

```
!pip -q install pandas numpy matplotlib scikit-learn shap lime
```

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt

from sklearn.ensemble import RandomForestRegressor
from sklearn.model_selection import LeaveOneOut
from sklearn.metrics import r2_score, mean_absolute_error, mean_squared_error
from sklearn.inspection import permutation_importance, PartialDependenceDisplay

SEED = 42
np.random.seed(SEED)
```

```
# Run, A (mg), B (min), Y1 (solubility), Y2 (%CDR)
data = [
    (1, 600.0000, 7.00000, 52.79, 79.56),
    (2, 400.0000, 18.50000, 47.37, 71.48),
    (3, 400.0000, 18.50000, 42.23, 67.37),
    (4, 600.0000, 30.00000, 65.86, 85.93),
    (5, 400.0000, 18.50000, 46.70, 76.48),
    (6, 200.0000, 7.00000, 21.50, 33.89),
    (7, 400.0000, 34.76350, 52.28, 79.33),
    (8, 400.0000, 18.50000, 37.15, 62.15),
    (9, 200.0000, 30.00000, 35.64, 57.03),
    (10, 400.0000, 18.50000, 41.56, 66.46),
    (11, 682.8430, 18.50000, 74.63, 95.73),
    (12, 117.1570, 18.50000, 17.31, 26.08),
    (13, 400.0000, 2.23654, 9.83, 25.31),
]

df = pd.DataFrame(data, columns=["Run", "A", "B", "Y1", "Y2"])
display(df)
print(df.describe())
```

|       | Run      | A          | B         | Y1        | Y2        |
|-------|----------|------------|-----------|-----------|-----------|
| 0     | 1        | 600.000    | 7.00000   | 52.79     | 79.56     |
| 1     | 2        | 400.000    | 18.50000  | 47.37     | 71.48     |
| 2     | 3        | 400.000    | 18.50000  | 42.23     | 67.37     |
| 3     | 4        | 600.000    | 30.00000  | 65.86     | 85.93     |
| 4     | 5        | 400.000    | 18.50000  | 46.70     | 76.48     |
| 5     | 6        | 200.000    | 7.00000   | 21.50     | 33.89     |
| 6     | 7        | 400.000    | 34.76350  | 52.28     | 79.33     |
| 7     | 8        | 400.000    | 18.50000  | 37.15     | 62.15     |
| 8     | 9        | 200.000    | 30.00000  | 35.64     | 57.03     |
| 9     | 10       | 400.000    | 18.50000  | 41.56     | 66.46     |
| 10    | 11       | 682.843    | 18.50000  | 74.63     | 95.73     |
| 11    | 12       | 117.157    | 18.50000  | 17.31     | 26.08     |
| 12    | 13       | 400.000    | 2.23654   | 9.83      | 25.31     |
|       | Run      | A          | B         | Y1        | Y2        |
| count | 13.00000 | 13.000000  | 13.000000 | 13.000000 | 13.000000 |
| mean  | 7.00000  | 400.000000 | 18.500003 | 41.911538 | 63.600000 |
| std   | 3.89444  | 163.299399 | 9.389718  | 18.339206 | 22.519117 |
| min   | 1.00000  | 117.157000 | 2.236540  | 9.830000  | 25.310000 |
| 25%   | 4.00000  | 400.000000 | 18.500000 | 35.640000 | 57.030000 |
| 50%   | 7.00000  | 400.000000 | 18.500000 | 42.230000 | 67.370000 |
| 75%   | 10.00000 | 400.000000 | 18.500000 | 52.280000 | 79.330000 |
| max   | 13.00000 | 682.843000 | 34.763500 | 74.630000 | 95.730000 |

```
import numpy as np

# Validation points: R1, R9, Optimized
val_points = [(600.0, 7.0), (200.0, 30.0), (600.0, 30.0)]

def is_val_point(a, b):
    return any(np.isclose(a, aa) and np.isclose(b, bb) for aa, bb in val_points)

