

## Appendix A

**Article Title:** Enhancing streamflow projections under climate change using optimized machine learning: A comparative study in the Babolrood River Basin, Iran

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To enhance the clarity and readability of the main manuscript, detailed performance data for the machine learning models used in this study are provided in Supplementary Table S1. The table presents the results for seven different input data models during the training and testing phases, covering both their standalone performance and their performance when optimized by the PSO and FDA algorithms.

Table S1: Comparison of machine learning model performance in independent and optimized states during training and testing phases.

| Model          | Train |       |       |      |      | Test  |       |      |      |      |
|----------------|-------|-------|-------|------|------|-------|-------|------|------|------|
| M <sub>1</sub> | RMSE  | MAE   | NSE   | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -     | -    | -    | 18.45 | 9.76  | 0.55 | 0.65 | 0.75 |
| KNN-FDA        | -     | -     | -     | -    | -    | 17.25 | 7.88  | 0.64 | 0.68 | 0.82 |
| KNN-PSO        | -     | -     | -     | -    | -    | 17.07 | 7.88  | 0.63 | 0.65 | 0.84 |
| SVR            | 14.36 | 6.32  | 0.76  | 0.76 | 0.87 | 30.02 | 18.03 | 0.00 | 0.37 | 0.06 |
| SVR-FDA        | 11.73 | 5.24  | 0.84  | 0.87 | 0.92 | 15.13 | 7.94  | 0.63 | 0.60 | 0.80 |
| SVR-PSO        | 13.94 | 6.15  | 0.77  | 0.78 | 0.88 | 16.84 | 7.66  | 0.70 | 0.70 | 0.84 |
| LSTM           | 22.49 | 13.85 | 0.43  | 0.41 | 0.63 | 23.27 | 15.46 | 0.49 | 0.60 | 0.70 |
| LSTM-FDA       | 13.99 | 7.76  | 0.79  | 0.73 | 0.89 | 14.42 | 8.03  | 0.75 | 0.63 | 0.83 |
| LSTM-PSO       | 14.60 | 7.73  | 0.76  | 0.77 | 0.88 | 13.62 | 7.59  | 0.70 | 0.75 | 0.84 |
| RF             | 25.95 | 15.11 | 0.24  | 0.16 | 0.56 | 21.70 | 13.83 | 0.24 | 0.17 | 0.55 |
| RF-FDA         | 8.87  | 4.16  | 0.91  | 0.86 | 0.96 | 13.38 | 7.13  | 0.79 | 0.82 | 0.86 |
| RF-PSO         | 9.68  | 4.34  | 0.89  | 0.84 | 0.95 | 15.01 | 7.54  | 0.68 | 0.75 | 0.82 |
| XGBoost        | 0.71  | 20.48 | 11.10 | 0.50 | 0.71 | 21.77 | 11.42 | 0.54 | 0.63 | 0.73 |
| XGBoost-FDA    | 2.58  | 1.76  | 0.99  | 0.98 | 0.99 | 16.97 | 8.30  | 0.73 | 0.73 | 0.86 |
| XGBoost-PSO    | 4.30  | 2.91  | 0.98  | 0.96 | 0.99 | 18.75 | 8.92  | 0.68 | 0.72 | 0.82 |

Continued Table S1: Comparison of machine learning model performance in independent and optimized states during training and testing phases.

