

1 **Supplementary Information**

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3 **Breaking the Rate-Limiting Barrier in Solid-Solid Sulfur Redox**

4 **Reactions via Spin-State Engineering**

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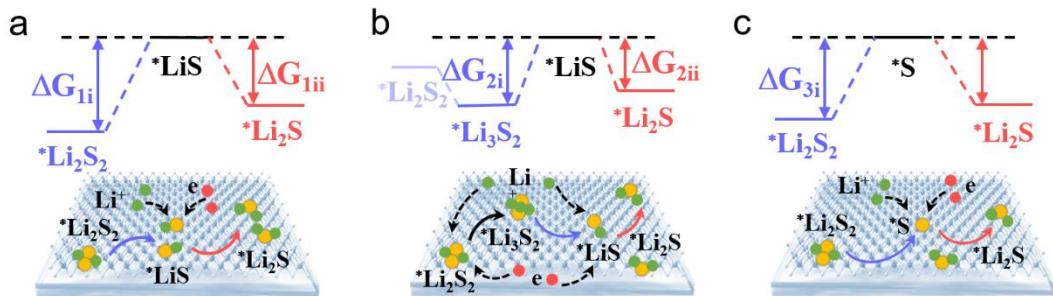
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Supplementary Fig. 1 | Schematic of the three possible reaction paths in converting Li_2S_2 to Li_2S . a, $\text{*Li}_2\text{S}_2$ - *LiS - $\text{*Li}_2\text{S}$. b, $\text{*Li}_2\text{S}_2$ - $\text{*Li}_3\text{S}_2$ - *LiS - $\text{*Li}_2\text{S}$. c, $\text{*Li}_2\text{S}_2$ - *S - $\text{*Li}_2\text{S}$. The yellow and green spheres represent the S and Li atoms, respectively.

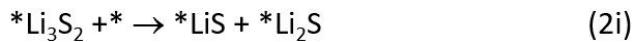
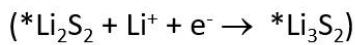
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Pathway 1:



Pathway 2:



Pathway 3:

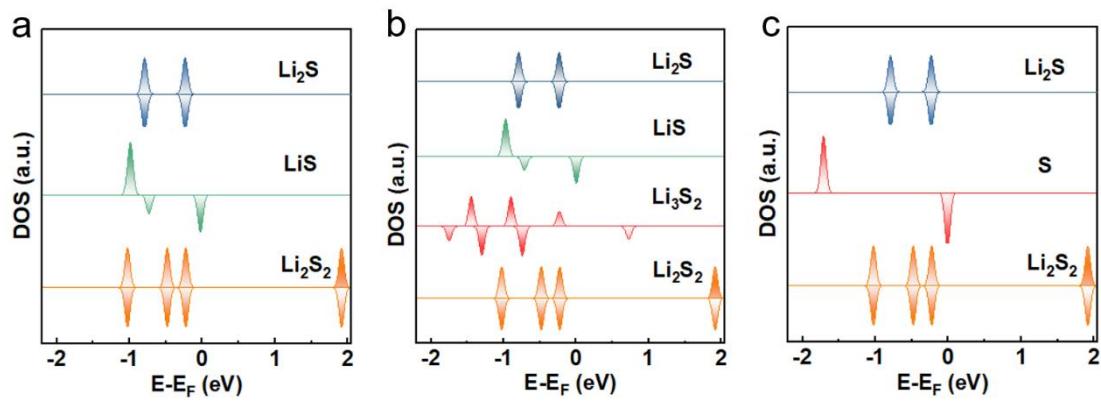


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24 **Supplementary Fig. 2** | The detailed reaction equation for the formation of three
25 possible intermediates (${}^* \text{LiS}$, ${}^* \text{Li}_3\text{S}_2$, and ${}^* \text{S}$) during the Li_2S_2 to Li_2S reaction's three
26 possible reaction paths.

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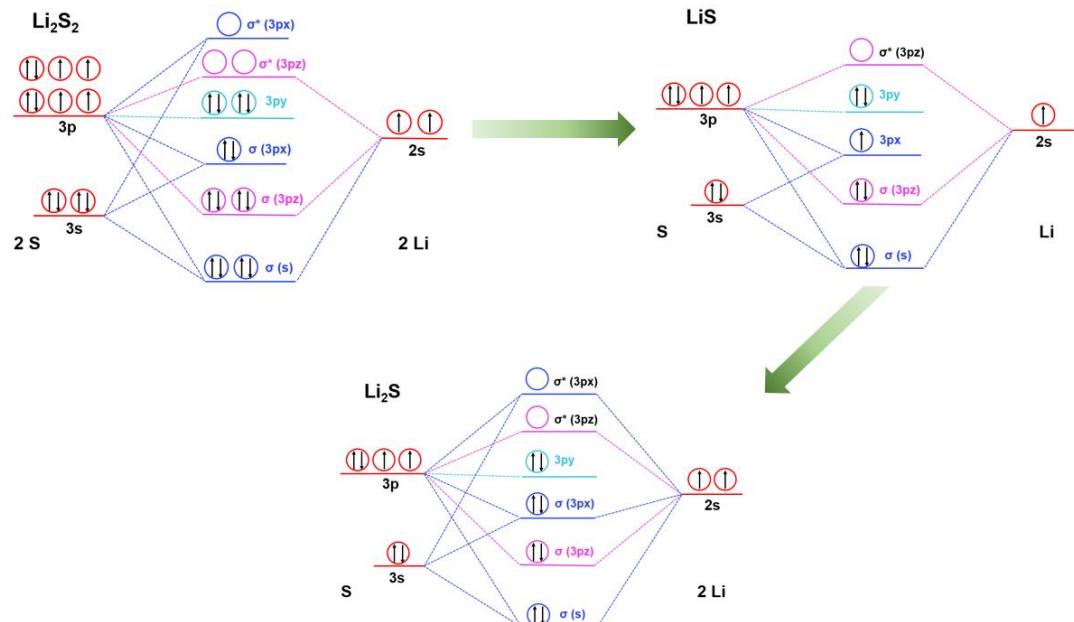
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30 **Supplementary Fig. 3** | The DOS of each transition state of a, *Li₂S₂ - *LiS - *Li₂S,
 31 b, *Li₂S₂ - *Li₃S₂ - *LiS - *Li₂S, c, *Li₂S₂ - *S - *Li₂S.

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Pathway 1



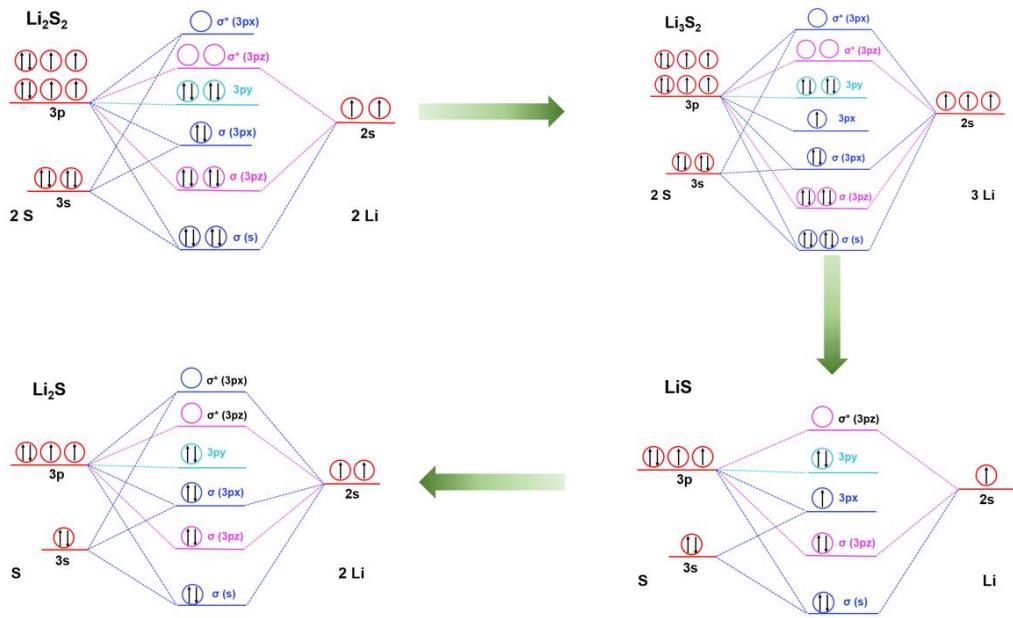
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36 **Supplementary Fig. 4** | Schematic of the degeneracy of molecular orbitals in path 1,
37 (Li_2S_2 - LiS - Li_2S).

