

# Supplementary Information

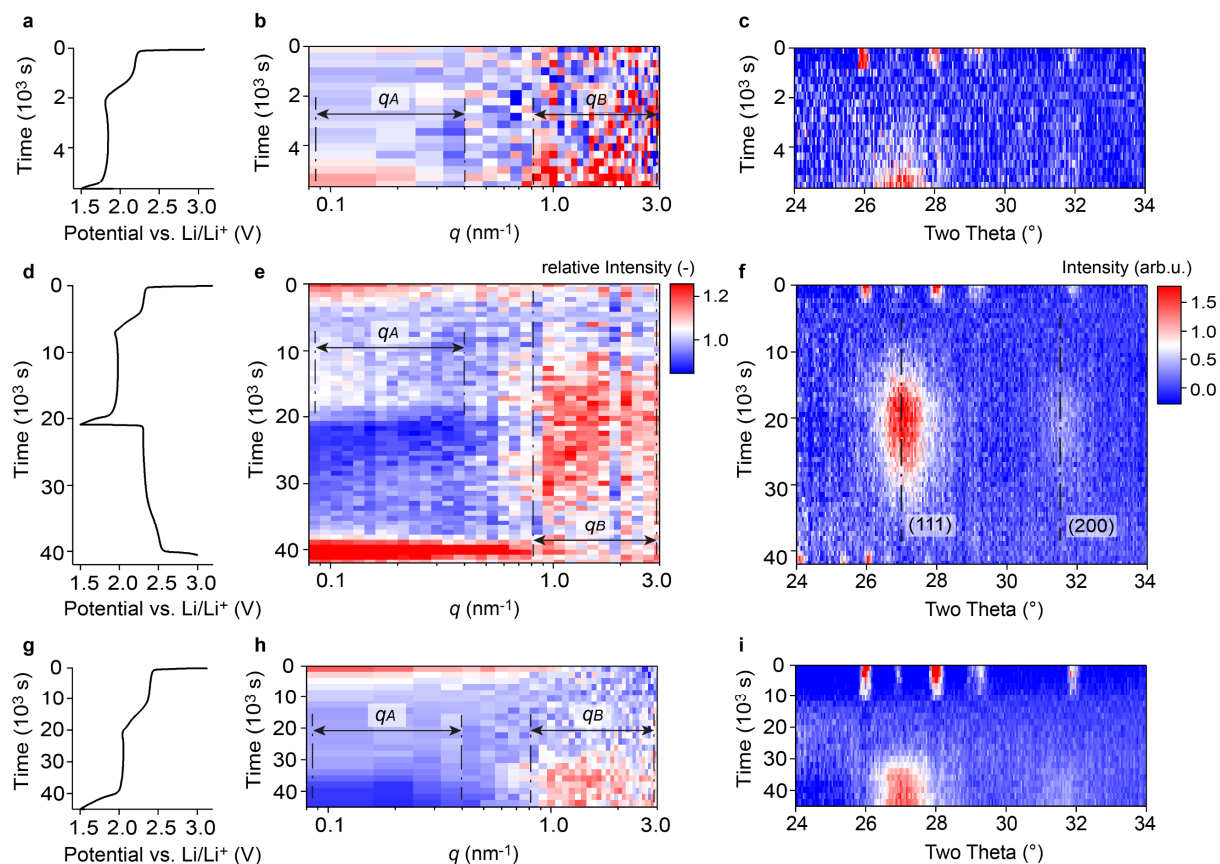
## Mechanism of Li<sub>2</sub>S formation and dissolution in Lithium-Sulphur batteries

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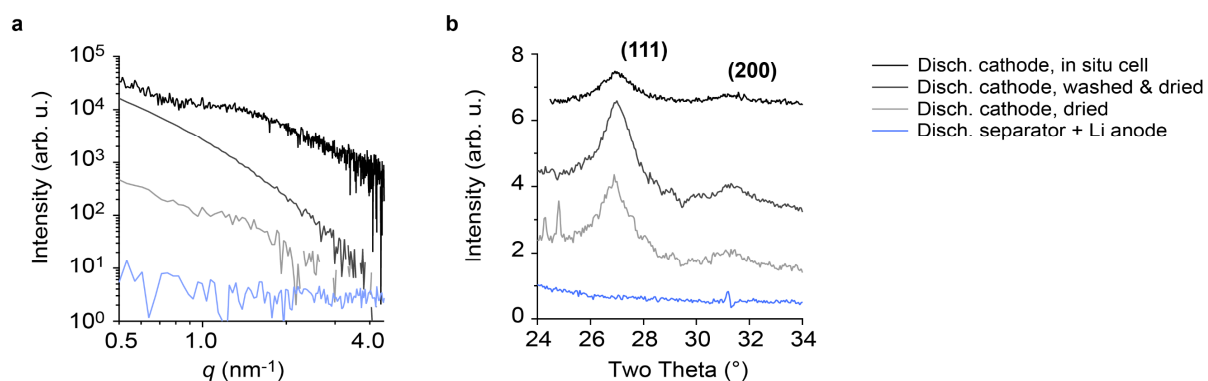
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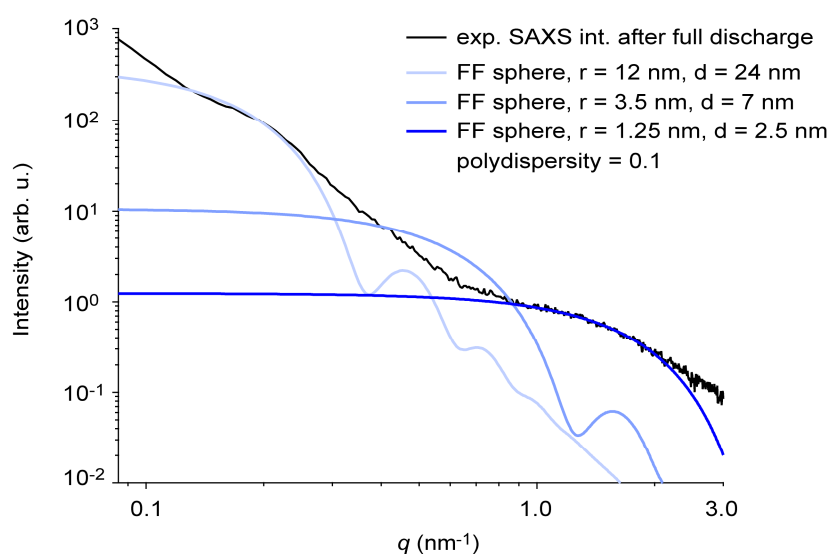
## Supplementary Figures