# df must already exist with columns: A, B, Y1, Y2
mask_val = df.apply(lambda r: is_val_point(r["A"], r["B"]), axis=1)

train_df = df.loc[~mask_val].copy()
val_df = df.loc[mask_val].copy()

print("Training n =", len(train_df), " Validation n =", len(val_df))
display(train_df)
display(val_df)
```

Training n = 10    Validation n = 3

|    | Run | A       | B        | Y1    | Y2    |
|----|-----|---------|----------|-------|-------|
| 1  | 2   | 400.000 | 18.50000 | 47.37 | 71.48 |
| 2  | 3   | 400.000 | 18.50000 | 42.23 | 67.37 |
| 4  | 5   | 400.000 | 18.50000 | 46.70 | 76.48 |
| 5  | 6   | 200.000 | 7.00000  | 21.50 | 33.89 |
| 6  | 7   | 400.000 | 34.76350 | 52.28 | 79.33 |
| 7  | 8   | 400.000 | 18.50000 | 37.15 | 62.15 |
| 9  | 10  | 400.000 | 18.50000 | 41.56 | 66.46 |
| 10 | 11  | 682.843 | 18.50000 | 74.63 | 95.73 |
| 11 | 12  | 117.157 | 18.50000 | 17.31 | 26.08 |
| 12 | 13  | 400.000 | 2.23654  | 9.83  | 25.31 |

|   | Run | A     | B    | Y1    | Y2    |
|---|-----|-------|------|-------|-------|
| 0 | 1   | 600.0 | 7.0  | 52.79 | 79.56 |
| 3 | 4   | 600.0 | 30.0 | 65.86 | 85.93 |
| 8 | 9   | 200.0 | 30.0 | 35.64 | 57.03 |

```
X_train = train_df[["A","B"]]
y1_train = train_df["Y1"].values
y2_train = train_df["Y2"].values

rf_y1 = RandomForestRegressor(n_estimators=800, random_state=SEED)
rf_y2 = RandomForestRegressor(n_estimators=800, random_state=SEED)

rf_y1.fit(X_train, y1_train)
rf_y2.fit(X_train, y2_train)

print("RF models trained.")
```

RF models trained.

```
import numpy as np
import pandas as pd
from copy import deepcopy
from sklearn.model_selection import LeaveOneOut
from sklearn.metrics import r2_score, mean_absolute_error, mean_squared_error

def loocv_predict(model, X, y):
    loo = LeaveOneOut()
    preds = np.zeros(len(y), dtype=float)

    for tr, te in loo.split(X):
        m = deepcopy(model)
        m.fit(X.iloc[tr], y[tr])
        preds[te[0]] = m.predict(X.iloc[te])[0]

    return preds

def report_metrics(y_true, y_pred, label):
    r2 = r2_score(y_true, y_pred)
    mae = mean_absolute_error(y_true, y_pred)
    mse = mean_squared_error(y_true, y_pred) # no squared=False
    rmse = float(np.sqrt(mse)) # RMSE = sqrt(MSE)

    print(f"{label}: R2={r2:.4f} MAE={mae:.4f} RMSE={rmse:.4f}")
    return r2, mae, rmse

# ---- Run LOOCV predictions (RF models must already be trained) ----
pred_loocv_y1 = loocv_predict(rf_y1, X_train, y1_train)
pred_loocv_y2 = loocv_predict(rf_y2, X_train, y2_train)

m_y1 = report_metrics(y1_train, pred_loocv_y1, "RF (LOOCV) Y1")
m_y2 = report_metrics(y2_train, pred_loocv_y2, "RF (LOOCV) Y2")

metrics_table = pd.DataFrame([
    {"Model": "RF", "Response": "Y1", "R2": m_y1[0], "MAE": m_y1[1], "RMSE": m_y1[2]},
    {"Model": "RF", "Response": "Y2", "R2": m_y2[0], "MAE": m_y2[1], "RMSE": m_y2[2]},
])

metrics_table.to_csv("Table_RF_LOOCV_train.csv", index=False)
display(metrics_table)
print("Saved: Table_RF_LOOCV_train.csv")
```

RF (LOOCV) Y1: R2=0.1651    MAE=12.0030    RMSE=16.4042  
RF (LOOCV) Y2: R2=0.2217    MAE=14.4085    RMSE=20.0952

|   | Model | Response | R2       | MAE       | RMSE      |
|---|-------|----------|----------|-----------|-----------|
| 0 | RF    | Y1       | 0.165112 | 12.003022 | 16.404238 |
| 1 | RF    | Y2       | 0.221661 | 14.408530 | 20.095215 |

Saved: Table\_RF\_LOOCV\_train.csv

```

X_val = val_df[["A","B"]]
val_pred_y1 = rf_y1.predict(X_val)
val_pred_y2 = rf_y2.predict(X_val)