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Pathway 2



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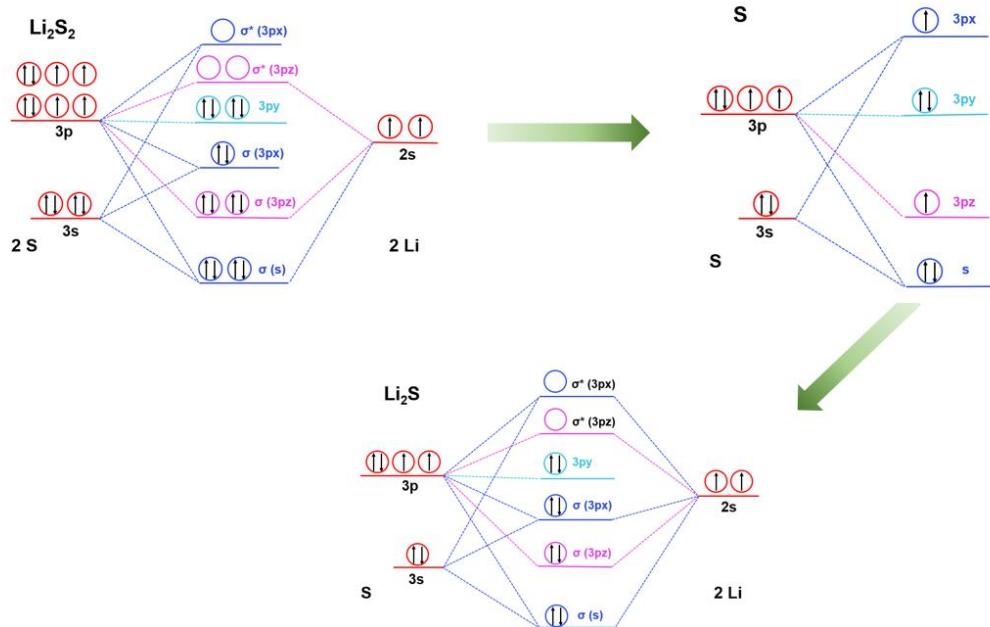
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41 **Supplementary Fig. 5** | Schematic of the degeneracy of molecular orbitals in path 2
42 (Li_2S_2 - Li_3S_2 - LiS - Li_2S).

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Pathway 3

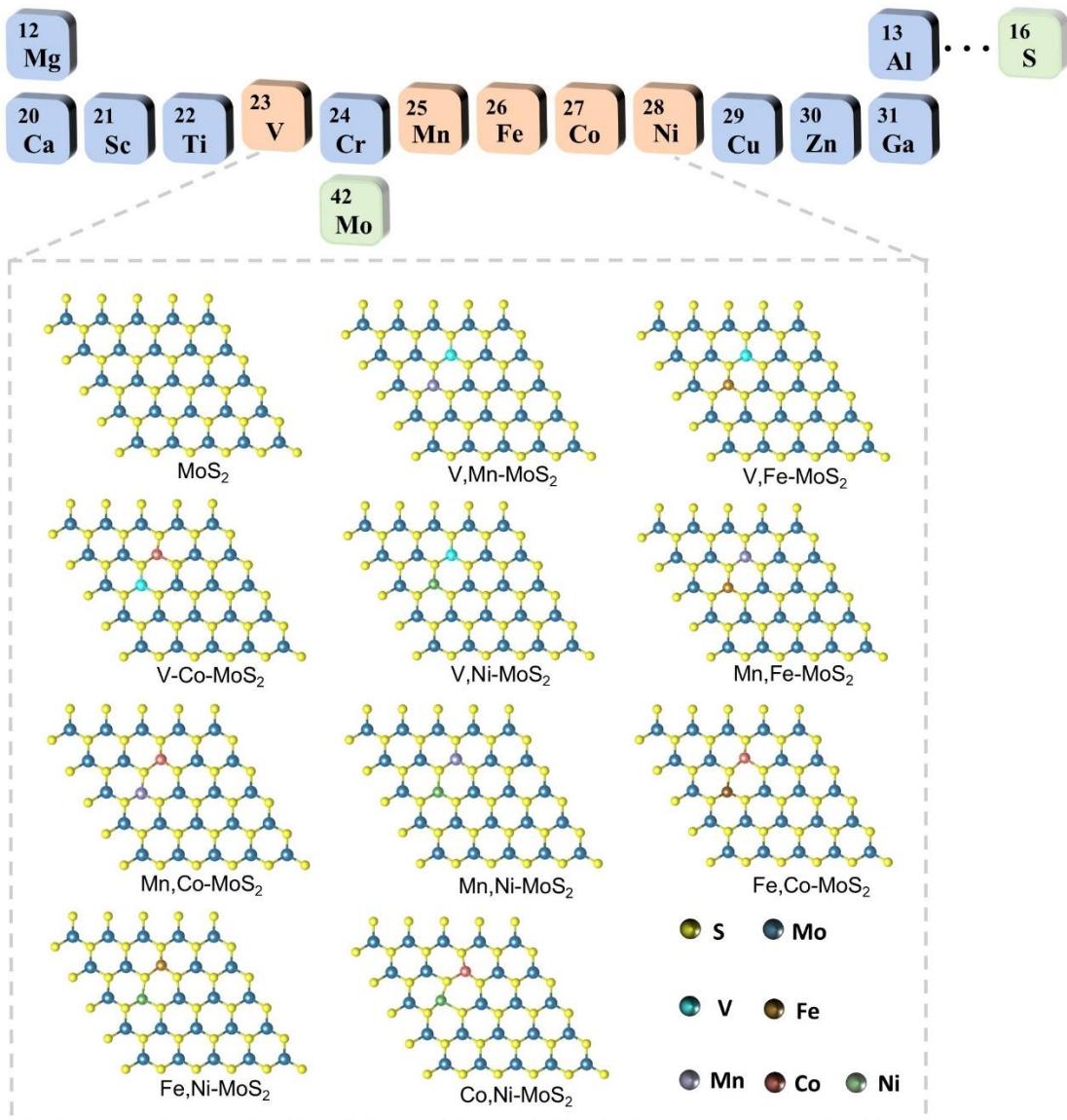


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47 **Supplementary Fig. 6** | Schematic of the degeneracy of molecular orbitals in path 3
48 (Li_2S_2 - S - Li_2S).