| Model          | Train |       |      |      |      | Test  |       |      |      |      |
|----------------|-------|-------|------|------|------|-------|-------|------|------|------|
| M <sub>2</sub> | RMSE  | MAE   | NSE  | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -    | -    | -    | 24.26 | 9.76  | 0.55 | 0.65 | 0.75 |
| KNN-FDA        | -     | -     | -    | -    | -    | 19.56 | 9.82  | 0.45 | 0.66 | 0.76 |
| KNN-PSO        | -     | -     | -    | -    | -    | 18.17 | 9.51  | 0.53 | 0.56 | 0.73 |
| SVR            | 14.54 | 6.03  | 0.76 | 0.02 | 0.87 | 28.82 | 17.69 | 0.02 | 0.24 | 0.15 |
| SVR-FDA        | 16.94 | 7.72  | 0.66 | 0.68 | 0.82 | 19.22 | 9.12  | 0.65 | 0.58 | 0.81 |
| SVR-PSO        | 18.13 | 8.18  | 0.61 | 0.61 | 0.80 | 20.65 | 9.40  | 0.54 | 0.52 | 0.76 |
| LSTM           | 24.88 | 13.03 | 0.41 | 0.21 | 0.64 | 29.50 | 14.27 | 0.38 | 0.40 | 0.62 |
| LSTM-FDA       | 19.86 | 11.19 | 0.64 | 0.47 | 0.80 | 18.70 | 11.42 | 0.48 | 0.33 | 0.69 |
| LSTM-PSO       | 13.67 | 8.26  | 0.77 | 0.79 | 0.73 | 23.28 | 11.22 | 0.53 | 0.67 | 0.73 |
| RF             | 26.76 | 15.36 | 0.19 | 0.10 | 0.59 | 23.31 | 14.67 | 0.12 | 0.01 | 0.41 |
| RF-FDA         | 11.60 | 5.54  | 0.85 | 0.82 | 0.93 | 17.68 | 9.75  | 0.50 | 0.56 | 0.72 |
| RF-PSO         | 11.80 | 5.76  | 0.84 | 0.80 | 0.92 | 19.35 | 10.01 | 0.56 | 0.71 | 0.76 |
| XGBoost        | 20.44 | 11.25 | 0.50 | 0.61 | 0.71 | 23.79 | 11.99 | 0.42 | 0.51 | 0.65 |
| XGBoost-FDA    | 11.32 | 6.52  | 0.83 | 0.83 | 0.91 | 16.97 | 8.30  | 0.73 | 0.73 | 0.86 |
| XGBoost-PSO    | 10.59 | 6.31  | 0.87 | 0.87 | 0.94 | 19.45 | 10.27 | 0.49 | 0.63 | 0.70 |
| M <sub>3</sub> | RMSE  | MAE   | NSE  | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -    | -    | -    | 23.21 | 11.50 | 0.32 | 0.58 | 0.61 |
| KNN-FDA        | -     | -     | -    | -    | -    | 19.87 | 9.34  | 0.55 | 0.65 | 0.74 |
| KNN-PSO        | -     | -     | -    | -    | -    | 21.07 | 9.51  | 0.53 | 0.56 | 0.73 |
| SVR            | 15.64 | 6.25  | 0.74 | 0.74 | 0.87 | 23.98 | 16.48 | 0.02 | 0.20 | 0.20 |
| SVR-FDA        | 17.97 | 7.70  | 0.64 | 0.68 | 0.80 | 17.32 | 8.56  | 0.52 | 0.51 | 0.72 |
| SVR-PSO        | 19.34 | 8.34  | 0.57 | 0.57 | 0.77 | 18.36 | 8.83  | 0.60 | 0.62 | 0.79 |
| LSTM           | 24.50 | 19.09 | 0.50 | 0.35 | 0.71 | 25.65 | 19.37 | 0.41 | 0.53 | 0.64 |
| LSTM-FDA       | 20.04 | 10.18 | 0.55 | 0.55 | 0.74 | 16.87 | 9.76  | 0.54 | 0.50 | 0.74 |
| LSTM-PSO       | 17.57 | 9.25  | 0.62 | 0.66 | 0.79 | 21.35 | 10.64 | 0.58 | 0.50 | 0.80 |
| RF             | 24.72 | 14.45 | 0.29 | 0.21 | 0.65 | 24.58 | 14.19 | 0.28 | 0.20 | 0.62 |
| RF-FDA         | 12.40 | 5.82  | 0.83 | 0.78 | 0.92 | 16.00 | 8.77  | 0.52 | 0.58 | 0.74 |
| RF-PSO         | 12.13 | 6.37  | 0.84 | 0.76 | 0.93 | 14.10 | 8.44  | 0.61 | 0.65 | 0.79 |
| XGBoost        | 21.59 | 11.48 | 0.48 | 0.65 | 0.70 | 22.34 | 11.41 | 0.21 | 0.50 | 0.54 |
| XGBoost-FDA    | 10.90 | 6.00  | 0.86 | 0.85 | 0.93 | 20.62 | 10.36 | 0.45 | 0.62 | 0.68 |
| XGBoost-PSO    | 10.18 | 5.77  | 0.88 | 0.87 | 0.94 | 20.43 | 10.58 | 0.49 | 0.58 | 0.70 |
| M <sub>4</sub> | RMSE  | MAE   | NSE  | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -    | -    | -    | 24.21 | 11.38 | 0.52 | 0.57 | 0.73 |
| KNN-FDA        | -     | -     | -    | -    | -    | 22.77 | 10.52 | 0.50 | 0.61 | 0.74 |
| KNN-PSO        | -     | -     | -    | -    | -    | 19.78 | 9.32  | 0.52 | 0.56 | 0.74 |
| SVR            | 14.32 | 6.19  | 0.78 | 0.77 | 0.89 | 25.04 | 16.48 | 0.01 | 0.34 | 0.10 |
| SVR-FDA        | 11.47 | 5.14  | 0.84 | 0.86 | 0.92 | 22.49 | 9.42  | 0.60 | 0.52 | 0.82 |
| SVR-PSO        | 15.20 | 6.63  | 0.73 | 0.72 | 0.86 | 17.83 | 8.28  | 0.61 | 0.66 | 0.78 |
| LSTM           | 29.62 | 16.60 | 0.02 | 0.01 | 0.58 | 29.63 | 15.86 | 0.03 | 0.35 | 0.60 |
| LSTM-FDA       | 14.51 | 8.50  | 0.79 | 0.71 | 0.89 | 15.82 | 9.11  | 0.60 | 0.52 | 0.77 |
| LSTM-PSO       | 15.04 | 8.33  | 0.75 | 0.77 | 0.86 | 13.85 | 7.94  | 0.70 | 0.83 | 0.83 |
| RF             | 25.41 | 14.97 | 0.23 | 0.15 | 0.57 | 28.26 | 15.32 | 0.23 | 0.14 | 0.59 |
| RF-FDA         | 9.94  | 4.71  | 0.88 | 0.83 | 0.94 | 19.58 | 8.24  | 0.66 | 0.55 | 0.83 |
| RF-PSO         | 10.03 | 4.49  | 0.89 | 0.82 | 0.95 | 16.78 | 7.62  | 0.58 | 0.63 | 0.76 |
| XGBoost        | 20.80 | 11.39 | 0.52 | 0.66 | 0.73 | 20.17 | 11.60 | 0.29 | 0.55 | 0.59 |
| XGBoost-FDA    | 7.02  | 4.44  | 0.94 | 0.93 | 0.97 | 17.75 | 8.82  | 0.70 | 0.70 | 0.84 |
| XGBoost-PSO    | 3.44  | 2.36  | 0.99 | 0.97 | 0.99 | 18.82 | 8.96  | 0.66 | 0.71 | 0.81 |