# QbD predicted values (Table 4) for comparison
qbd_pred = {
(600.0, 7.0): (48.82, 71.99),
(200.0, 30.0): (34.99, 55.20),
(600.0, 30.0): (70.64, 98.47),
}

val_table = val_df[["Run","A","B","Y1","Y2"]].copy()
val_table["RF_Y1_pred"] = val_pred_y1
val_table["RF_Y2_pred"] = val_pred_y2

val_table["RF_Y1_%error"] = 100*(val_table["RF_Y1_pred"]-val_table["Y1"])/val_table["Y1"]
val_table["RF_Y2_%error"] = 100*(val_table["RF_Y2_pred"]-val_table["Y2"])/val_table["Y2"]

val_table["QbD_Y1_pred"] = val_table.apply(lambda r: qbd_pred[(float(r["A"]), float(r["B"]))][0], axis=1)
val_table["QbD_Y2_pred"] = val_table.apply(lambda r: qbd_pred[(float(r["A"]), float(r["B"]))][1], axis=1)

val_table["QbD_Y1_%error"] = 100*(val_table["QbD_Y1_pred"]-val_table["Y1"])/val_table["Y1"]
val_table["QbD_Y2_%error"] = 100*(val_table["QbD_Y2_pred"]-val_table["Y2"])/val_table["Y2"]

val_table.to_csv("Table_RF_validation_checkpoints.csv", index=False)
display(val_table)
print("Saved: Table_RF_validation_checkpoints.csv")

```

|   | Run | A     | B    | Y1    | Y2    | RF_Y1_pred | RF_Y2_pred | RF_Y1_%error | RF_Y2_%error | QbD_Y1_pred | QbD_Y2_pred | QbD_Y1_%error | QbD_Y2_%error |
|---|-----|-------|------|-------|-------|------------|------------|--------------|--------------|-------------|-------------|---------------|---------------|
| 0 | 1   | 600.0 | 7.0  | 52.79 | 79.56 | 46.676787  | 51.429836  | -11.580247   | -35.357169   | 48.82       | 71.99       | -7.520364     | -9.514832     |
| 3 | 4   | 600.0 | 30.0 | 65.86 | 85.93 | 66.092435  | 89.079350  | 0.352923     | 3.665018     | 70.64       | 98.47       | 7.257820      | 14.593274     |
| 8 | 9   | 200.0 | 30.0 | 35.64 | 57.03 | 28.078118  | 42.132041  | -21.217401   | -26.123022   | 34.99       | 55.20       | -1.823793     | -3.208837     |

Saved: Table\_RF\_validation\_checkpoints.csv

```

import matplotlib.pyplot as plt

def pred_vs_obs(y_true, y_pred, title, filename):
    plt.figure()
    plt.scatter(y_true, y_pred)

    mn = float(min(np.min(y_true), np.min(y_pred)))
    mx = float(max(np.max(y_true), np.max(y_pred)))

    plt.plot([mn, mx], [mn, mx])
    plt.xlabel("Observed")
    plt.ylabel("Predicted (LOOCV)")
    plt.title(title)
    plt.tight_layout()
    plt.savefig(filename, dpi=300)
    plt.close()

# ---- Call the function (these lines must NOT be indented) ----
pred_vs_obs(y1_train, pred_loocv_y1, "RF LOOCV: Predicted vs Observed (Y1)", "Fig_PredVsObs_Y1.png")
pred_vs_obs(y2_train, pred_loocv_y2, "RF LOOCV: Predicted vs Observed (Y2)", "Fig_PredVsObs_Y2.png")

print("Saved: Fig_PredVsObs_Y1.png and Fig_PredVsObs_Y2.png")

```

Saved: Fig\_PredVsObs\_Y1.png and Fig\_PredVsObs\_Y2.png

```

import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import shap

# Use TRAIN set for explanations (recommended)
# Make sure these exist before running:
# df, X_train, y1_train, y2_train, rf_y1, rf_y2

# ----- Y1 -----
explainer_y1 = shap.TreeExplainer(rf_y1)
shap_exp_y1 = explainer_y1(X_train) # Explanation object

# Summary plot (beeswarm)
shap.summary_plot(shap_exp_y1.values, X_train, show=False)
plt.tight_layout()
plt.savefig("Fig_SHAP_summary_Y1.png", dpi=300)
plt.close()