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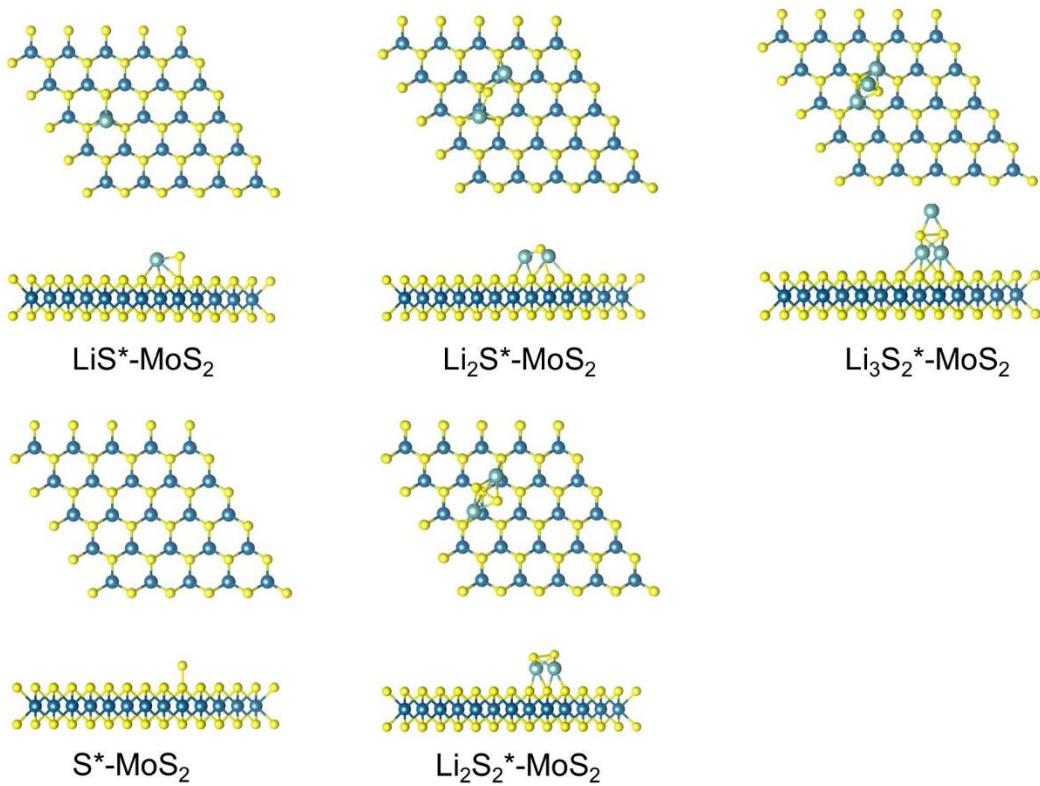


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52 **Supplementary Fig. 7** | The optimized structures of pristine MoS_2 and ten MoS_2
53 materials doped with two different atoms.

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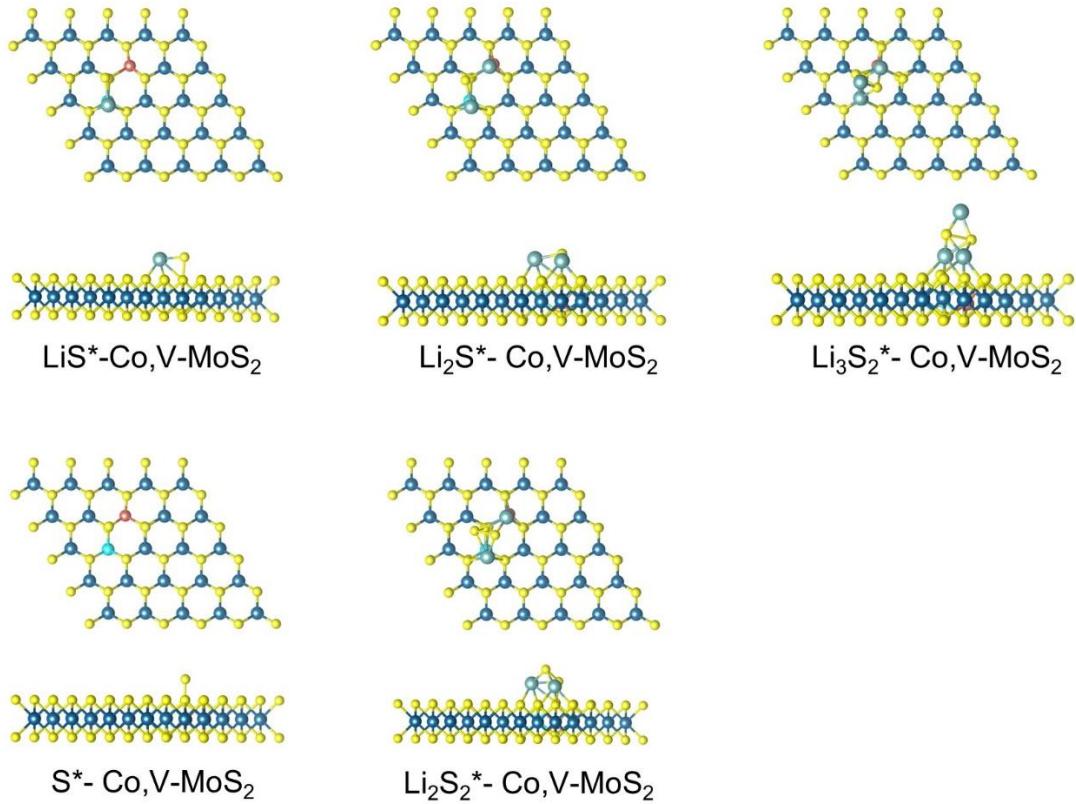
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57 **Supplementary Fig. 8** | The optimized structures of the initial state $^*\text{Li}_2\text{S}_2$, three
58 intermediates ($^*\text{LiS}$, $^*\text{Li}_3\text{S}_2$, and $^*\text{S}$), and the final state $^*\text{Li}_2\text{S}$ on the MoS_2 surface.
59 Yellow, blue, and green spheres denote S, Mo, and Li atoms, respectively.

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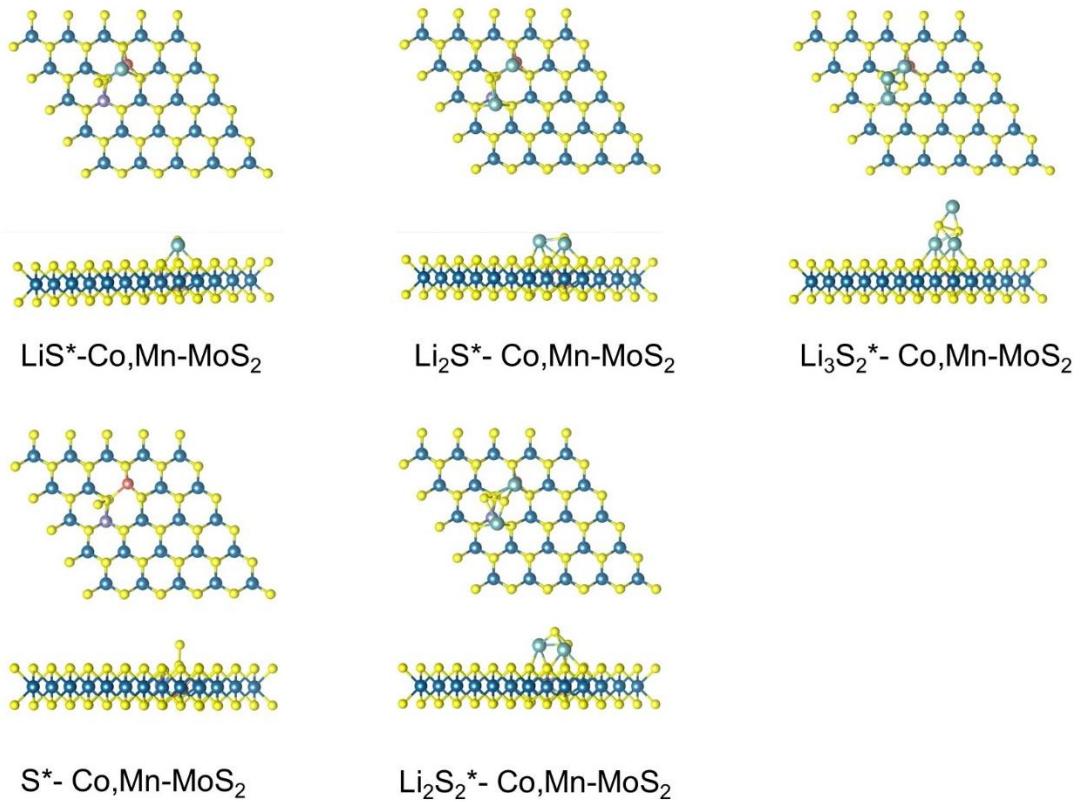
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64 **Supplementary Fig. 9** | The optimized structures of initial state *Li₂S₂, three
 65 intermediates (*LiS, *Li₃S₂, and *S), and final state *Li₂S on the Co,V-MoS₂ surface.
 66 Yellow, blue, slight blue, cyan, and pink spheres denote S, Mo, Li, V, and Co atoms,
 67 respectively.