Continued Table S1: Comparison of machine learning model performance in independent and optimized states during training and testing phases.

| Model          | Train |       |      |      |      | Test  |       |      |      |      |
|----------------|-------|-------|------|------|------|-------|-------|------|------|------|
| M <sub>5</sub> | RMSE  | MAE   | NSE  | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -    | -    | -    | 21.77 | 10.04 | 0.42 | 0.53 | 0.66 |
| KNN-FDA        | -     | -     | -    | -    | -    | 19.88 | 7.76  | 0.56 | 0.51 | 0.75 |
| KNN-PSO        | -     | -     | -    | -    | -    | 24.36 | 10.70 | 0.52 | 0.46 | 0.77 |
| SVR            | 13.89 | 6.26  | 0.78 | 0.78 | 0.89 | 27.46 | 17.74 | 0.00 | 0.35 | 0.08 |
| SVR-FDA        | 13.18 | 5.95  | 0.80 | 0.81 | 0.90 | 14.38 | 7.54  | 0.67 | 0.58 | 0.82 |
| SVR-PSO        | 14.33 | 6.49  | 0.76 | 0.76 | 0.88 | 17.74 | 7.79  | 0.63 | 0.68 | 0.79 |
| LSTM           | 18.52 | 10.80 | 0.67 | 0.32 | 0.82 | 20.63 | 11.98 | 0.57 | 0.38 | 0.76 |
| LSTM-FDA       | 23.77 | 13.48 | 0.50 | 0.23 | 0.71 | 27.30 | 14.50 | 0.48 | 0.20 | 0.69 |
| LSTM-PSO       | 16.21 | 9.43  | 0.70 | 0.67 | 0.86 | 17.01 | 10.05 | 0.60 | 0.66 | 0.79 |
| RF             | 25.29 | 16.55 | 0.24 | 0.16 | 0.59 | 28.75 | 16.55 | 0.20 | 0.11 | 0.54 |
| RF-FDA         | 10.50 | 4.91  | 0.88 | 0.83 | 0.94 | 14.35 | 7.54  | 0.67 | 0.61 | 0.82 |
| RF-PSO         | 9.71  | 4.47  | 0.88 | 0.83 | 0.95 | 15.19 | 7.61  | 0.66 | 0.73 | 0.81 |
| XGBoost        | 20.49 | 11.14 | 0.51 | 0.63 | 0.71 | 22.01 | 10.85 | 0.47 | 0.58 | 0.68 |
| XGBoost-FDA    | 3.62  | 2.44  | 0.98 | 0.97 | 0.99 | 21.36 | 9.92  | 0.63 | 0.64 | 0.80 |
| XGBoost-PSO    | 5.38  | 3.50  | 0.97 | 0.95 | 0.98 | 19.15 | 9.16  | 0.62 | 0.69 | 0.79 |
| M <sub>6</sub> | RMSE  | MAE   | NSE  | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -    | -    | -    | 29.58 | 15.87 | 0.34 | 0.40 | 0.59 |
| KNN-FDA        | -     | -     | -    | -    | -    | 19.88 | 7.76  | 0.56 | 0.45 | 0.55 |
| KNN-PSO        | -     | -     | -    | -    | -    | 23.10 | 13.19 | 0.37 | 0.35 | 0.63 |
| SVR            | 13.31 | 6.22  | 0.80 | 0.79 | 0.90 | 28.36 | 18.04 | 0.00 | 0.35 | 0.08 |
| SVR-FDA        | 18.61 | 9.86  | 0.61 | 0.67 | 0.79 | 19.68 | 12.41 | 0.38 | 0.46 | 0.64 |
| SVR-PSO        | 22.70 | 12.09 | 0.43 | 0.41 | 0.69 | 18.68 | 11.46 | 0.50 | 0.52 | 0.72 |