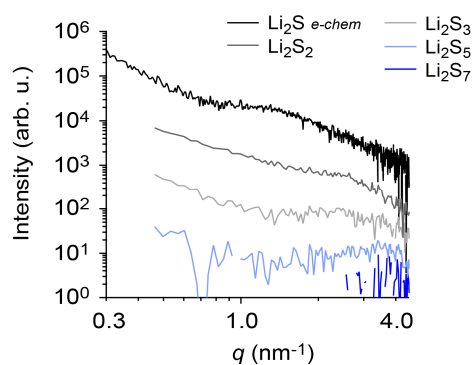
**Supplementary Figure 1:** In situ SAXS / WAXS during galvanostatic discharge / charge of a ENSACO350G/S composite cathode and a 1 M LiTFSI TEGDME:DOL (1:1) electrolyte at C/3 (**a-c**), C/10 (**d-f**) and C/30 (**g-i**). The SAXS/WAXS data were recorded on a laboratory SAXS facility (SAXSpot 2.0, Anton Paar), resulting in a significantly higher signal-to-noise ratio as compared to the Synchrotron data. **a**, Potential vs. Li/Li<sup>+</sup> as a function of time during galvanostatic discharge at C/3. **b**, The corresponding relative SAXS intensity change as a function of time and scattering vector length  $q$ . **c**, WAXS intensity as a function of time and scattering angle Two Theta. **d-e** and **h-i** show the same data for a full galvanostatic discharge / charge cycle at C/10 (**d-e**) and galvanostatic discharge at C/30 (**h-i**). The SAXS/WAXS data verify the important features observed in Fig. 2 in an alternative Li-S systems. The high- $q$  ( $q_B$ ) SAXS intensity maximum at the end of discharge is present at all rates; the low- $q$  ( $q_A$ ) SAXS intensity maximum is more pronounced at higher C-rates. The Scherrer crystallite sizes at C/3, C/10 and C/30 correspond to 6.5 nm, 6.7 nm and 6.0 nm obtained from a Lorentzian peak fit and the Scherrer equation. This is practically identical to the values shown in Fig. 2. The sharp peaks in **c**, **f**, **i** correspond to the diffraction peaks of the relatively large sulfur crystallites.



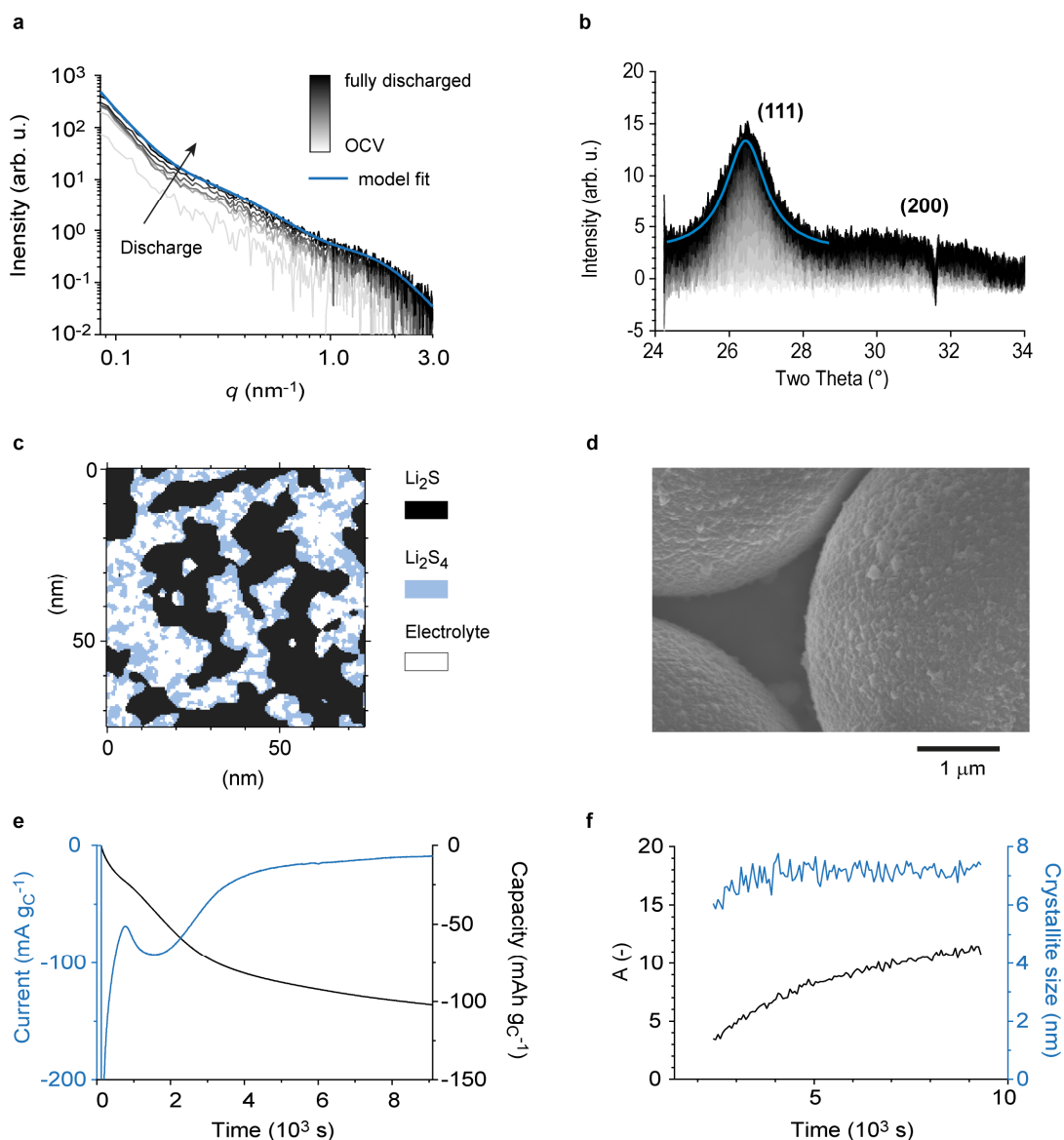
**Supplementary Figure 2:** SAXS/WAXS intensities versus scattering vector length  $q$  (a) and scattering angle (b) for the discharged cathode in the *in situ* cell. The black solid line shows the equivalent to the reduced SAXS intensity after discharge in Fig. 5a, the discharged cathode after washing with glyme and subsequent drying under vacuum (dark grey solid line) and the discharged cathode without washing, but with drying under vacuum (grey solid line). The blue solid line shows the SAXS/WAXS intensities of separator and Li metal after discharger. The absence of any SAXS feature and the Li<sub>2</sub>S diffraction peaks gives evidence that the recorded structural changes take place in the cathode only.