# Dependence plots (A and B)
for feat in ["A", "B"]:
    shap.dependence_plot(feat, shap_exp_y1.values, X_train, show=False)
    plt.tight_layout()
    plt.savefig(f"Fig_SHAP_dependence_Y1_{feat}.png", dpi=300)
    plt.close()

# Local SHAP waterfall: highest and lowest observed Y1 within TRAIN
idx_hi = int(np.argmax(y1_train))
idx_lo = int(np.argmin(y1_train))

```

```

for name, idx in [("high", idx_hi), ("low", idx_lo)]:
    shap.plots.waterfall(shap_exp_y1[idx], show=False)
    plt.tight_layout()
    plt.savefig(f"Fig_SHAP_waterfall_Y1_{name}.png", dpi=300)
    plt.close()

print("Saved SHAP figures for Y1")

# ----- Y2 -----
explainer_y2 = shap.TreeExplainer(rf_y2)
shap_exp_y2 = explainer_y2(X_train)

shap.summary_plot(shap_exp_y2.values, X_train, show=False)
plt.tight_layout()
plt.savefig("Fig_SHAP_summary_Y2.png", dpi=300)
plt.close()

for feat in ["A", "B"]:
    shap.dependence_plot(feat, shap_exp_y2.values, X_train, show=False)
    plt.tight_layout()
    plt.savefig(f"Fig_SHAP_dependence_Y2_{feat}.png", dpi=300)
    plt.close()

idx_hi2 = int(np.argmax(y2_train))
idx_lo2 = int(np.argmin(y2_train))

for name, idx in [("high", idx_hi2), ("low", idx_lo2)]:
    shap.plots.waterfall(shap_exp_y2[idx], show=False)
    plt.tight_layout()
    plt.savefig(f"Fig_SHAP_waterfall_Y2_{name}.png", dpi=300)
    plt.close()

print("Saved SHAP figures for Y2")

# ----- SHAP global importance table -----
imp_y1 = np.abs(shap_exp_y1.values).mean(axis=0)
imp_y2 = np.abs(shap_exp_y2.values).mean(axis=0)

shap_table = pd.DataFrame({
    "Feature": list(X_train.columns),
    "mean_abs_SHAP_Y1": imp_y1,
    "mean_abs_SHAP_Y2": imp_y2
})

shap_table.to_csv("Table_SHAP_importance.csv", index=False)
display(shap_table)
print("Saved: Table_SHAP_importance.csv")

```

```

/tmp/ipython-input-1010726122.py:15: FutureWarning: The NumPy global RNG was seeded by calling `np.random.seed`. In a future version this function will no longer use th
    shap.summary_plot(shap_exp_y1.values, X_train, show=False)
Saved SHAP figures for Y1
/tmp/ipython-input-1010726122.py:43: FutureWarning: The NumPy global RNG was seeded by calling `np.random.seed`. In a future version this function will no longer use th
    shap.summary_plot(shap_exp_y2.values, X_train, show=False)
Saved SHAP figures for Y2

```

|   | Feature | mean_abs_SHAP_Y1 | mean_abs_SHAP_Y2 |
|---|---------|------------------|------------------|
| 0 | A       | 5.219187         | 8.014233         |
| 1 | B       | 5.724004         | 8.042018         |

Saved: Table\_SHAP\_importance.csv

```

import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.inspection import permutation_importance

# SEED must exist; if not, define it
try:
    SEED
except NameError:
    SEED = 42

def run_pfi(model, X, y, title, out_csv, out_png):
    r = permutation_importance(
        model, X, y,
        scoring="neg_mean_absolute_error",
        n_repeats=200,
        random_state=SEED
    )

    pfi = pd.DataFrame({
        "Feature": list(X.columns),
        "Importance_mean": r.importances_mean,
        "Importance_std": r.importances_std
    }).sort_values("Importance_mean", ascending=False)

    pfi.to_csv(out_csv, index=False)

    plt.figure()
    plt.bar(pfi["Feature"], pfi["Importance_mean"], yerr=pfi["Importance_std"])
    plt.ylabel("PFI (increase in MAE units)")
    plt.title(title)
    plt.tight_layout()
    plt.savefig(out_png, dpi=300)
    plt.close()

```

