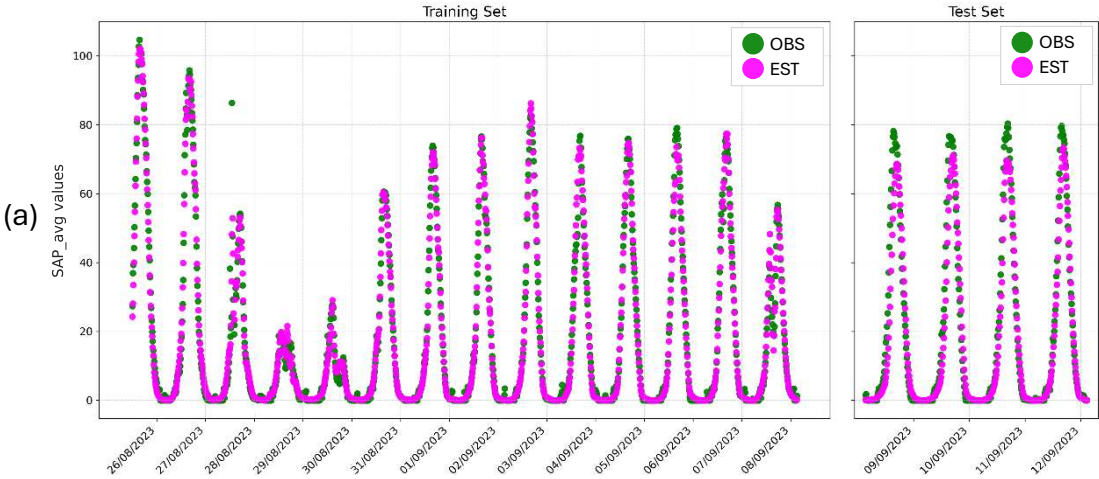
514 **45 minutes temporal windows for TE-PA and TE-FC strategies**

515 Results obtained by concatenating the average (TE-PA) of the previous 3 samples
516 (corresponding to 45 minutes) along with those derived from direct feature concatenation (TE-
517 FC) are presented below. Quantitative outcomes are summarised in Table 6. The transition from
518 PE to TE-FC improved the R^2 for split3 from 0.849 (see table 5) to 0.959, confirming the
519 importance of temporal context.

520 **Table 6** Results of SVR and MLPR with best hyperparameters found with GridSearchCV.

Temporal Estimate (TE) models									
(a) TE-PA					(b) TE-FC				
	Model	RMSE		R2-score		RMSE		R2-score	
		train	test	train	test	train	test	train	test
split1	SVR	5.849	7.481	0.944	0.921	6.079	7.914	0.940	0.912
	MLPR	3.041	5.964	0.985	0.950	3.898	5.377	0.975	0.959
split2	SVR	2.719	10.087	0.990	0.337	2.819	9.523	0.989	0.409
	MLPR	2.826	7.247	0.989	0.658	5.327	6.905	0.960	0.689
split3	SVR	4.967	4.263	0.965	0.912	5.353	3.608	0.959	0.940
	MLPR	2.421	6.334	0.992	0.805	3.022	3.005	0.943	0.959

521 Figures 9, 10 and 11 depict qualitative results for each split, highlighting the impact of the
522 different test sets.



523

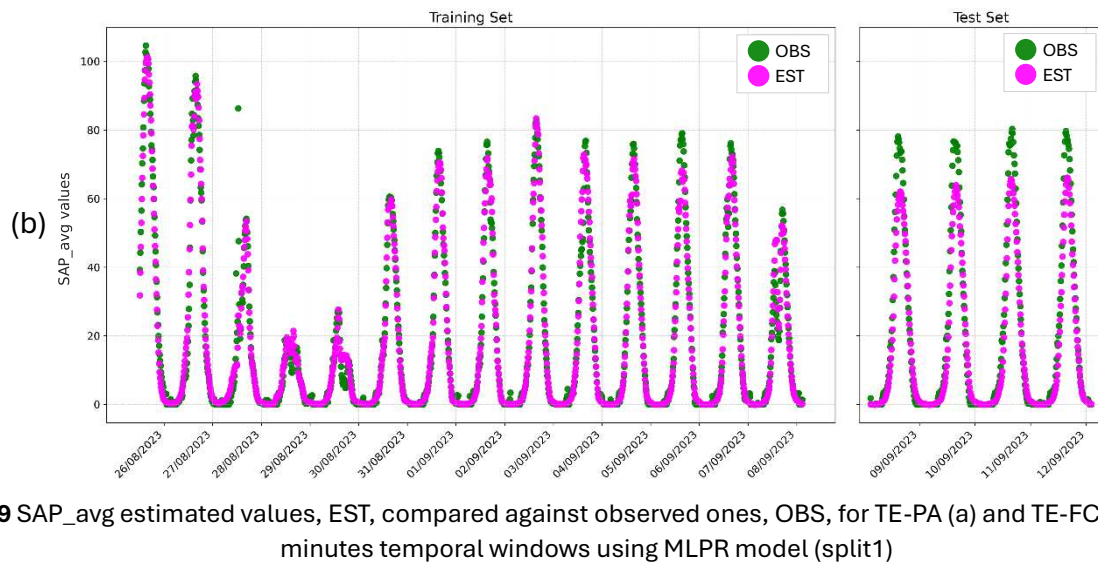


Fig. 9 SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 45 minutes temporal windows using MLPR model (split1)