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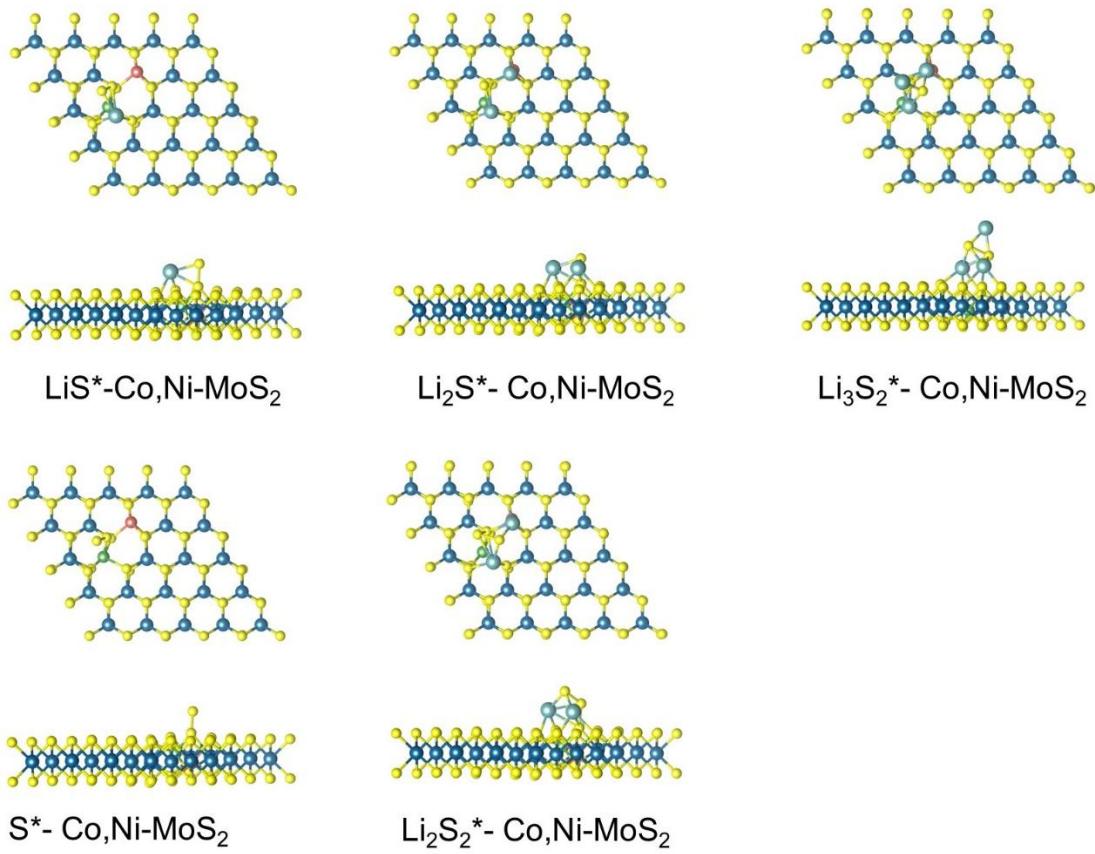
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73 **Supplementary Fig. 10** | The optimized structures of initial state *Li₂S₂, three
 74 intermediates (*LiS, *Li₃S₂, and *S), and final state *Li₂S on the Co,Mn-MoS₂
 75 surface. Yellow, blue, slight blue, purple, and pink spheres denote S, Mo, Li, Mn, and
 76 Co atoms, respectively.

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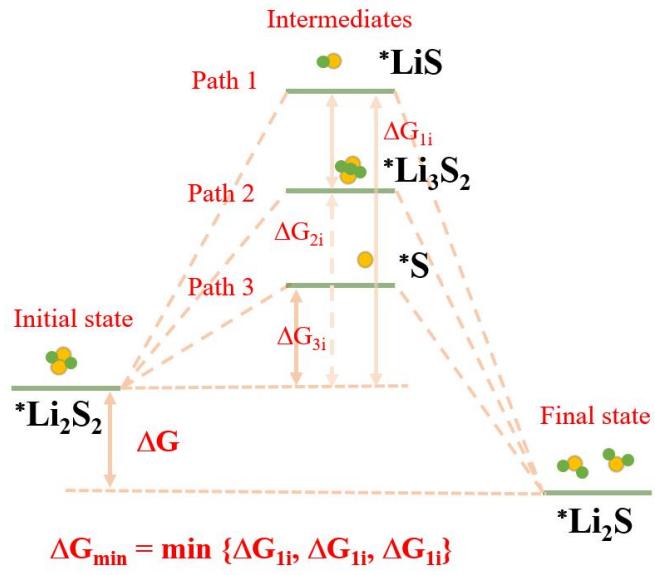
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82 **Supplementary Fig. 11** | The optimized structures of initial state $^*\text{Li}_2\text{S}_2$, three
 83 intermediates ($^*\text{LiS}$, $^*\text{Li}_3\text{S}_2$, and $^*\text{S}$), and final state $^*\text{Li}_2\text{S}$ on the Co,Ni-MoS₂ surface.
 84 Yellow, blue, slight blue, green, and pink spheres denote S, Mo, Li, Ni, and Co atoms,
 85 respectively.

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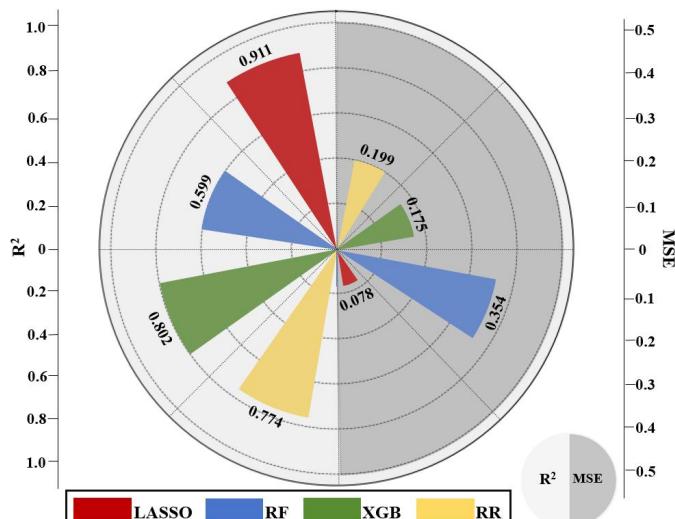


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90 **Supplementary Fig. 12** | Schematic of the Gibbs free energy charge (ΔG) between
91 Li_2S_2 , Li_2S , and the different intermediates.