```

    return pfi

# ---- Run PFI on TRAIN set ----
pfi_y1 = run_pfi(rf_y1, X_train, y1_train, "Permutation Feature Importance (RF-Y1)", "Table_PFI_Y1.csv", "Fig_PFI_Y1.png")
pfi_y2 = run_pfi(rf_y2, X_train, y2_train, "Permutation Feature Importance (RF-Y2)", "Table_PFI_Y2.csv", "Fig_PFI_Y2.png")

display(pfi_y1)
display(pfi_y2)
print("Saved: Table_PFI_Y1.csv, Fig_PFI_Y1.png, Table_PFI_Y2.csv, Fig_PFI_Y2.png")

```

|   | Feature | Importance_mean | Importance_std |
|---|---------|-----------------|----------------|
| 0 | A       | 6.928346        | 2.151580       |
| 1 | B       | 5.020840        | 1.816498       |

  

|   | Feature | Importance_mean | Importance_std |
|---|---------|-----------------|----------------|
| 0 | A       | 8.846882        | 3.002529       |
| 1 | B       | 6.997089        | 2.700590       |

Saved: Table\_PFI\_Y1.csv, Fig\_PFI\_Y1.png, Table\_PFI\_Y2.csv, Fig\_PFI\_Y2.png

```

# 1D PDP
fig, ax = plt.subplots(1, 2, figsize=(10,4))
PartialDependenceDisplay.from_estimator(rf_y1, X_train, ["A"], ax=ax[0], grid_resolution=50)
PartialDependenceDisplay.from_estimator(rf_y1, X_train, ["B"], ax=ax[1], grid_resolution=50)
plt.suptitle("PDP (1D) - RF-Y1")
plt.tight_layout()
plt.savefig("Fig_PDP1D_Y1.png", dpi=300)
plt.close()

fig, ax = plt.subplots(1, 2, figsize=(10,4))
PartialDependenceDisplay.from_estimator(rf_y2, X_train, ["A"], ax=ax[0], grid_resolution=50)
PartialDependenceDisplay.from_estimator(rf_y2, X_train, ["B"], ax=ax[1], grid_resolution=50)
plt.suptitle("PDP (1D) - RF-Y2")
plt.tight_layout()
plt.savefig("Fig_PDP1D_Y2.png", dpi=300)
plt.close()

# 2D PDP
fig, ax = plt.subplots(figsize=(6,5))
PartialDependenceDisplay.from_estimator(rf_y1, X_train, [("A","B")], ax=ax, grid_resolution=40)
plt.title("PDP (2D AxB) - RF-Y1")
plt.tight_layout()
plt.savefig("Fig_PDP2D_Y1.png", dpi=300)
plt.close()

fig, ax = plt.subplots(figsize=(6,5))
PartialDependenceDisplay.from_estimator(rf_y2, X_train, [("A","B")], ax=ax, grid_resolution=40)
plt.title("PDP (2D AxB) - RF-Y2")
plt.tight_layout()
plt.savefig("Fig_PDP2D_Y2.png", dpi=300)
plt.close()

# ICE
fig, ax = plt.subplots(figsize=(6,4))
PartialDependenceDisplay.from_estimator(rf_y1, X_train, ["A"], kind="individual", ax=ax, grid_resolution=50)
plt.title("ICE - A on RF-Y1")
plt.tight_layout()
plt.savefig("Fig_ICE_Y1_A.png", dpi=300)
plt.close()

fig, ax = plt.subplots(figsize=(6,4))
PartialDependenceDisplay.from_estimator(rf_y1, X_train, ["B"], kind="individual", ax=ax, grid_resolution=50)
plt.title("ICE - B on RF-Y1")
plt.tight_layout()
plt.savefig("Fig_ICE_Y1_B.png", dpi=300)
plt.close()

fig, ax = plt.subplots(figsize=(6,4))
PartialDependenceDisplay.from_estimator(rf_y2, X_train, ["A"], kind="individual", ax=ax, grid_resolution=50)
plt.title("ICE - A on RF-Y2")
plt.tight_layout()
plt.savefig("Fig_ICE_Y2_A.png", dpi=300)
plt.close()

fig, ax = plt.subplots(figsize=(6,4))
PartialDependenceDisplay.from_estimator(rf_y2, X_train, ["B"], kind="individual", ax=ax, grid_resolution=50)
plt.title("ICE - B on RF-Y2")
plt.tight_layout()
plt.savefig("Fig_ICE_Y2_B.png", dpi=300)
plt.close()

print("Saved PDP/ICE figures")

```

Saved PDP/ICE figures

```
!pip -q install lime
```

```
275.7/275.7 kB 12.4 MB/s eta 0:00:00  
Preparing metadata (setup.py) ... done  
Building wheel for lime (setup.py) ... done
```