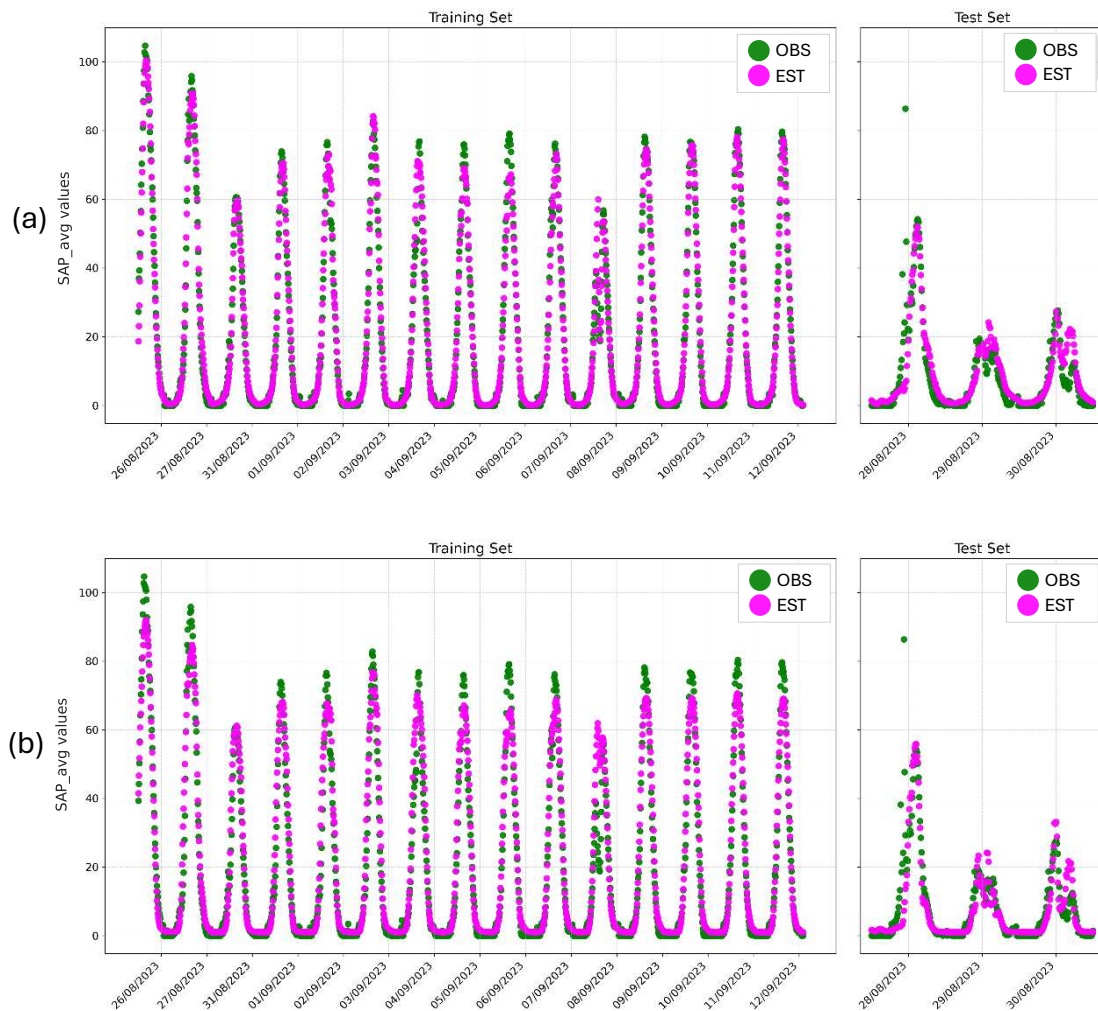


Fig. 10 SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 45 minutes temporal windows using MLPR model (split2)

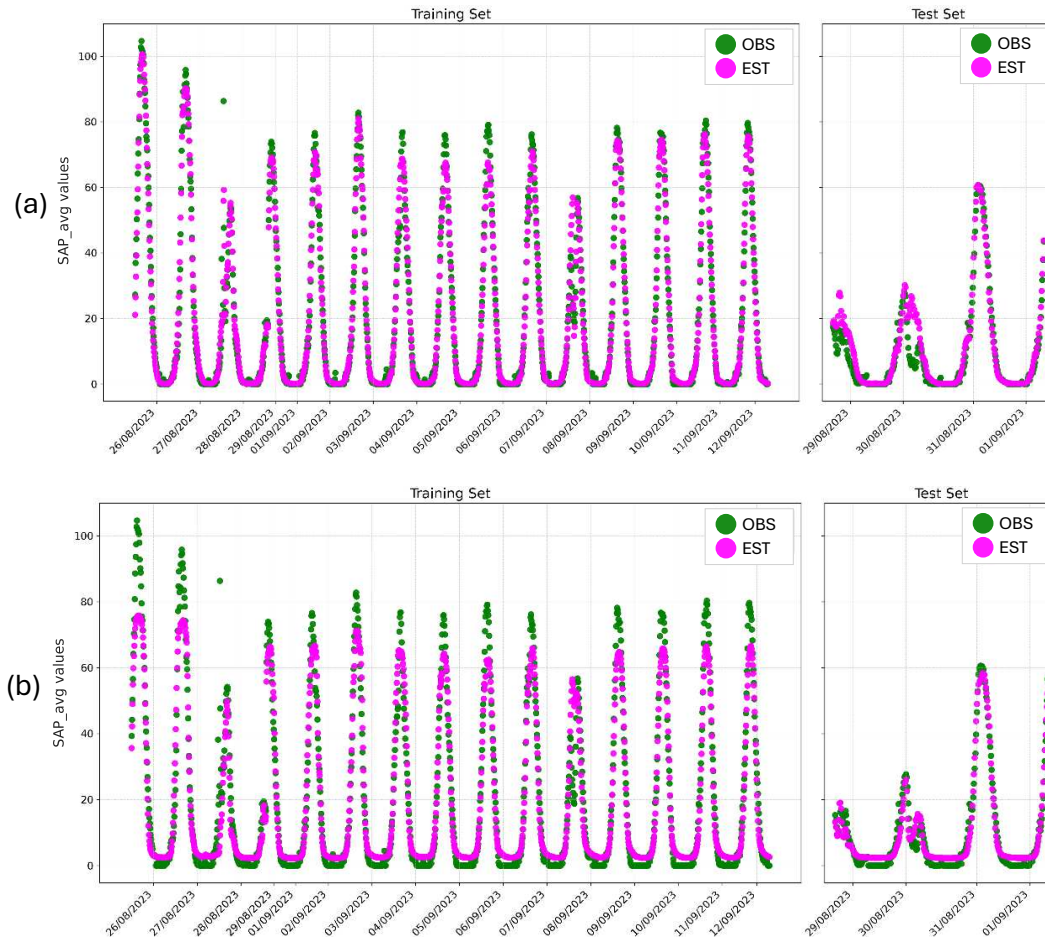


Fig. 11 SAP_avg estimated values EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 45 minutes temporal windows using MLPR model (split3)