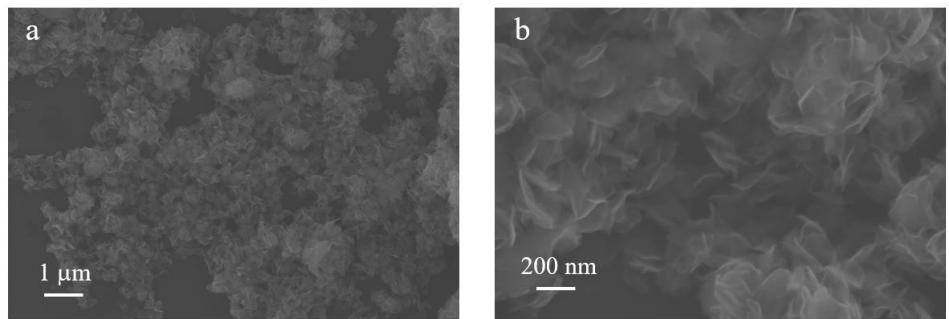
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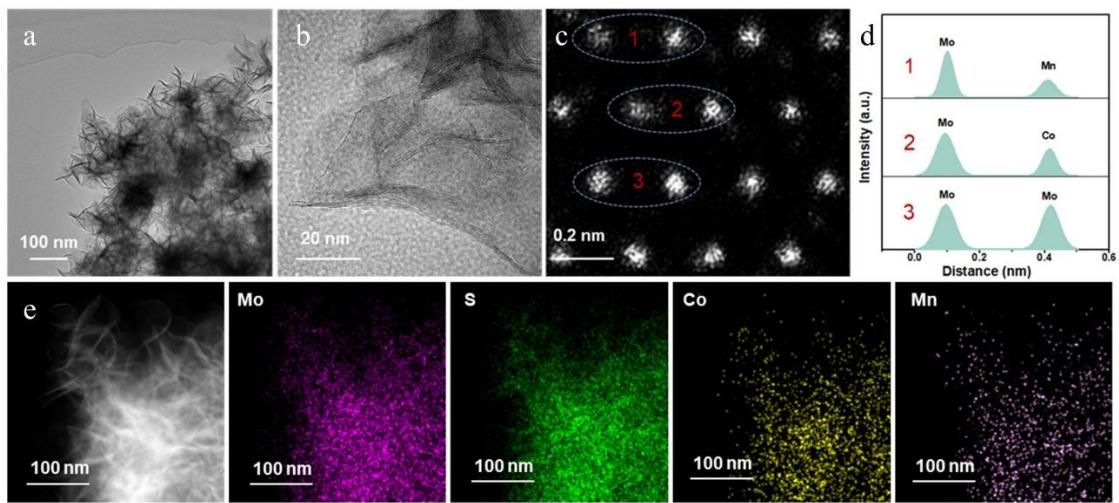
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95 **Supplementary Fig. 13** | The R^2 and MSE from optimal ML models, including the
96 LASSO (Least Absolute Shrinkage and Selection Operator) model, the RF (Random
97 Forest) model, the XGB (Extreme Gradient Boosting) model, and the RR (Ridge
98 Regression) model.

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103 **Supplementary Fig. 14** | The morphology of MoS₂. **a**, SEM image, **b**, TEM image.
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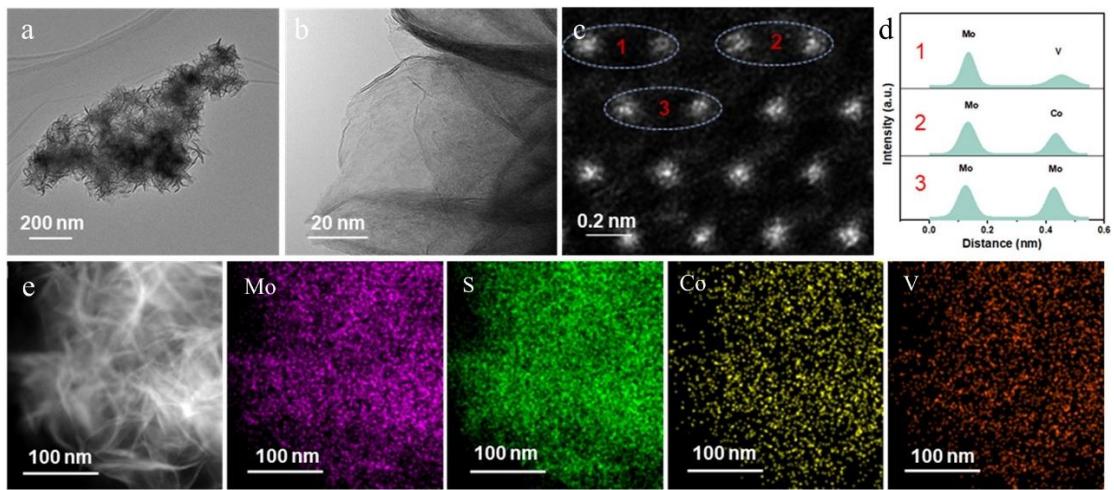


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107 **Supplementary Fig. 15** | The morphology of Co,Mn-MoS₂, **a**, TEM image, **b**,
108 HRTEM image. **c**, HAADF-STEM image, **d**, the corresponding linear intensity
109 profiles, and **e**, the elemental EDS maps.

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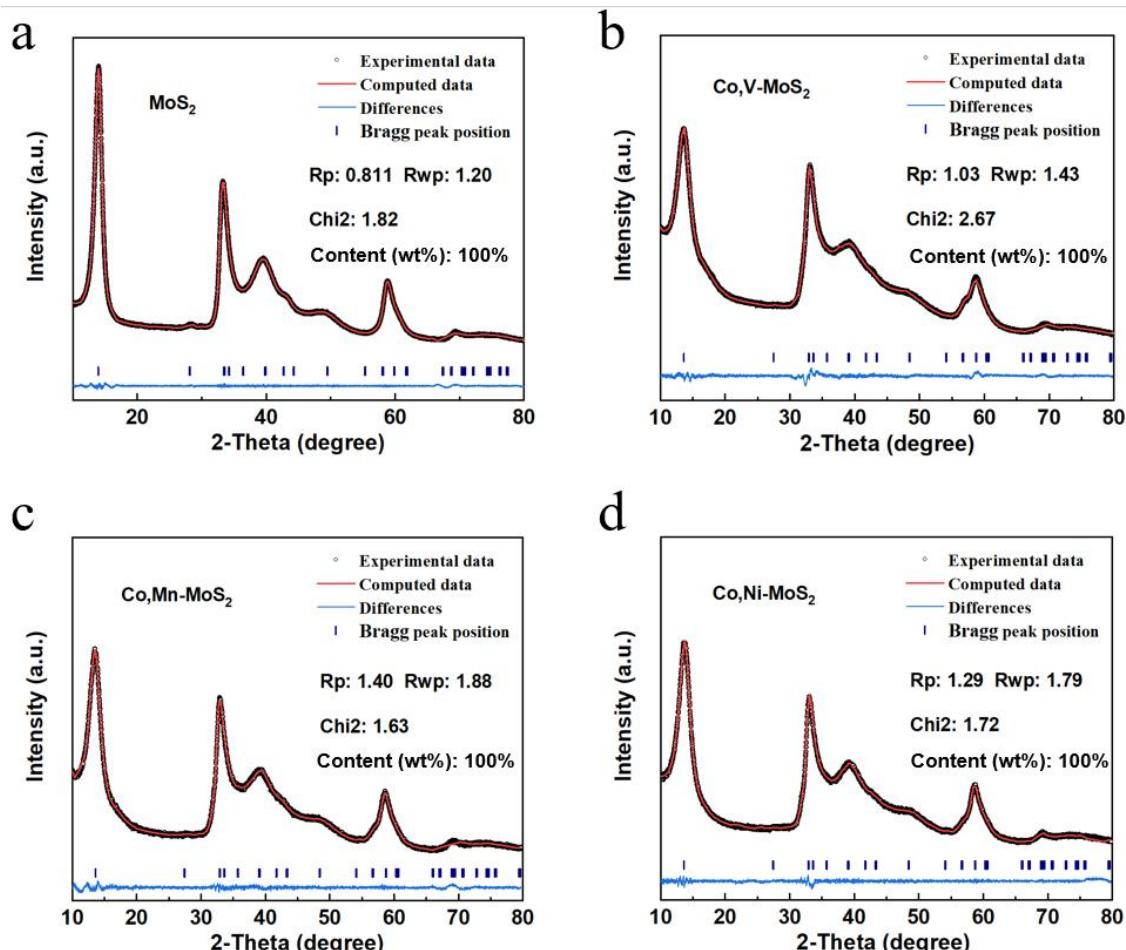