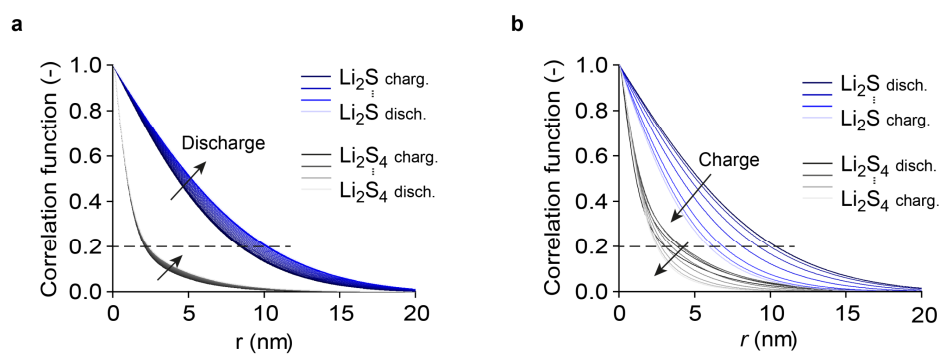
**Supplementary Figure 3:** Reduced, experimental SAXS intensity versus scattering vector length  $q$  for the fully discharged KB cathode in the diglyme catholyte after subtracting the SAXS intensity prior to discharge at OCV and hence the carbon black scattering contribution (black solid line, details see methods, all SAXS intensities during discharge are shown in Fig. 5a). The blue curves correspond to the analytical SAXS formfactor of spheres with 10 % polydispersity and a mean diameter of 24 nm, 7 nm and 2.5 nm and give an estimate about the size of possible real-space structures. The primary  $\text{Li}_2\text{S}$  crystallites with a size of 7 nm (as obtained from the  $\text{Li}_2\text{S}$  WAXS diffraction peak width) are not present as individual, solid particles since the corresponding intensity shoulder is missing in the SAXS regime. The high- $q$  ( $1.5 \text{ nm}^{-1}$ ) and low- $q$  ( $0.2 \text{ nm}^{-1}$ ) intensity shoulders correspond to solid particles / aggregates with a size around 2.5 nm and 24 nm, respectively.



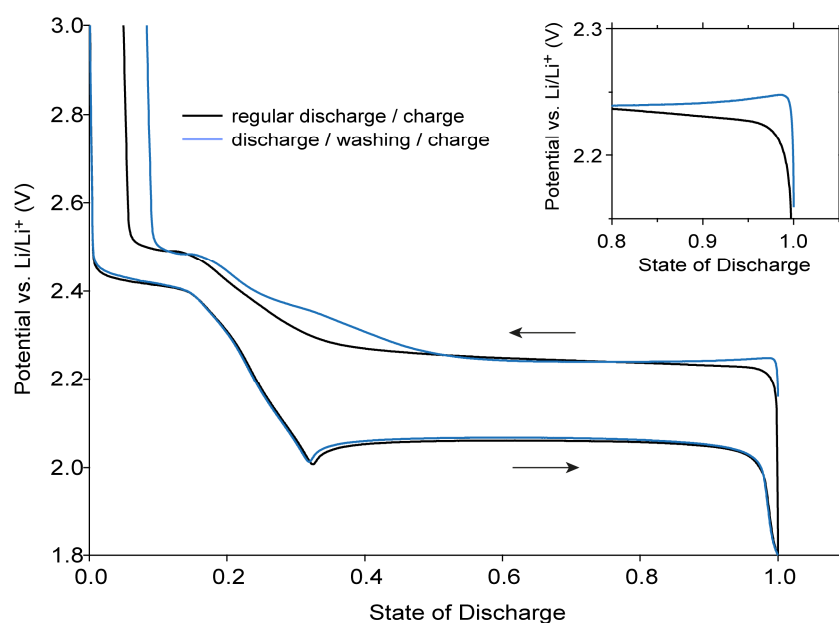
**Supplementary Figure 4:** SAXS intensity versus scattering vector length  $q$  of nominal  $\text{Li}_2\text{S}_2$ ,  $\text{Li}_2\text{S}_3$ ,  $\text{Li}_2\text{S}_5$ ,  $\text{Li}_2\text{S}_7$  polysulfide powders. The black solid line shows the SAXS intensity of the reduced in situ SAXS intensity at the end of discharge (equivalent to Fig. 5a). The corresponding XRD data is given in Fig. 4b.  $\text{Li}_2\text{S}_2$  and  $\text{Li}_2\text{S}_3$  show an intensity shoulder at high  $q$ , similar like the electrochemically formed  $\text{Li}_2\text{S}/\text{Li}_2\text{S}_4$  deposits shown in Fig. 5. The presence of the intensity shoulder at higher  $q$ -values may point at smaller  $\text{Li}_2\text{S}_4$  particles also present in the polysulfide powders.