```
import numpy as np  
import pandas as pd  
from lime.lime_tabular import LimeTabularExplainer  
  
# Make sure these exist before running:  
# X_train, rf_y1, rf_y2, SEED  
  
feature_names = list(X_train.columns)  
  
lime_explainer = LimeTabularExplainer(  
    training_data=X_train.values,  
    feature_names=feature_names,  
    mode="regression",  
    discretize_continuous=True,  
    random_state=SEED  
)  
  
# Wrapper functions (must return a 1D array of predictions)  
def predict_y1(arr):  
    arr_df = pd.DataFrame(arr, columns=feature_names)  
    return rf_y1.predict(arr_df)  
  
def predict_y2(arr):  
    arr_df = pd.DataFrame(arr, columns=feature_names)  
    return rf_y2.predict(arr_df)  
  
# Choose one "best" and one "worst" point based on RF predictions (within TRAIN)  
pred_train_y1 = rf_y1.predict(X_train)  
idx_best = int(np.argmax(pred_train_y1))  
idx_worst = int(np.argmin(pred_train_y1))  
  
NUM_SAMPLES = 5000  
  
for label, idx in [("best", idx_best), ("worst", idx_worst)]:  
    # Explain Y1  
    exp1 = lime_explainer.explain_instance(  
        data_row=X_train.values[idx],  
        predict_fn=predict_y1,  
        num_features=2,  
        num_samples=NUM_SAMPLES  
    )  
    exp1.save_to_file(f"LIME_Y1_{label}.html")  
  
    # Explain Y2 at the same point (so it's comparable)  
    exp2 = lime_explainer.explain_instance(  
        data_row=X_train.values[idx],  
        predict_fn=predict_y2,  
        num_features=2,  
        num_samples=NUM_SAMPLES  
    )  
    exp2.save_to_file(f"LIME_Y2_{label}.html")  
  
print("Saved: LIME_Y1_best.html, LIME_Y1_worst.html, LIME_Y2_best.html, LIME_Y2_worst.html")  
print("Open them from Colab > Files (left panel) > click the .html files.")
```

```
Saved: LIME_Y1_best.html, LIME_Y1_worst.html, LIME_Y2_best.html, LIME_Y2_worst.html  
Open them from Colab > Files (left panel) > click the .html files.
```

```
import numpy as np  
import pandas as pd  
import matplotlib.pyplot as plt  
  
# ---- Dense grid in A and B ----  
A_grid = np.linspace(df["A"].min(), df["A"].max(), 120)  
B_grid = np.linspace(df["B"].min(), df["B"].max(), 120)  
AA, BB = np.meshgrid(A_grid, B_grid)  
  
grid = pd.DataFrame({"A": AA.ravel(), "B": BB.ravel()})  
Z1 = rf_y1.predict(grid).reshape(AA.shape)  
Z2 = rf_y2.predict(grid).reshape(AA.shape)  
  
# ---- RF contour plots ----  
plt.figure()  
plt.contourf(AA, BB, Z1, levels=20)  
plt.xlabel("A (mg)")  
plt.ylabel("B (min)")  
plt.title("RF contour - Y1")  
plt.tight_layout()  
plt.savefig("Fig_RF_contour_Y1.png", dpi=300)  
plt.close()  
  
plt.figure()  
plt.contourf(AA, BB, Z2, levels=20)  
plt.xlabel("A (mg)")  
plt.ylabel("B (min)")  
plt.title("RF contour - Y2")  
plt.tight_layout()  
plt.savefig("Fig_RF_contour_Y2.png", dpi=300)  
plt.close()
```

```
# ---- Desirability (maximize both) ----
def desirability_max(y, low, high):
    y = np.asarray(y)
    d = np.zeros_like(y, dtype=float)
    d[y >= high] = 1.0
    mid = (y > low) & (y < high)
    d[mid] = (y[mid] - low) / (high - low)
    return d

Y1_low, Y1_high = df["Y1"].min(), df["Y1"].max()
Y2_low, Y2_high = df["Y2"].min(), df["Y2"].max()

d1 = desirability_max(Z1, Y1_low, Y1_high)
d2 = desirability_max(Z2, Y2_low, Y2_high)
D = np.sqrt(d1 * d2)