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113 **Supplementary Fig. 16** | The morphology of $\text{Co}_3\text{V}-\text{MoS}_2$, **a**, TEM image, **b**, HRTEM
114 image. **c**, HAADF-STEM image, **d**, the corresponding linear intensity profiles, and **e**,
115 the elemental EDS maps.

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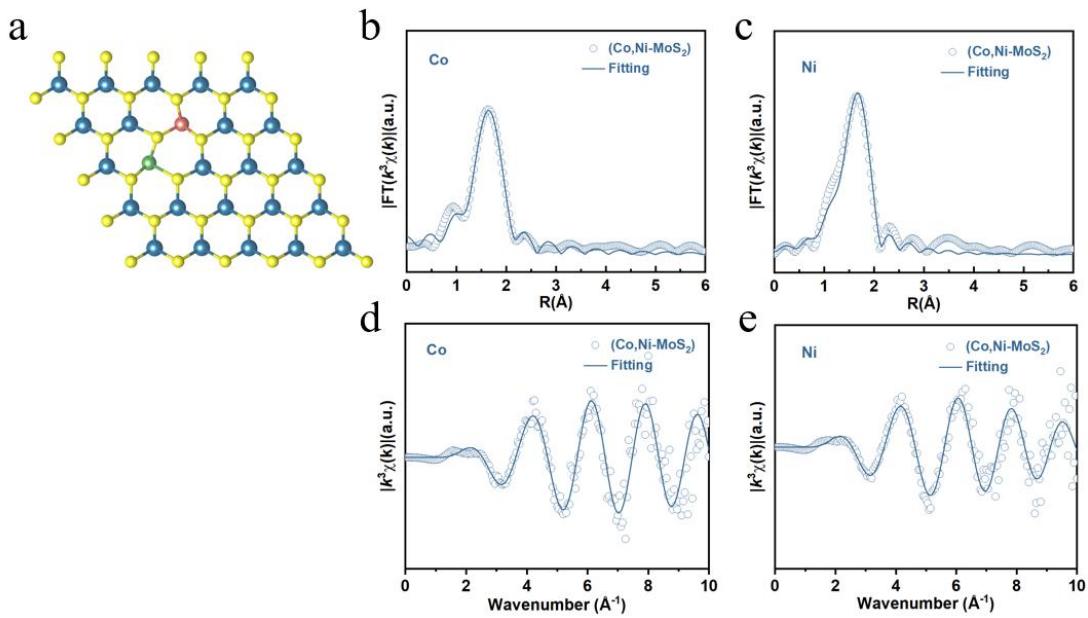


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119 **Supplementary Fig. 17** | Rietveld refinement XRD patterns for **a**, MoS₂, **b**,
120 Co,V-MoS₂, **c**, Co,Mn-MoS₂, and **d**, Co,Ni-MoS₂.

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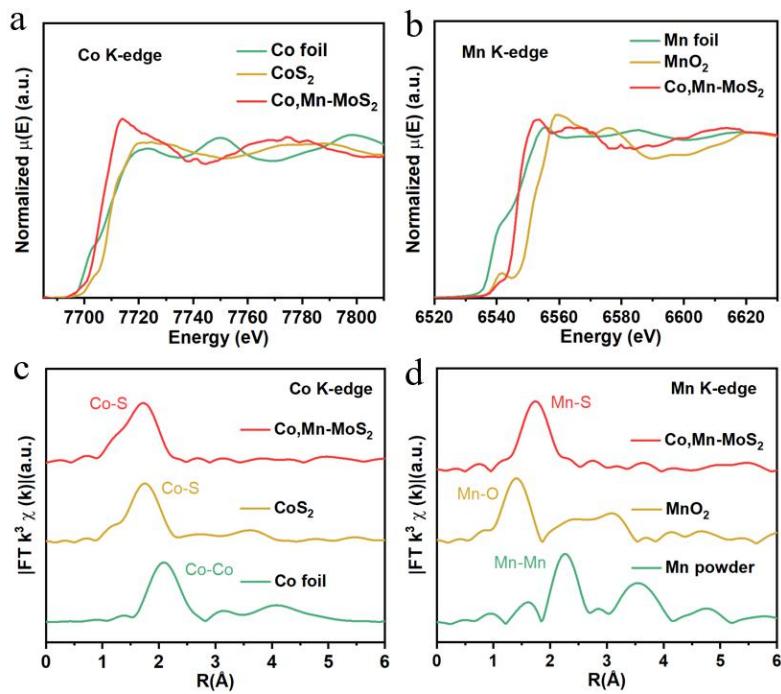


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124 **Supplementary Fig. 18 | a**, The atom structure of Co,Ni-MoS₂ obtained by DFT. **b**,
 125 Co K-edge and **c**, Ni K-edge EXAFS fitting spectra of the Co,Ni-MoS₂. **d**, The
 126 corresponding Co K-edge and **e**, Ni K-edge EXAFS oscillations were extracted from
 127 the K-edge spectra of this material in k space.