**Supplementary Figure 5:** In situ SAXS / WAXS and plurigaussian random field model for potentiostatic discharge with a Glassy Carbon bead cathode and the 0.5 M Li<sub>2</sub>S<sub>8</sub> / 2G catholyte as used in Fig. 1, 2, 3, 5. **a**, reduced SAXS intensities versus scattering vector length  $q$  during potentiostatic discharge at 2.0 V vs. Li/Li<sup>+</sup> to a capacity of 102 mAh g<sub>C</sub><sup>-1</sup>. The SAXS intensity prior to discharge (at OCV) was subtracted from averaged SAXS intensities. The plurigaussian random field (PGRF) model fit is given in blue. Fit parameters are given in Table S1. **b**, Background corrected WAXS intensities versus scattering angle during potentiostatic discharge at 2.0 V vs. Li/Li<sup>+</sup> to a capacity of 250 mAh g<sub>C</sub><sup>-1</sup>. The (111) Li<sub>2</sub>S diffraction peak is fitted using a Lorentz function. **c**, Cross section of the representative real space model generated via PGRFs and the input parameters obtained from the model fit in **a**. **d**, Scanning electron microscopy image showing the Li<sub>2</sub>S deposits on top of the large Glassy carbon beads (> 1 μm) after potentiostatic discharge. **e**, Specific current (blue) and specific capacity (black) versus time during potentiostatic discharge of the in situ SAXS cell. Both current and capacity are normalized by the bare glassy carbon electrode mass. **f**, (111) diffraction peak height  $A$  (obtained from Lorentzian peak fit) and crystallite size (obtained from the (111) peak width and the Scherrer equation) as a function of time during potentiostatic discharge. The good fit quality in **a** indicates that the deviation in Fig. 5a stem from neglected Li<sub>2</sub>S / Li<sub>2</sub>S<sub>4</sub> – carbon black correlations. As the glassy carbon beads are much larger than the Li<sub>2</sub>S / Li<sub>2</sub>S<sub>4</sub> deposits any cross correlations are negligible in the SAXS intensities.

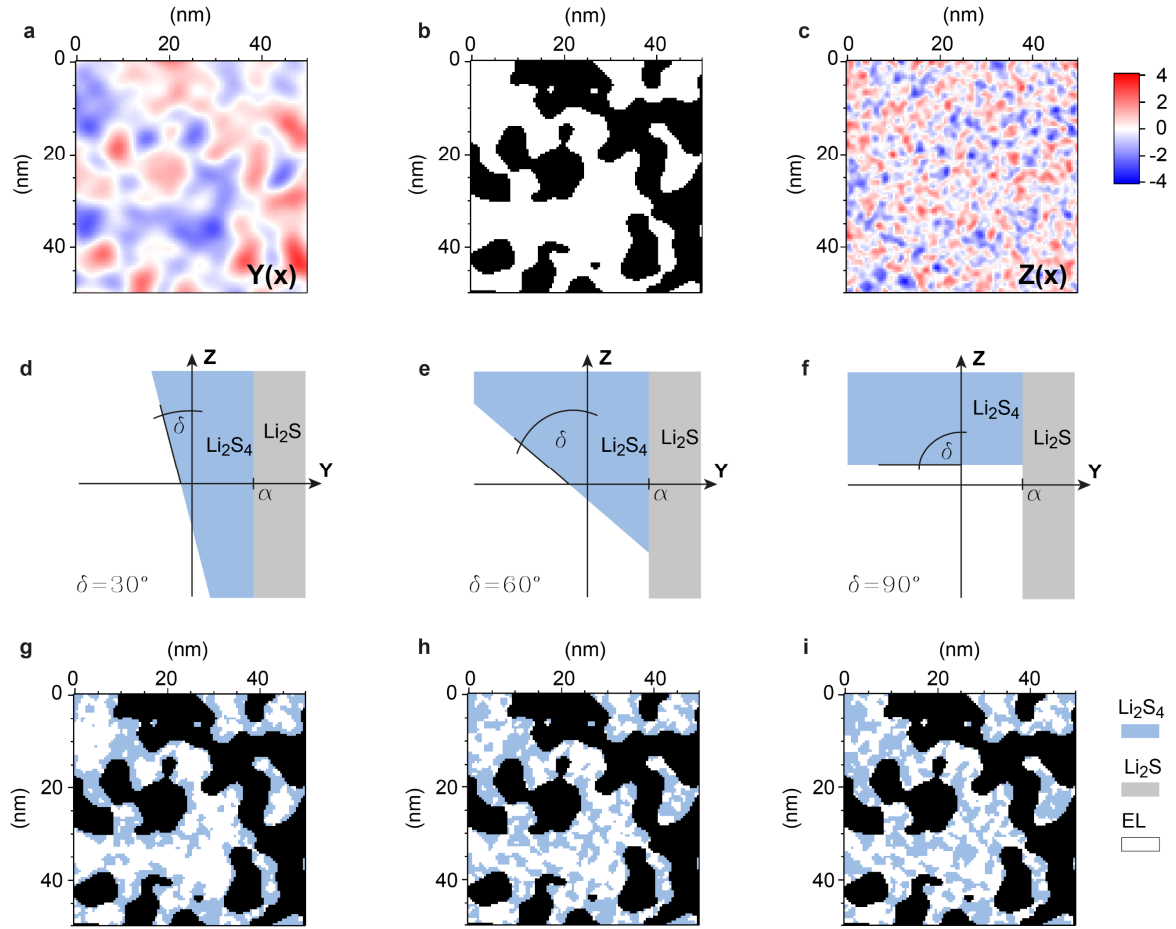


**Supplementary Figure 6: a-b**,  $\text{Li}_2\text{S} - \text{Li}_2\text{S}$  (blue to light grey) and  $\text{Li}_2\text{S}_4 - \text{Li}_2\text{S}_4$  (black to light grey) correlation functions versus distance  $r$  of the Plurigaussian random field model in Fig. 5e-h, during discharge (**a**) and charge (**b**). The normalized correlation functions are calculated from the two-point probability functions as described in the methods section. The  $\text{Li}_2\text{S}$  and  $\text{Li}_2\text{S}_4$  correlation length (shown in Fig. 5g, h) is (arbitrarily) defined as the distance  $r$ , where the correlation function reaches the value of 0.2.