# ---- Find optimum ----
best_idx = np.unravel_index(np.argmax(D), D.shape)
A_star = float(AA[best_idx])
B_star = float(BB[best_idx])
Y1_star = float(Z1[best_idx])
Y2_star = float(Z2[best_idx])
D_star = float(D[best_idx])

opt = pd.DataFrame([
    "A_opt_mg": A_star,
    "B_opt_min": B_star,
    "Y1_pred": Y1_star,
    "Y2_pred": Y2_star,
    "Overall_desirability": D_star
])

opt.to_csv("Table_RF_optimum.csv", index=False)
display(opt)

# ---- Desirability contour ----
plt.figure()
plt.contourf(AA, BB, D, levels=20)
plt.scatter([A_star], [B_star])
plt.xlabel("A (mg)")
plt.ylabel("B (min)")
plt.title("Overall desirability (RF)")
plt.tight_layout()
plt.savefig("Fig_Desirability_contour.png", dpi=300)
plt.close()

print("Saved: Fig_RF_contour_Y1.png, Fig_RF_contour_Y2.png, Fig_Desirability_contour.png, Table_RF_optimum.csv")
```

|   | A_opt_mg   | B_opt_min | Y1_pred   | Y2_pred  | Overall_desirability |
|---|------------|-----------|-----------|----------|----------------------|
| 0 | 544.986748 | 26.836762 | 66.092435 | 89.07935 | 0.886706             |

Saved: Fig\_RF\_contour\_Y1.png, Fig\_RF\_contour\_Y2.png, Fig\_Desirability\_contour.png, Table\_RF\_optimum.csv

```
import os
from google.colab import files
```

```
!zip -r Results_RF_XAI.zip *.png *.csv *.html
files.download("Results_RF_XAI.zip")
```

```
adding: Fig_Desirability_contour.png (deflated 29%)
adding: Fig_ICE_Y1_A.png (deflated 14%)
adding: Fig_ICE_Y1_B.png (deflated 16%)
adding: Fig_ICE_Y2_A.png (deflated 15%)
adding: Fig_ICE_Y2_B.png (deflated 17%)
adding: Fig_PDP1D_Y1.png (deflated 16%)
adding: Fig_PDP1D_Y2.png (deflated 17%)
adding: Fig_PDP2D_Y1.png (deflated 9%)
adding: Fig_PDP2D_Y2.png (deflated 9%)
adding: Fig_PFI_Y1.png (deflated 30%)
adding: Fig_PFI_Y2.png (deflated 28%)
adding: Fig_PredVsObs_Y1.png (deflated 17%)
adding: Fig_PredVsObs_Y2.png (deflated 17%)
adding: Fig_RF_contour_Y1.png (deflated 32%)
adding: Fig_RF_contour_Y2.png (deflated 32%)
adding: Fig_SHAP_dependence_Y1_A.png (deflated 29%)
adding: Fig_SHAP_dependence_Y1_B.png (deflated 28%)
adding: Fig_SHAP_dependence_Y2_A.png (deflated 31%)
adding: Fig_SHAP_dependence_Y2_B.png (deflated 28%)
adding: Fig_SHAP_summary_Y1.png (deflated 15%)
adding: Fig_SHAP_summary_Y2.png (deflated 16%)
adding: Fig_SHAP_waterfall_Y1_high.png (deflated 19%)
adding: Fig_SHAP_waterfall_Y1_low.png (deflated 18%)
adding: Fig_SHAP_waterfall_Y2_high.png (deflated 19%)
adding: Fig_SHAP_waterfall_Y2_low.png (deflated 19%)
adding: Table_PFI_Y1.csv (deflated 20%)
adding: Table_PFI_Y2.csv (deflated 20%)
adding: Table_RF_LOOCV_train.csv (deflated 24%)
adding: Table_RF_optimum.csv (deflated 20%)
adding: Table_RF_validation_checkpoints.csv (deflated 45%)
adding: Table_SHAP_importance.csv (deflated 19%)
adding: LIME_Y1_best.html (deflated 80%)
adding: LIME_Y1_worst.html (deflated 80%)
adding: LIME_Y2_best.html (deflated 80%)
adding: LIME_Y2_worst.html (deflated 80%)
```