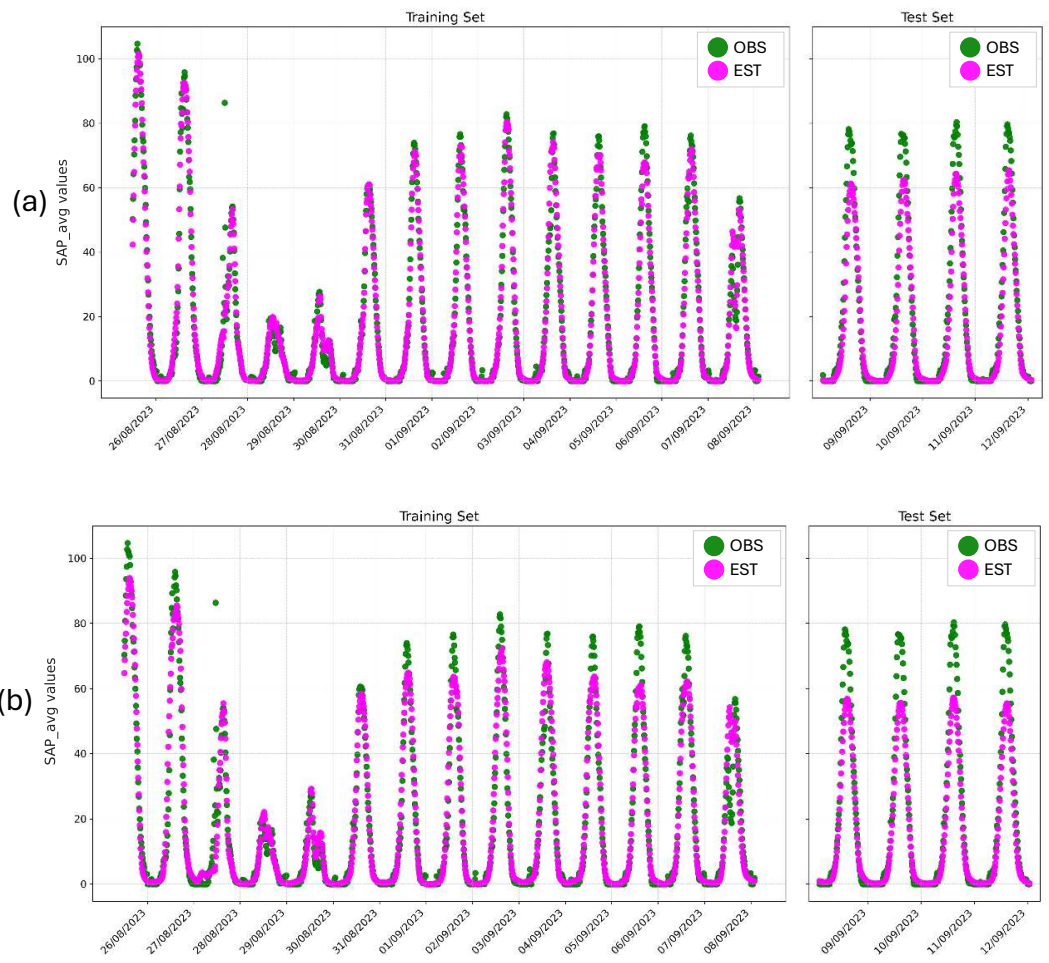
2 hours temporal windows for TE-PA and TE-FC strategies

The results, obtained by concatenating the average (TE-PA) of the previous 8 samples (2 hours), are shown below along with those obtained by directly concatenating features (TE-FC). Table 7 shows the quantitative results, while Figures 12, 13 and 14 illustrate the qualitative results as the split change.

Table 7 Results of SVR and MLPR with best hyperparameters found with GridSearchCV.

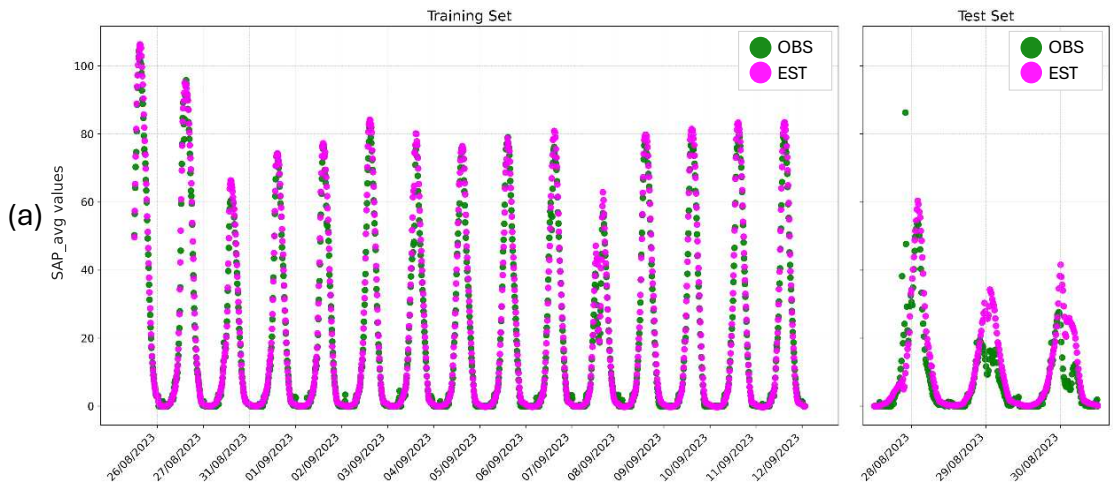
Temporal Estimate (TE) models									
(a) TE-PA					(b) TE-FC				
	Model	RMSE		R2-score		RMSE		R2-score	
		train	test	train	test	train	test	train	test
split1	SVR	5.897	7.249	0.943	0.926	6.356	8.310	0.934	0.903
	MLPR	4.067	6.888	0.973	0.933	5.542	9.097	0.950	0.884
split2	SVR	2.485	9.519	0.991	0.409	2.746	8.169	0.989	0.565
	MLPR	2.274	7.347	0.993	0.648	2.833	6.816	0.989	0.697
split3	SVR	5.153	3.553	0.962	0.947	3.391	3.011	0.983	0.967
	MLPR	2.762	3.889	0.989	0.937	4.064	2.816	0.976	0.971