**Supplementary Figure 7:** Galvanostatic discharge / charge of a sulfur melt-infiltrated KB cathode (S:C mass ratio of 2:1) in 1 M LiTFSI + 0.4 M LiNO<sub>3</sub> / 2G at C/10 with a maximum discharge capacity of 1117 mAh g<sub>S</sub><sup>-1</sup> (black curve) and 1231 mAh g<sub>S</sub><sup>-1</sup> (blue curve). The black solid line shows a regular discharge / charge cycle. The blue solid line shows an identical galvanostatic discharge / charge cycle with an additional washing step of the discharged cathode between discharge and charge. The washing step includes rinsing the discharged cathode with 2G solvent, drying the washed and discharged cathode under vacuum, and reassembling the cell using the washed cathode, a new separator and a fresh 1 M LiTFSI + 0.4 M LiNO<sub>3</sub> / 2G electrolyte. The overpotential at the onset of charge shows that washing removes parts of the dissolved Li<sub>2</sub>S<sub>2</sub> polysulfides and solid Li<sub>2</sub>S<sub>4</sub> particles. Without the dissolved PSs serving as mediators initial charging requires the direct oxidation of Li<sub>2</sub>S and hence electron transport across the poorly conducting Li<sub>2</sub>S. In line with the first charging cycle of Li-S batteries using Li<sub>2</sub>S / C composite cathodes<sup>1</sup>, charging overpotentials in the beginning are high. The charging overpotential drops to values of the regularly cycled cell (black solid line) after a significant amount of dissolved PSs have been formed.





**Supplementary Figure 8:** Plurigaussian random field (PGRF), real space structure generation with the parameters shown in Table S1, second column. Only the parameter  $\delta$  is varied. **a**, Cross-section of 3D Gaussian random field  $Y(x)$ . **b**, Cross section of 3D  $\text{Li}_2\text{S}$  structure generated from  $Y(x)$  using the threshold value  $\alpha$ . **c**, Cross-section of 3D Gaussian random field  $Z(x)$ . **d-e**, Z-Y planes visualizing the threshold value dependencies of the two GRFs  $Y(x)$  and  $Z(x)$ . The threshold value  $\alpha$  to generate the  $\text{Li}_2\text{S}$  structure is indicated on the horizontal axis. The borderline between blue and white area determines whether the  $\text{Li}_2\text{S}_4$  phase shows a strong correlation (**d**,  $\delta \rightarrow 0^\circ$ ) or no correlation (**f**,  $\delta \rightarrow 90^\circ$ ) to the  $\text{Li}_2\text{S}$  phase. The corresponding morphologies for  $\delta = 30^\circ$ ,  $\delta = 60^\circ$ , and  $\delta = 90^\circ$  are shown in **g**, **h** and **i**, respectively.

## Supplementary Tables

**Table S1 | PGRF model fit results.**  $\rho_{e-}$  is given in units of  $\text{cm}^{-2}$  and corresponds to the electron density times the classical electron radius ( $2.82 \times 10^{-13}$  cm).

|                                     | Carbon black electrode<br>(Model fit Fig. 5a) | Glass Carbon electrode<br>(Model fit Supplementary Fig. 5a) |
|-------------------------------------|---|---|
| $K$                                 | 10  | 5.5   |
| $V / V_{max}$                       | 1   | 1   |
| $\rho_{e-, EL} (\text{cm}^{-2})$    | $1.10 \times 10^{11}$                         | $1.10 \times 10^{11}$                                       |
| $\rho_{e-, Li2S} (\text{cm}^{-2})$  | $1.34 \times 10^{11}$                         | $1.34 \times 10^{11}$                                       |
| $\rho_{e-, Li2S4} (\text{cm}^{-2})$ | $1.52 \times 10^{11}$                         | $1.52 \times 10^{11}$                                       |
| $l_Y (\text{nm})$                   | 0.9   | 1.1   |
| $d_Y (\text{nm})$                   | 6.0   | 4.6   |
| $l_Z (\text{nm})$                   | 7.0   | 3.2   |
| $d_Z (\text{nm})$                   | 48  | 32  |
| $\phi_{Li2S}$                       | 0.4   | 0.48  |
| $\phi_{Li2S4}$                      | 0.2   | 0.24  |
| $\delta (^\circ)$                   | 45  | 45  |
| $A$                                 | 0.03  | 0.007   |
| $\gamma$                            | -4  | -4.5  |

**Table S2 | Electron (scattering length) densities of the various components.**  $\rho_{e-}$  is given in units of  $\text{cm}^{-2}$  and corresponds to the electron density times the classical electron radius ( $2.82 \times 10^{-13}$  cm). The  $\text{Li}_2\text{S}_4$  mass density,  $1.82 \text{ cm}^3 \text{ g}^{-1}$ , was taken from DFT simulations, calculating crystal structures of solid PSs<sup>2</sup>. For the catholyte, we assumed a  $\text{Li}_2\text{S}_8$  concentration of 2 M inside the carbon black pores, i.e., higher than in the bulk liquid (0.5 M). The electron (scattering length) density of the as-prepared catholyte with 0.5 M  $\text{Li}_2\text{S}_8$  corresponds to  $0.98 \times 10^{11} \text{ cm}^{-2}$ . The carbon black skeleton density is lower than the graphite density due to the significant micropore content<sup>3,4</sup>.

|                         | Mass density<br>( $\text{g cm}^{-3}$ ) | Molar mass<br>( $\text{g mol}^{-1}$ ) | Molar volume<br>( $\text{cm}^3 \text{ mol}^{-1}$ ) | $\rho_{e-} (\text{cm}^{-2})$ |
|-------------------------|--|---------------------------------------|--|------------------------------|
| $\text{Li}_2\text{S}$   | 1.66                                   | 45.95                                 | 27.68  | $1.34 \times 10^{11}$        |
| $\text{Li}_2\text{S}_4$ | 1.82                                   | 142                                   | 73.57  | $1.52 \times 10^{11}$        |
| S                       | 2.00                                   | 32                                    | 16   | $1.69 \times 10^{11}$        |
| Catholyte               | -                                      | -                                     | -  | $0.98 \times 10^{11}$        |
| Carbon                  | 2.05                                   | 12                                    | 5.85   | $1.74 \times 10^{11}$        |