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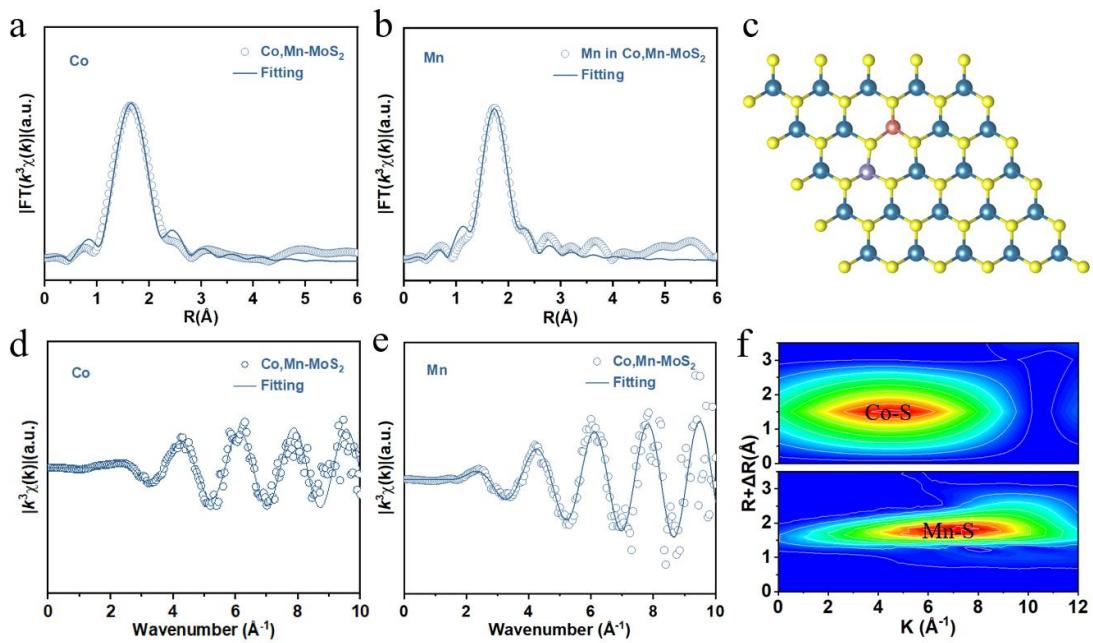


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131 **Supplementary Fig. 19 | a**, The Co K-edge and **b**, Mn K-edge XANES spectra of
 132 Co,Mn-MoS₂. **c** and **d**, the corresponding fourier-transform k^3 -weighted EXAFS
 133 spectra of the samples.

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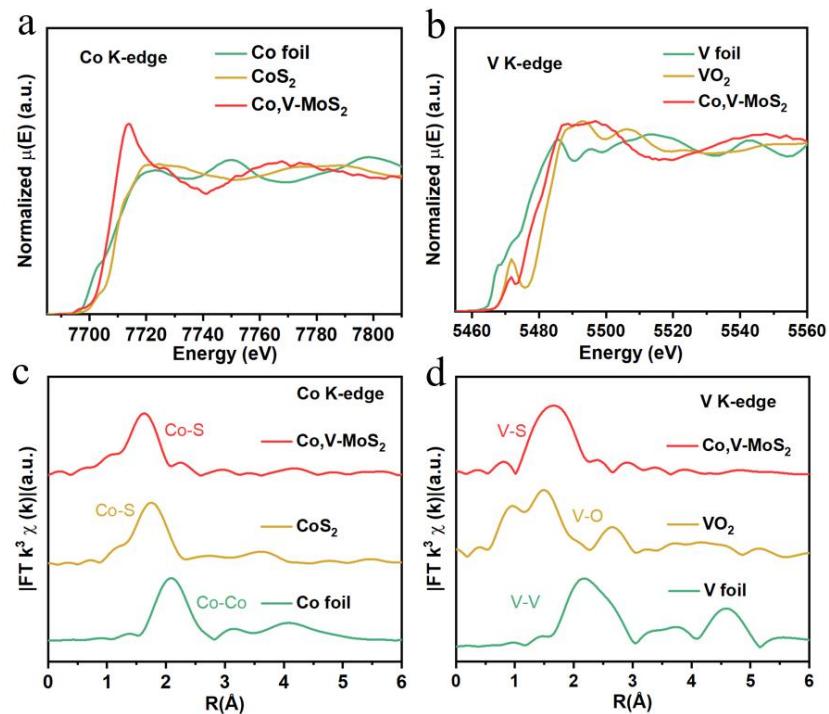
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137 **Supplementary Fig. 20** | **a**, The Co K-edge and **b**, Mn K-edge EXAFS fit spectra of
138 Co,Mn-MoS₂. **c**, The atomic structure of Co,Mn-MoS₂ obtained by DFT. **d**, The
139 corresponding Co K-edge and **e**, Mn K-edge EXAFS oscillations extracted from the
140 K-edge spectra of the composites in k space. **f**, The corresponding wavelet-transform
141 contour plots of the EXAFS signal of the samples.

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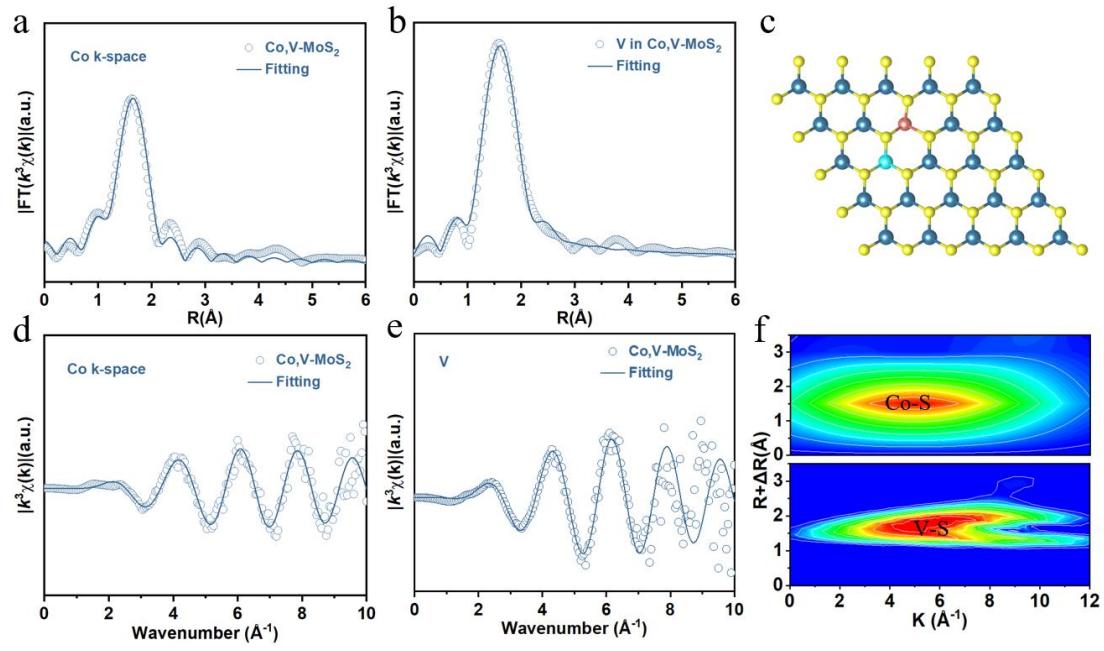
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146 **Supplementary Fig. 21 | a**, The Co K-edge and **b**, V K-edge XANES spectra of
 147 Co,V-MoS₂. **c** and **d**, the corresponding fourier-transform k^3 -weighted EXAFS spectra
 148 of the samples.