541



542

543 **Fig. 12** SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 2
544 hours temporal windows using MLPR model (split1)



545

546

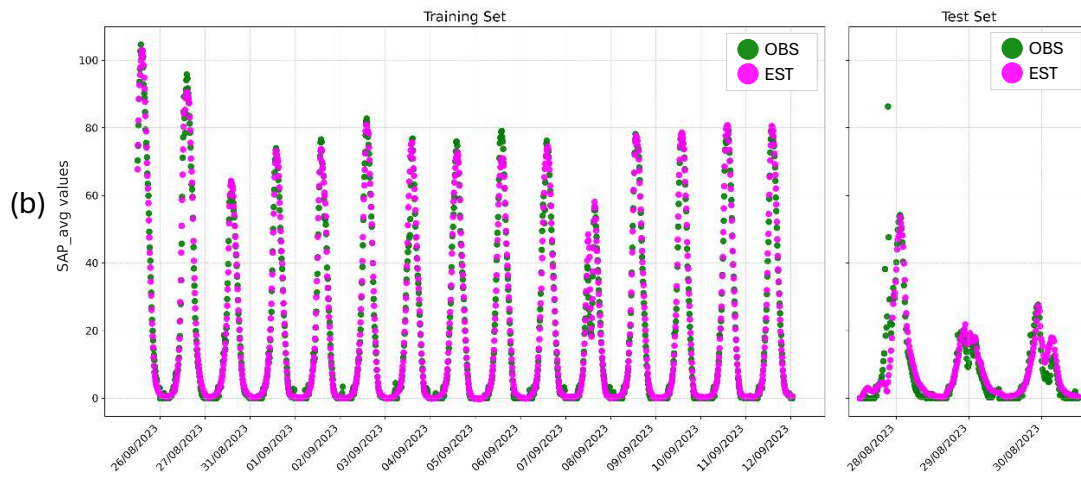


Fig. 13 SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 2 hours temporal windows using MLPR model (split2)