## Supplementary Notes

### Supplementary Note 1 | Discussion of alternative SAXS data interpretation

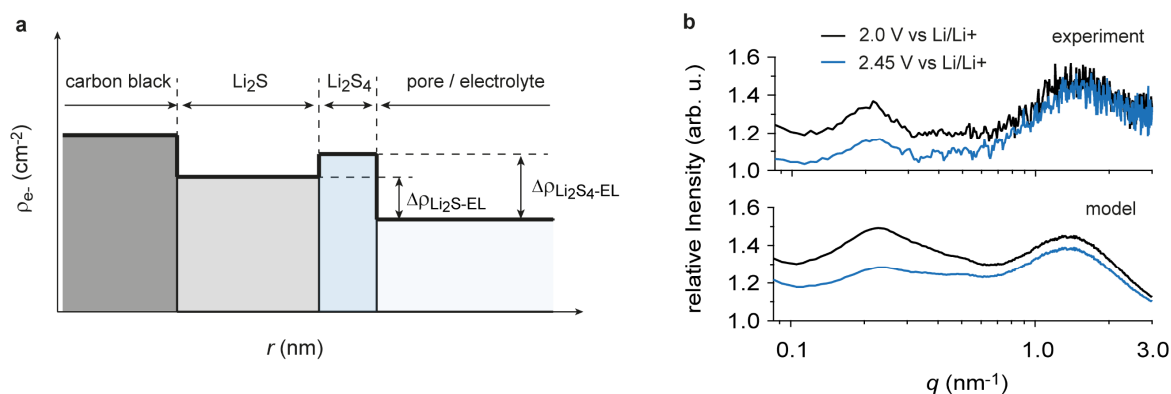
The SAXS model presented in Fig. 5 is consistent with all electrochemical (Fig. 1b), *in situ* SAXS (Fig. 2), *in situ* WAXS (Fig. 2), SEM (Fig. 3) and *ex situ* SAXS/WAXS data (Fig. 4b, Supplementary Figs. 2, 4). Focusing on the SAXS/WAXS data, we argue in the following why alternative interpretations remain possible, yet unlikely.

#### Why is the high- $q$ intensity shoulder (Fig. 5a) likely caused by $\text{Li}_2\text{S}_4$ (or similar higher-order PS)?

An alternative interpretation of the high- $q$  intensity shoulder in Fig. 5a could be a second fraction of smaller  $\text{Li}_2\text{S}$  particles generated by a mechanism other than disproportionation. While a large fraction of  $\text{Li}_2\text{S}$  would still be formed via solution-mediated disproportionation (as confirmed by the *in situ* WAXS data), a certain amount of  $\text{Li}_2\text{S}$  could be formed via direct electroreduction at the carbon-electrolyte interface. However, this is unlikely, as a conformal or somewhat patchy coating of  $\text{Li}_2\text{S}$  on the carbon black surface would decrease the high- $q$  SAXS intensity<sup>5</sup>.

As shown in Supplementary Fig. 9b, the structure causing the high- $q$  intensity shoulder requires a higher electron density than its surrounding. Otherwise the significant intensity hump could not be reproduced.

A change in the electrolyte's electron density causes a larger scattering intensity change at low  $q$  (Supplementary Fig. 9a). This reflects the high sensitivity of the  $\text{Li}_2\text{S}$  aggregate structures against electrolyte electron density changes, due to the low  $\text{Li}_2\text{S}$  electron density (Supplementary Fig. 9a). This is best seen in the experimental SAXS intensity change directly after charging has started (Supplementary Fig. 9b). The quick increase in anion concentration causes a quick increase in the electrolyte electron density and hence a quick SAXS intensity drop (due to the reduced  $\text{Li}_2\text{S}$ –electrolyte electron density contrast  $\Delta\rho_{\text{Li}_2\text{S-EL}}$ ), specifically at low  $q$ . If the same material would cause both the low- $q$  and high- $q$  intensity shoulders, the intensity drop would be the same for all  $q$ .



**Supplementary Figure 9:** **a**, Sketch of electron density levels  $\rho_e$  of the different phases.  $\rho_e$  is given in units of cm<sup>-2</sup> and corresponds to the electron density times the classical electron radius ( $2.82 \times 10^{-13}$  cm). The electron density contrast with respect to the surrounding phase determines the phase's "scattering power". **b**, relative SAXS intensities as a function of scattering vector length  $q$  at the end of discharge at 2.0 V vs. Li/Li<sup>+</sup> (black) and right after charge has started at 2.45 V vs. Li/Li<sup>+</sup> (blue) for the experimental data (top) and the PluriGRF SAXS model (bottom). To obtain the relative SAXS intensities, the SAXS intensities were normalized by the SAXS intensity prior to discharge at OCV. The difference in the relative SAXS intensities in **b** is primarily caused by the quick change in the electrolyte electron density. The relative SAXS intensity change for both model and experimental data is larger at small  $q$  and smaller at high  $q$  – indicating that the high- $q$  SAXS intensity must stem from  $\text{Li}_2\text{S}_4$  (or other higher-order PS) particles with an electron density larger than the  $\text{Li}_2\text{S}$  electron density. If all generated solid structures were  $\text{Li}_2\text{S}$  with constant electron density, the SAXS intensity changes in **b** should be equal for all  $q$ .

The required high electron density suggests that higher-order PS solids, such as  $\text{Li}_2\text{S}_4$  are responsible for the high- $q$  intensity shoulder. As shown by DFT calculations<sup>2</sup>, higher-order PS solids have a higher mass density and consequently a higher electron density than crystalline  $\text{Li}_2\text{S}$  (Table S2). Amorphous  $\text{Li}_2\text{S}$  has a lower density than crystalline  $\text{Li}_2\text{S}$  and can be ruled out to be responsible for the high  $q$  intensity shoulder.

A similar high- $q$  intensity shoulder is present in the  $\text{Li}_2\text{S}_2$  and  $\text{Li}_2\text{S}_3$  PS solids formed via chemical routes (i.e. disproportionation). This further suggests solid  $\text{Li}_2\text{S}_4$  to be the intensity hump's origin.