| LSTM           | 26.61 | 14.29 | 0.10 | 0.05 | 0.49 | 33.95 | 17.05 | 0.21 | 0.36 | 0.62 |
| LSTM-FDA       | 22.05 | 13.50 | 0.47 | 0.46 | 0.68 | 20.80 | 13.35 | 0.30 | 0.31 | 0.55 |
| LSTM-PSO       | 19.94 | 13.11 | 0.56 | 0.55 | 0.76 | 19.51 | 13.07 | 0.39 | 0.40 | 0.63 |
| RF             | 26.43 | 15.69 | 0.21 | 0.12 | 0.56 | 23.95 | 14.29 | 0.09 | 0.04 | 0.30 |
| RF-FDA         | 13.63 | 9.30  | 0.79 | 0.75 | 0.90 | 19.93 | 13.31 | 0.41 | 0.40 | 0.65 |
| RF-PSO         | 13.78 | 7.61  | 0.79 | 0.71 | 0.91 | 18.73 | 12.50 | 0.44 | 0.55 | 0.66 |
| XGBoost        | 23.65 | 14.38 | 0.37 | 0.49 | 0.61 | 23.27 | 14.68 | 0.19 | 0.44 | 0.50 |
| XGBoost-FDA    | 14.28 | 10.01 | 0.77 | 0.76 | 0.99 | 22.13 | 13.22 | 0.33 | 0.59 | 0.62 |
| XGBoost-PSO    | 13.30 | 9.36  | 0.80 | 0.79 | 0.90 | 22.10 | 13.63 | 0.40 | 0.51 | 0.63 |
| M <sub>7</sub> | RMSE  | MAE   | NSE  | KGE  | R    | RMSE  | MAE   | NSE  | KGE  | R    |
| KNN            | -     | -     | -    | -    | -    | 18.65 | 9.89  | 0.41 | 0.61 | 0.69 |
| KNN-FDA        | -     | -     | -    | -    | -    | 17.89 | 8.80  | 0.57 | 0.64 | 0.78 |
| KNN-PSO        | -     | -     | -    | -    | -    | 23.82 | 10.43 | 0.47 | 0.45 | 0.72 |
| SVR            | 10.91 | 5.94  | 0.86 | 0.82 | 0.94 | 27.35 | 17.83 | 0.00 | 0.30 | 0.11 |
| SVR-FDA        | 13.02 | 5.89  | 0.81 | 0.83 | 0.90 | 17.55 | 8.20  | 0.81 | 0.59 | 0.76 |
| SVR-PSO        | 15.41 | 6.93  | 0.74 | 0.73 | 0.87 | 14.47 | 7.41  | 0.66 | 0.72 | 0.82 |
| LSTM           | 27.11 | 14.60 | 0.16 | 0.15 | 0.59 | 25.65 | 14.14 | 0.09 | 0.44 | 0.58 |
| LSTM-FDA       | 20.69 | 10.44 | 0.58 | 0.47 | 0.76 | 13.89 | 8.78  | 0.67 | 0.47 | 0.82 |
| LSTM-PSO       | 14.96 | 7.85  | 0.73 | 0.75 | 0.86 | 17.40 | 8.56  | 0.70 | 0.66 | 0.83 |
| RF             | 25.76 | 14.46 | 0.26 | 0.17 | 0.66 | 21.32 | 14.10 | 0.27 | 0.18 | 0.64 |
| RF-FDA         | 9.73  | 4.43  | 0.89 | 0.85 | 0.95 | 17.17 | 8.03  | 0.58 | 0.51 | 0.77 |
| RF-PSO         | 10.30 | 4.63  | 0.88 | 0.81 | 0.94 | 15.42 | 7.84  | 0.64 | 0.74 | 0.80 |
| XGBoost        | 20.56 | 11.22 | 0.50 | 0.64 | 0.71 | 23.11 | 12.17 | 0.42 | 0.57 | 0.65 |
| XGBoost-FDA    | 12.50 | 7.05  | 0.80 | 0.82 | 0.90 | 19.58 | 9.55  | 0.68 | 0.70 | 0.83 |
| XGBoost-PSO    | 9.00  | 5.38  | 0.89 | 0.88 | 0.95 | 21.50 | 9.55  | 0.68 | 0.61 | 0.80 |