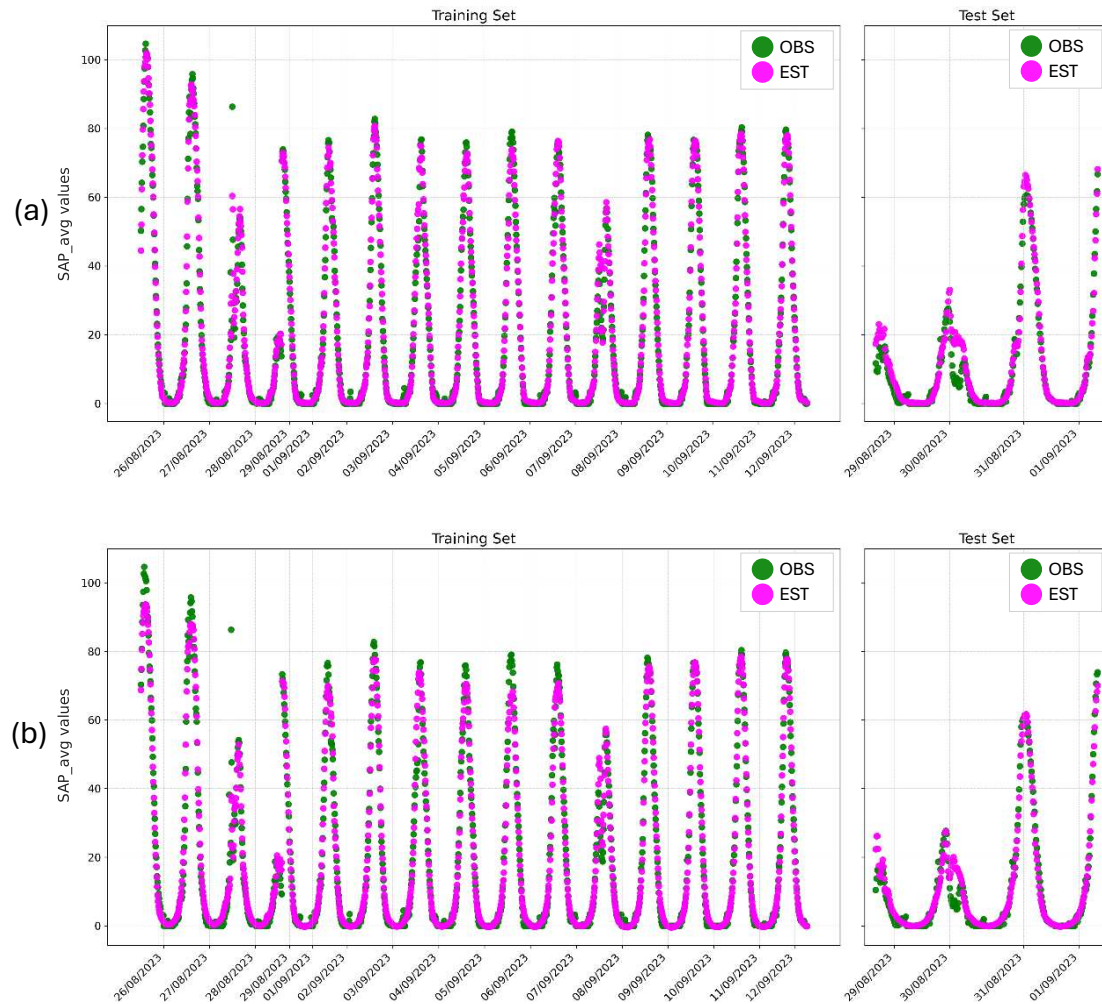


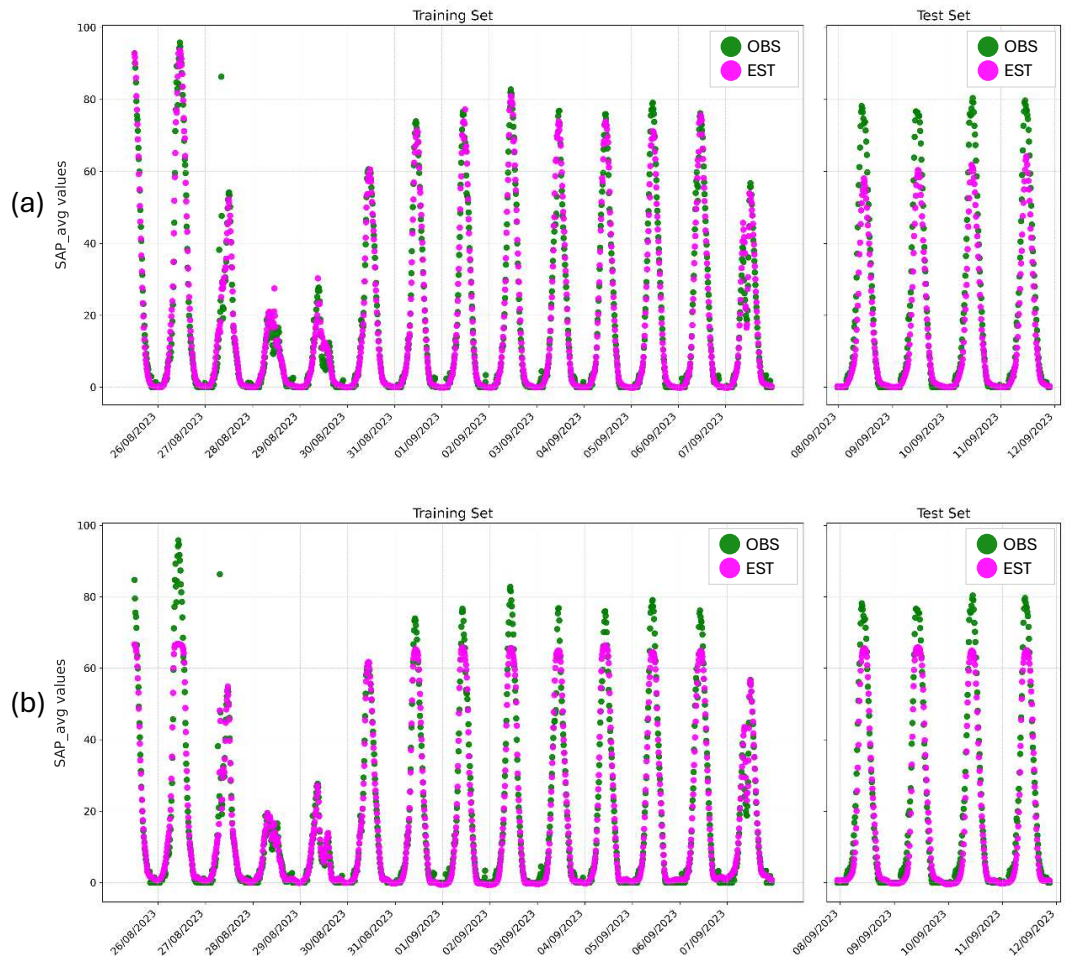
Fig. 14 SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 2 hours temporal windows using MLPR model (split3)

555 **6 hours temporal windows for TE-PA and TE-FC strategies**

556 The results concatenating the average (TE-PA) of the previous 24 samples (6 hours) are shown
557 below along with those obtained by directly concatenating features (TE-FC). Table 8 reports the
558 quantitative metrics, while Figures 15, 16, 17 depict the corresponding outcomes for each split.

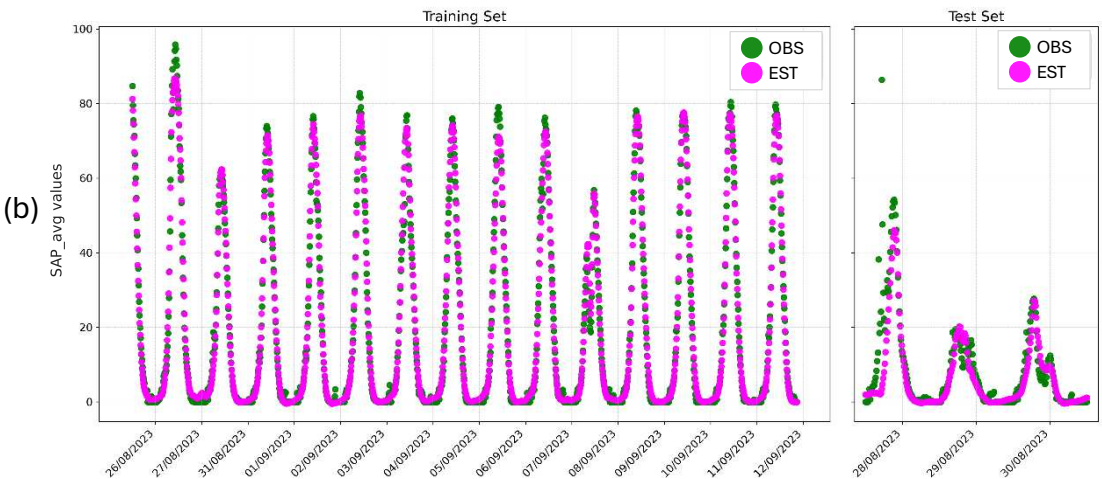
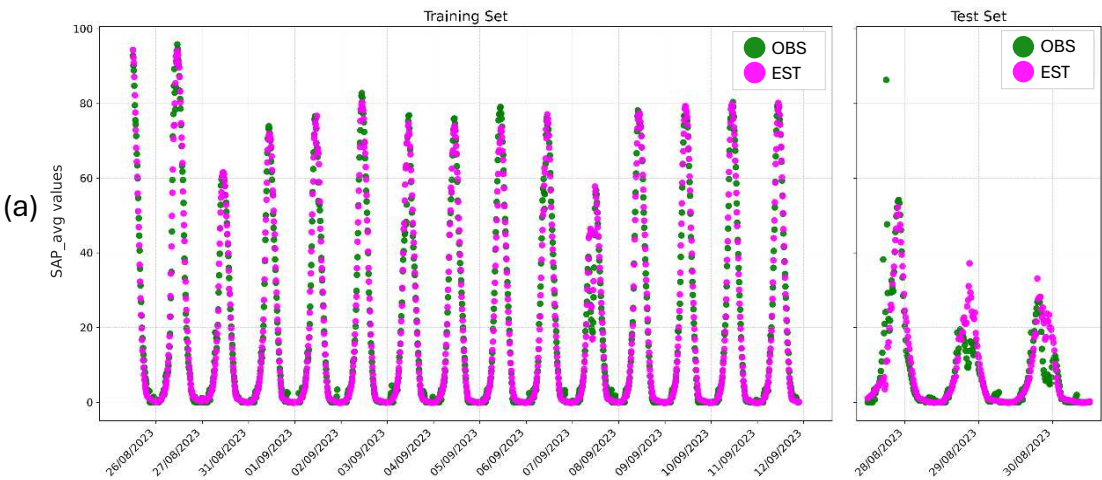
559 **Table 8** Results of SVR and MLPR with best hyperparameters found with GridSearchCV.