Unfortunately, the WAXS data cannot prove the existence of solid  $\text{Li}_2\text{S}_4$  (or alternative solid PS) particles. Diffraction peaks of crystalline, solid  $\text{Li}_2\text{S}_4$  are hard to identify, as the particles are small ( $< 3$  nm) and the diffraction peaks broad. The broad peaks may be at similar positions as the  $\text{Li}_2\text{S}$  diffraction peaks and difficult to distinguish from the significant background. Further, any solid  $\text{Li}_2\text{S}_4$  particles may be amorphous.

#### **Why are the primary $\text{Li}_2\text{S}$ crystallites with 7 nm in diameter hardly visible with SAXS?**

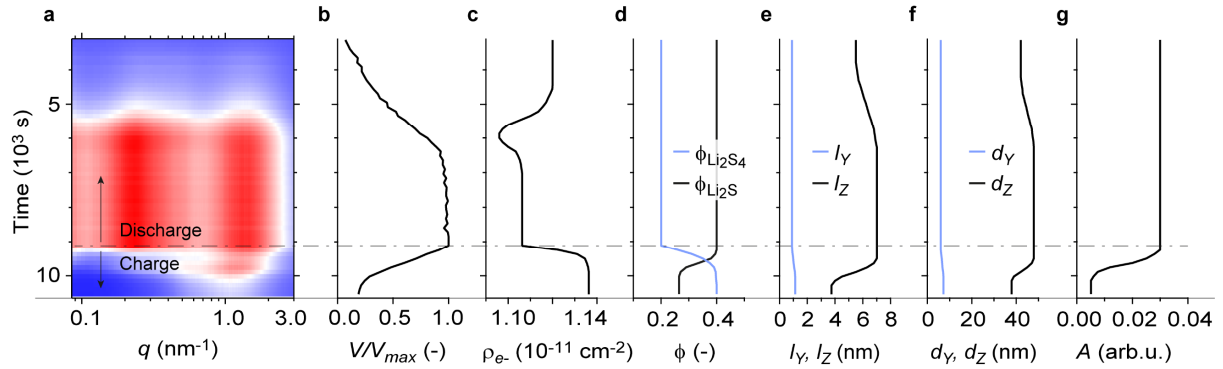
Besides the relatively low electron density contrast between  $\text{Li}_2\text{S}$  and electrolyte, the  $\text{Li}_2\text{S}$  structure likely forms larger aggregate fractal-like structures. Fractal-like structures cause typically a featureless power-law intensity decay, where the primary particle size is not necessarily visible as a distinct intensity hump / peak.

#### **What about carbon – $\text{Li}_2\text{S}$ / $\text{Li}_2\text{S}_4$ cross correlations?**

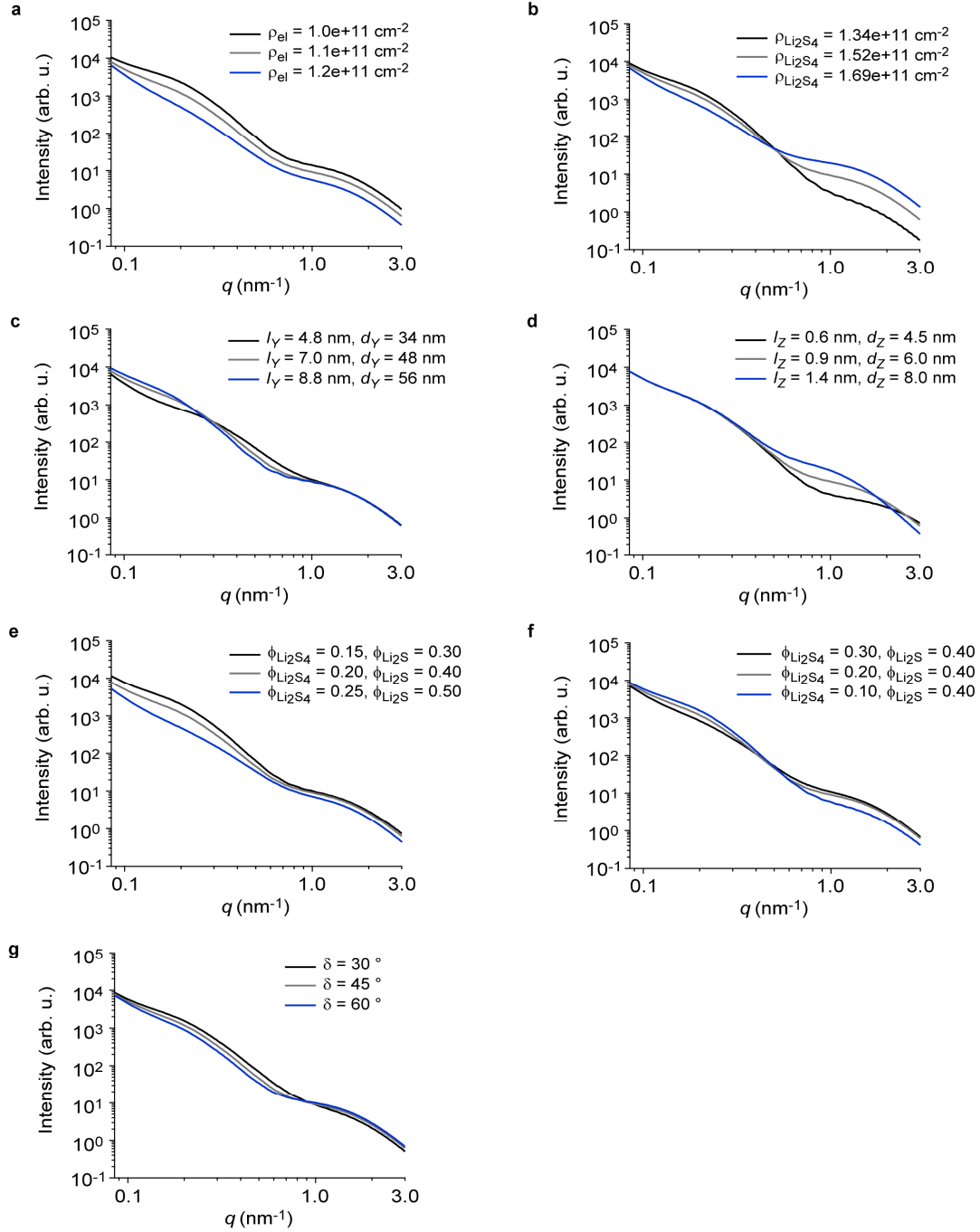
Carbon black –  $\text{Li}_2\text{S}$  /  $\text{Li}_2\text{S}_4$  cross correlations are most likely responsible for the significant deviation between model fit and experimental data in Fig. 5a. An improved model fit for a glassy carbon electrode with negligible cross correlation in Supplementary Fig. 5a indicates this (the glassy carbon beads are much larger than the  $\text{Li}_2\text{S}$  /  $\text{Li}_2\text{S}_4$  deposits).