Temporal Estimate (TE) models									
(a) TE-PA					(b) TE-FC				
	Model	RMSE		R2-score		RMSE		R2-score	
		train	test	train	test	train	test	train	test
split1	SVR	6.322	9.035	0.928	0.886	5.112	8.508	0.952	0.899
	MLPR	3.266	8.772	0.981	0.892	4.069	5.335	0.969	0.960
split2	SVR	2.893	8.932	0.987	0.480	2.450	10.547	0.991	0.275
	MLPR	3.146	7.073	0.985	0.674	2.742	7.281	0.988	0.655
split3	SVR	3.297	4.432	0.983	0.948	3.496	3.773	0.980	0.963
	MLPR	3.065	3.783	0.985	0.962	2.493	2.653	0.99	0.981



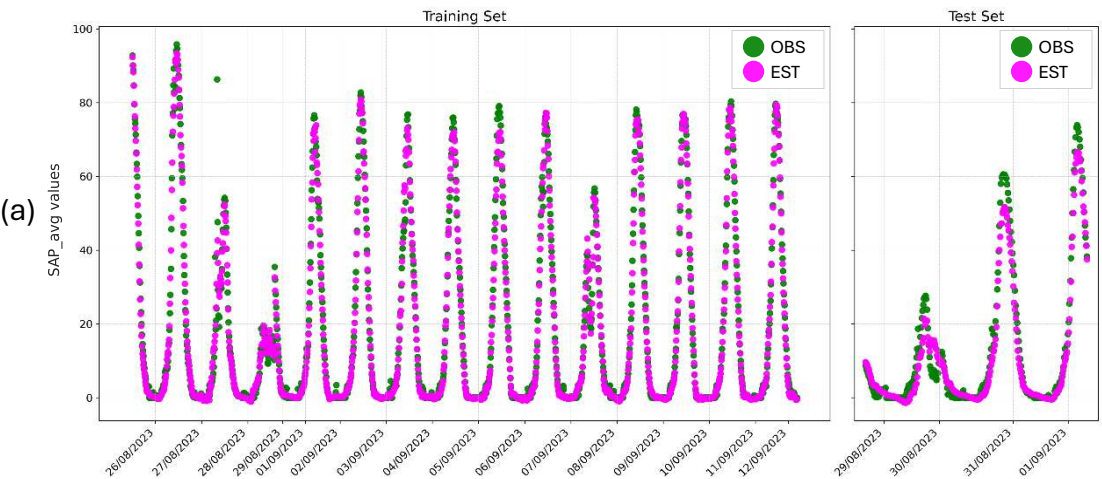
560
561 **Fig. 15** SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 6
562 hours temporal windows using MLPR model (split1)

563



564

565 **Fig. 16** SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 6
566 hours temporal windows using MLPR model (split2)



567

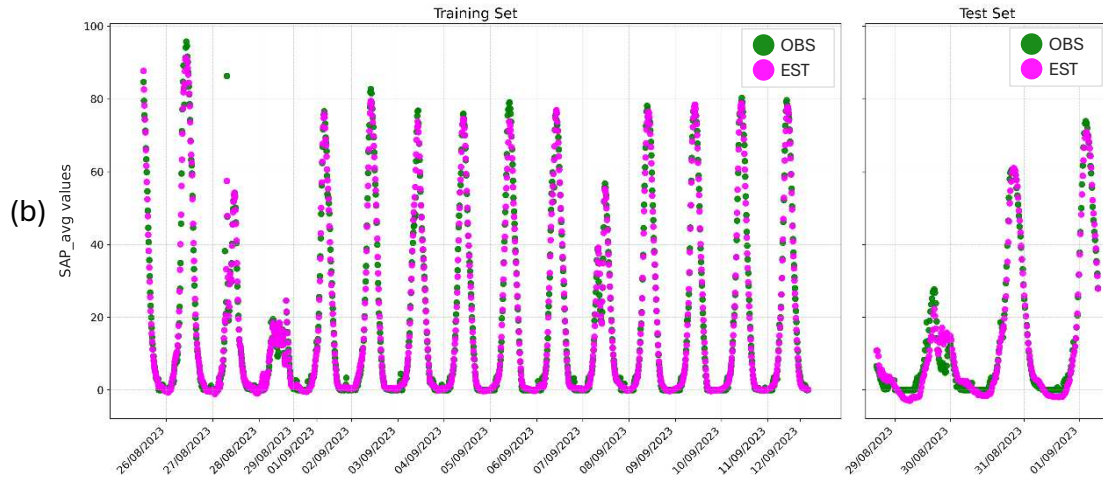


Fig. 17 SAP_avg estimated values, EST, compared against observed ones, OBS, for TE-PA (a) and TE-FC (b) with 6 hours temporal windows using MLPR model (split3)

Experiments with 2024 data

Quantitative results for 2024 are reported in Table 9, and qualitative outcomes for the MLPR model are shown in Figures 18 and 19. The differences observed between RMSE and R^2 across Exp1 and Exp2 (Section “Data partitioning for 2024”) are mainly explained by the variability of the target values in the corresponding test sets. In exp1, SAP_avg exhibits a much wider dynamic range, which increases the total variance of the ground truth and makes the R^2 metric less sensitive to large absolute errors. Conversely, the test set of exp2 shows a markedly lower variability, resulting in a smaller total variance; under these conditions, errors of comparable magnitude become proportionally more penalizing in the computation of R^2 , leading to higher RMSE but comparatively higher R^2 scores.