## Supplementary Note 2 | The PGRF model input parameters

Given the possible systematic errors in the SAXS data interpretation, it is feasible to reproduce the experimental SAXS intensities during discharge and charge by varying the PGRF SAXS model input parameters within physically reasonable constraints according to the state of charge. The model fit in Fig. 5a for the  $\text{Li}_2\text{S} / \text{Li}_2\text{S}_4$  structure provides the model input parameters after full discharge and serves as a starting point for the input parameter variation shown in Supplementary Fig. 10.



**Supplementary Figure 10:** Plurigaussian random field model input parameters. **a**, Modelled relative SAXS intensity change during potentiostatic discharge/charge (equivalent data in Fig. 5e). **b**, Relative volume change of the  $\text{Li}_2\text{S} / \text{Li}_2\text{S}_4$  nanostructure as a function of time. The amount is proportional to the  $\text{Li}_2\text{S}$  (111) diffraction peak intensity quantified by the Lorentzian model fit in Fig. 2b. **c**, Mean electrolyte electron (scattering length) density as a function of time (given in units of  $\text{cm}^{-2}$ ,  $\rho_e$  corresponds to the electron density times the classical electron radius,  $2.82 \times 10^{-13} \text{ cm}$ ). A subtle  $q$ -independent intensity maximum at 5000 – 6000 s (see Fig. 2c-d, Fig. 5d) indicates a minimum in the electrolyte electron density, due to a depletion of dissolved polysulfides at maximum current or maximum  $\text{Li}_2\text{S}$  formation rate. During charge at 2.4 V vs.  $\text{Li}/\text{Li}^+$ , the electrolyte electron density increases due to the higher concentration of heavy  $\text{TFSI}^-$  anions<sup>6</sup> compensating the more positive electrode potential. Assumed scattering length densities of catholyte,  $\text{Li}_2\text{S}$ ,  $\text{Li}_2\text{S}_4$ , and carbon are given in Table S2. **d**,  $\text{Li}_2\text{S}_4$  and  $\text{Li}_2\text{S}$  volume fractions as a function of time. Apart from charge, the  $\text{Li}_2\text{S}$  volume fraction is assumed to be twice the  $\text{Li}_2\text{S}_4$  volume fractions. **e**, Correlation parameters  $l_Y$  and  $l_Z$  of the two Gaussian random fields  $Y(\mathbf{x})$  and  $Z(\mathbf{x})$ . The slight increase of  $l_Y$  during charge indicates the slight growth of  $\text{Li}_2\text{S}_4$  particles at initial stages of charge. The increase of  $l_Z$  during discharge indicates the growth of the larger  $\text{Li}_2\text{S}$  aggregates; the decrease of  $l_Y$  the dissolution of  $\text{Li}_2\text{S}$  aggregates. **f**, Correlation parameters  $d_Y$  and  $d_Z$  of the two Gaussian random fields  $Y(\mathbf{x})$  and  $Z(\mathbf{x})$ . **g**, Factor  $A$  (see Equation 2) as a function of time. The drop during charge accounts for the dissolution of larger  $\text{Li}_2\text{S}$  aggregates. All other input parameters are kept constant (Table S1).



**Supplementary Figure 11:** Impact of parameter variation on the PGRF model SAXS intensities. The basic parameter configuration corresponds to the values given in Table S2, first column and the model fit shown in Fig. 5a. **a**, SAXS intensity versus scattering vector length  $q$  for different electrolyte electron (scattering length) densities, while leaving all other parameters constant. **b**, SAXS intensity versus scattering vector length  $q$  for different  $\text{Li}_2\text{S}_4$  electron (scattering length) densities, while leaving all other parameters constant. This shows that the high- $q$  intensity shoulder (Fig. 2, Fig. 5) must stem from particles with an electron density higher than the  $\text{Li}_2\text{S}$  electron density of  $1.34 \times 10^{11} \text{ cm}^{-2}$ . This points at solid, higher order polysulfides (such as  $\text{Li}_2\text{S}_4$ ) with higher mass density compared to solid  $\text{Li}_2\text{S}$ . **c**, SAXS intensity versus scattering vector length  $q$  for different correlation parameters of the Gaussian random field  $Y(\mathbf{x})$ , while leaving all other parameters constant. Changes concern mainly the low- $q$  intensity shoulder of  $\text{Li}_2\text{S}$  aggregates. **d**, SAXS intensity versus scattering vector length  $q$  for different correlation parameters of the Gaussian random field  $Z(\mathbf{x})$ , while leaving all other parameters constant. Changes concern mainly the high- $q$  intensity shoulder of  $\text{Li}_2\text{S}_4$  particles. **e-f**, SAXS intensity versus scattering vector length  $q$  for different  $\text{Li}_2\text{S}$  and  $\text{Li}_2\text{S}_4$  volume fractions, while leaving all other parameters constant. **g**, SAXS intensity versus scattering vector length  $q$  for different parameters  $\beta$ , while leaving all other parameters constant.  $\delta$  determines whether the  $\text{Li}_2\text{S}_4$  particles grow preferably on top of the  $\text{Li}_2\text{S}$  surface (low  $\delta$ ) or without any cross correlation to the  $\text{Li}_2\text{S}$  structure, i.e. towards the center of the  $\text{Li}_2\text{S}$  cavities (high  $\delta$ ).

## Supplementary References

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