Table 9 Results of SVR and MLPR with best hyperparameters found with GridSearchCV

	Model	RMSE		R2-score	
		train	test	train	test
exp1	SVR	4.392	16.535	0.970	0.796
	MLPR	4.261	15.152	0.971	0.828
exp2	SVR	5.948	7.431	0.969	0.932
	MLPR	5.291	9.208	0.976	0.896

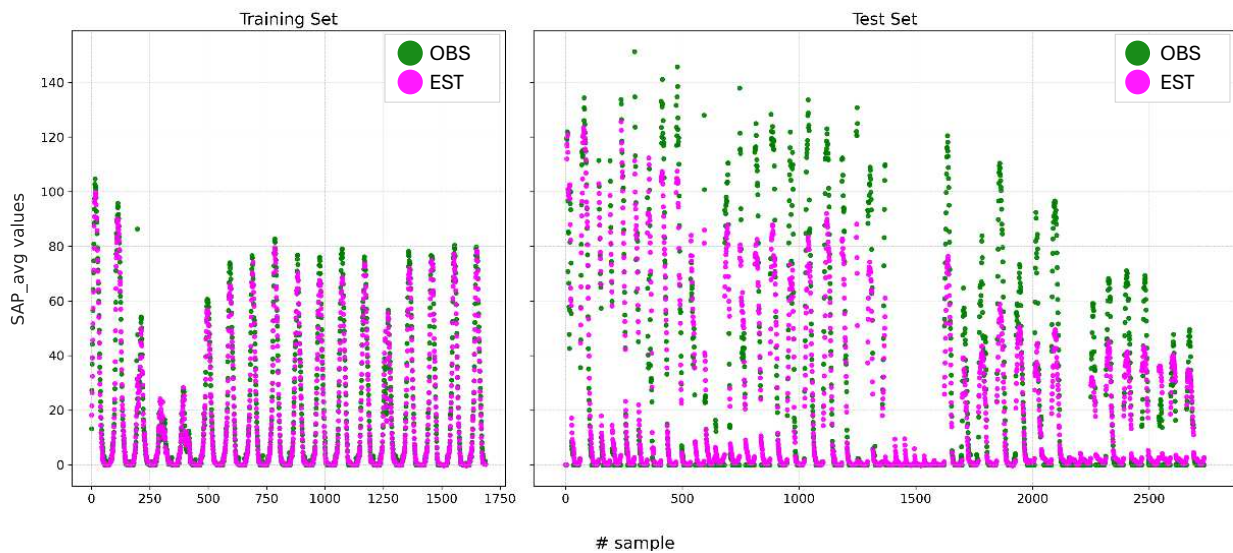


Fig. 18. SAP_avg values compared against observed ones for exp1 with MLPR model

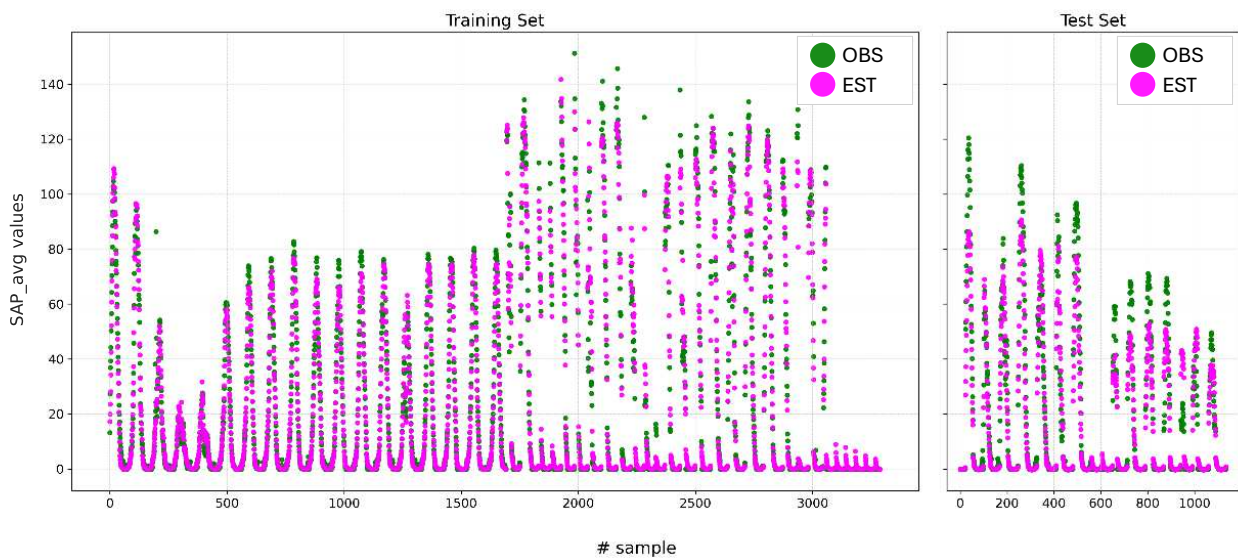


Fig. 19 SAP_avg values compared against observed ones for exp2 with MLPR model

Discussions

2023 data

Considering the results reported in the preceding figures and tables, the influence of historical information on the estimation of SAP_avg becomes clearer when comparing Point Estimate (PE) and Temporal Estimate (TE) strategies. Since LR and DTR showed limited predictive capability in the PE experiments, either because of poor generalization or evident overfitting, only the two best-performing models, MLPR and SVR, were retained for the temporal analyses.

For both MLPR and SVR, past observations affect performance in a way that depends on the temporal window and on the dataset split. Short windows, such as 45 minutes and 2 hours, generally provide stable improvements across most configurations, since they introduce additional temporal context without excessively smoothing the signal. This effect is not uniform across splits. In split1, short windows often yield the best balance between RMSE and R^2 , while

in split3 longer windows, particularly when using feature concatenation (TE-FC), frequently lead to the highest overall performance. This behaviour is consistent with the smoother temporal structure of the split3 test set, which benefits more from extended temporal information.

The TE-FC approach accentuates these differences. By treating each previous sample as an independent feature, it increases the dimensionality of the input space and allows the model, especially MLPR, to reconstruct the daily pattern of the sap flow signal more effectively. As a result, R^2 can rise substantially when the window is extended to 6 hours, even when RMSE does not improve to the same extent. This indicates that part of the gain comes from a better reproduction of the overall signal shape rather than from a uniform reduction in prediction errors (RMSE). In contrast, TE-PA, which relies on averaging past samples, tends to provide more conservative improvements, with limited benefits from longer windows, especially in split1 and split2.

Clear differences emerge when model performance is evaluated across the different data splits. In split2, both MLPR and SVR consistently achieve the lowest performance, as the reduced variability and irregular dynamics of the test set lead to higher RMSE values and lower R^2 scores across all temporal windows and for both temporal strategies. In split1, the models generally perform well when short temporal windows are used, although this configuration does not systematically yield the best results. In contrast, when evaluated on split3, the models, particularly under the TE-FC strategy with longer temporal windows, often achieve their highest performance. This behaviour can be attributed to the statistical properties of the split3 test set, which combines mixed yet smoother sap-flow dynamics. Under these conditions, the additional temporal context allows the models to better reconstruct the daily transpiration pattern, resulting in improved R^2 values.

Overall, the results show that the benefit of incorporating historical data depends strongly on both the temporal strategy and the characteristics of the test set. Short windows remain the most consistently reliable option, although longer windows combined with TE-FC can provide substantial improvements when the target signal exhibits regular and slowly varying dynamics, as observed in split3.

2024 data

Despite the technical discontinuities in the 2024 dataset, the stable predictive performance of MLPR and SVR confirms the robustness of the proposed framework. The results indicate that the models can generalize effectively across growing seasons when properly trained and that combining data from multiple years enhances adaptability and reliability.

Overall, these results suggest that ML-based models trained on multi-season data can effectively generalize across different growth cycles, provided that missing data are properly handled, and the feature set remains consistent. The differences observed between the two years mainly result from the data completeness rather than the intrinsic behaviour of the models, emphasizing the importance of continuous and high-quality data acquisition for reliable estimation of sap flow and transpiration in field conditions.

641 **Conclusions**

642 This study demonstrated the potential of data-driven frameworks to estimate maize sap flow
643 transpiration using widely available climatic and soil moisture data. The comparative analysis
644 of multiple machine learning models revealed that non-linear architectures, particularly MLPR
645 and SVR, consistently outperform linear and tree-based approaches in both point and temporal
646 estimation tasks.

647 A key finding of this research is that incorporating short-term historical information, specifically
648 temporal windows of 45 minutes and 2 hours, significantly enhances predictive accuracy by
649 providing relevant temporal context while preserving the intrinsic dynamics of the sap flow
650 signal. In contrast, extending the temporal horizon beyond a few hours (e.g., 3–4 hours) tends
651 to reduce reliability, as the process follows a pronounced 12-hour diurnal cycle with rapid
652 daytime variations and near-zero night-time values.

653 Specifically, the Feature Concatenation (TE-FC) strategy allowed models to better reconstruct
654 the complex patterns of transpiration, providing a more reliable estimation of crop water
655 demand compared to traditional instantaneous predictors. The results obtained for the 2023
656 dataset show that concatenation strategies allow the models to better reconstruct the diurnal
657 transpiration pattern, leading to higher R^2 values, although these gains do not always
658 correspond to proportional reductions in RMSE. In contrast, the previous-averages approach
659 provides more conservative improvements, typically yielding more stable error behaviour but
660 limited benefits when longer temporal windows are considered. The effectiveness of temporal
661 information was shown to depend strongly on the statistical properties of the test data,
662 highlighting the importance of dataset characteristics when evaluating model performance.

663 The analysis conducted on the 2024 dataset confirms the robustness of the selected models
664 under more challenging conditions, including data discontinuities and interannual variability.
665 The 2024 database encompasses measurements collected under markedly different
666 meteorological conditions, soil states, and crop responses, thus providing a broader and more
667 representative characterization of sap flow dynamics that is essential for an effective and
668 unbiased model training process. Despite the restriction to point estimation, MLPR and SVR
669 demonstrated good generalization capability across growing seasons, particularly when multi-
670 year data were combined during training.

671 Overall, the proposed modelling framework offers an effective and minimally invasive tool for
672 estimating maize sap flow. These findings support the applicability of machine learning-based
673 approaches for real-time irrigation management and decision support in precision agriculture.
674 Future work will focus on extending temporal modelling to longer and more continuous
675 datasets and on integrating additional data sources, such as remote sensing or plant
676 physiological indicators, to further enhance model robustness and scalability.

677 **Statements and Declarations**

678 **Author contributions** T.G.: Data curation; Formal analysis; Investigation; Methodology;
679 Resources; Supervision; Validation; Visualization; Writing – original draft; Writing – review and
680 editing. L.M.: Data curation; Formal analysis; Investigation; Methodology; Resources;
681 Software; Supervision; Validation; Visualization; Writing – original draft; Writing – review and

682 editing. C.F.: Formal analysis; Investigation; Methodology; Writing – review and editing. C.G.:
683 Conceptualization; Investigation; Methodology; Supervision; Validation; Visualization; Writing
684 – review and editing. B.J.: Data curation; Methodology; Resources; Writing – review and editing.
685 V.L.: Data curation; Methodology; Resources; Writing – review and editing. V.P.: Funding
686 acquisition; Project administration; Supervision. T.F.: Conceptualization; Data curation; Formal
687 analysis; Funding acquisition; Investigation; Methodology; Project administration; Supervision;
688 Validation; Visualization; Writing – original draft; Writing – review and editing.

689 **Data availability** Part of the datasets generated and analyzed during the current study are
690 publicly available at [https://github.com/isarlab-department-](https://github.com/isarlab-department-engineering/Agritech3.1.5FIWARE)
691 [engineering/Agritech3.1.5FIWARE](https://github.com/isarlab-department-engineering/Agritech3.1.5FIWARE). The source code used for data processing and analysis will
692 be released upon acceptance of the paper in the GitHub repository [https://github.com/isarlab-](https://github.com/isarlab-department-engineering/DD_Maize_Sap_Flow)
693 [department-engineering/DD_Maize_Sap_Flow](https://github.com/isarlab-department-engineering/DD_Maize_Sap_Flow).

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698 **Declarations**

699 **Competing Interests** The authors declare that they have no known competing financial or
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