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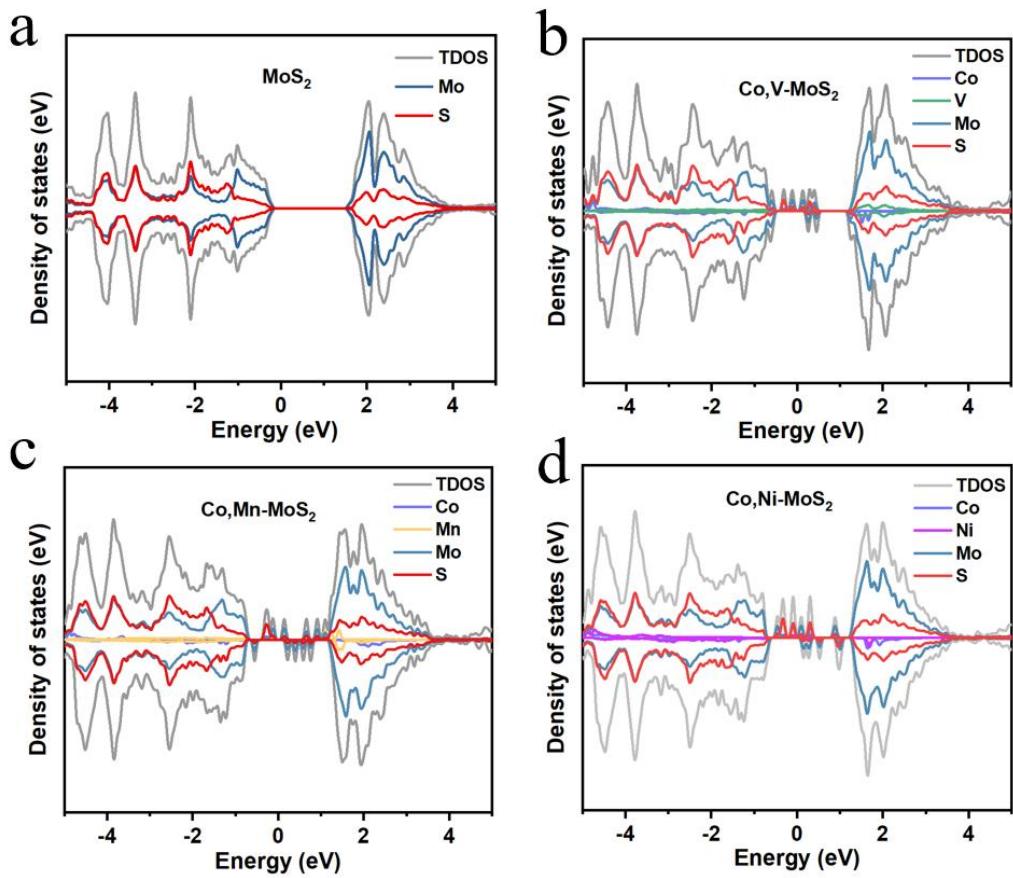


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152

153 **Supplementary Fig. 22 | a**, The Co K-edge and **b**, V K-edge EXAFS fitting spectra of
154 Co,V-MoS₂. **c**, The atomic structure of Co,V-MoS₂ obtained by DFT. **d**, The
155 corresponding Co K-edge and **e**, Mn K-edge EXAFS oscillations extracted from
156 K-edge spectra of the composites in k space. **f**, The corresponding wavelet-transform
157 contour plots of the EXAFS signal of the samples.

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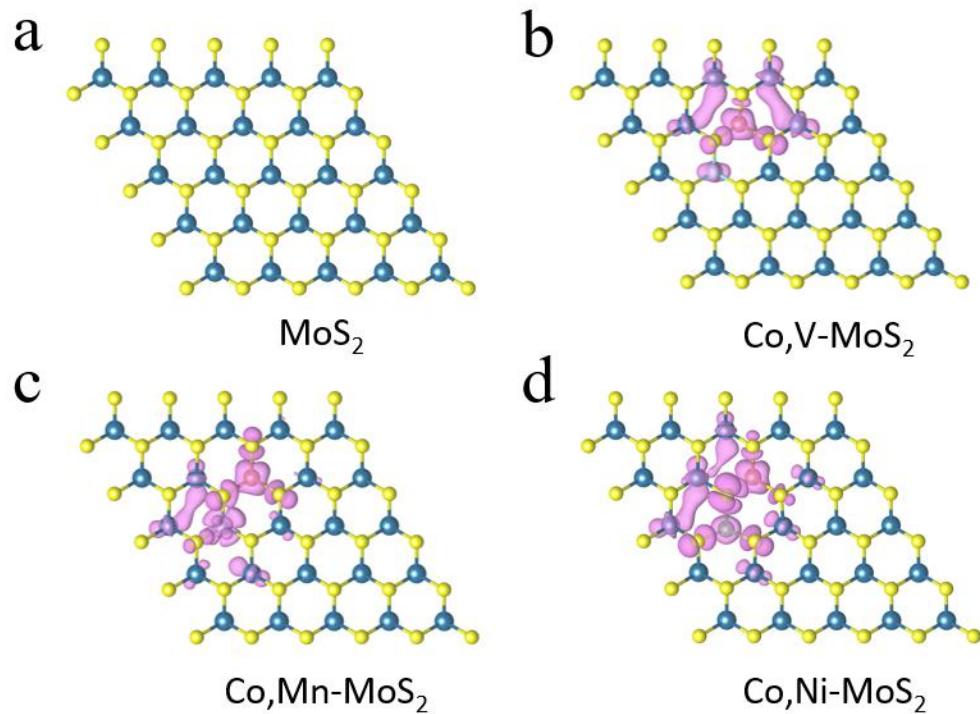


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161 **Supplementary Fig. 23** | The calculated DOS near the Fermi level for **a**, MoS₂, **b**,
 162 Co,V-MoS₂, **c**, Co,Mn-MoS₂, **d**, Co,Ni-MoS₂.

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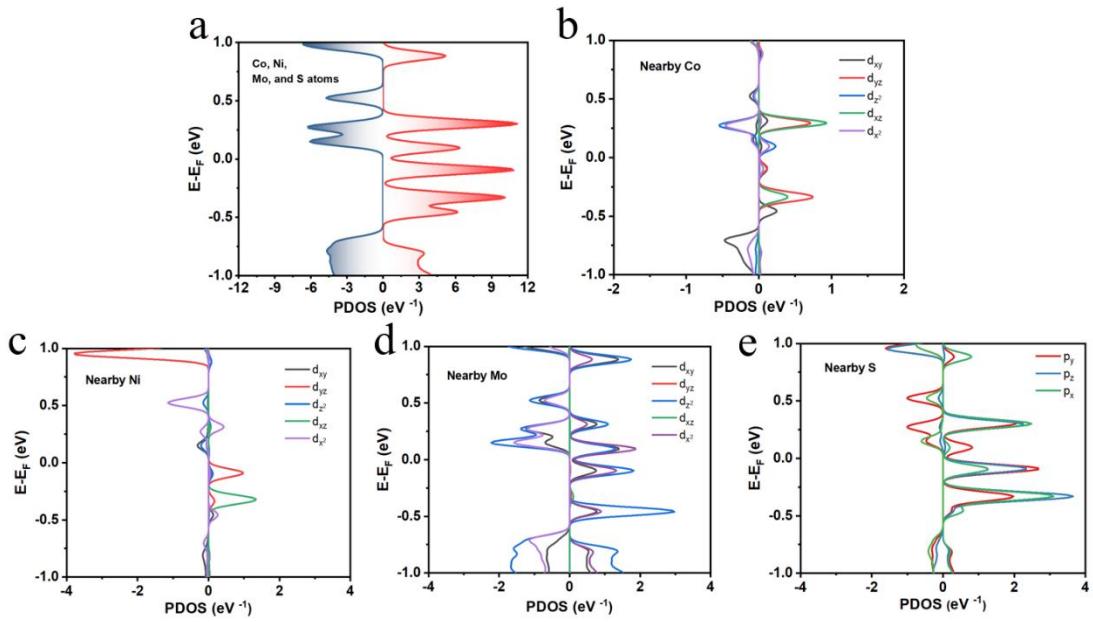
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166 **Supplementary Fig. 24** | Spin density plots of **a**, pristine MoS_2 , **b**, Co, V-MoS_2 , **c**,
167 Co, Mn-MoS_2 , and **d**, Co, Ni-MoS_2 . Yellow, blue, red, cyan, purple, and green spheres
168 denote S, Mo, Co, V, Mn, and Ni atoms, respectively. The light purple isosurfaces
169 show the spin-state density.

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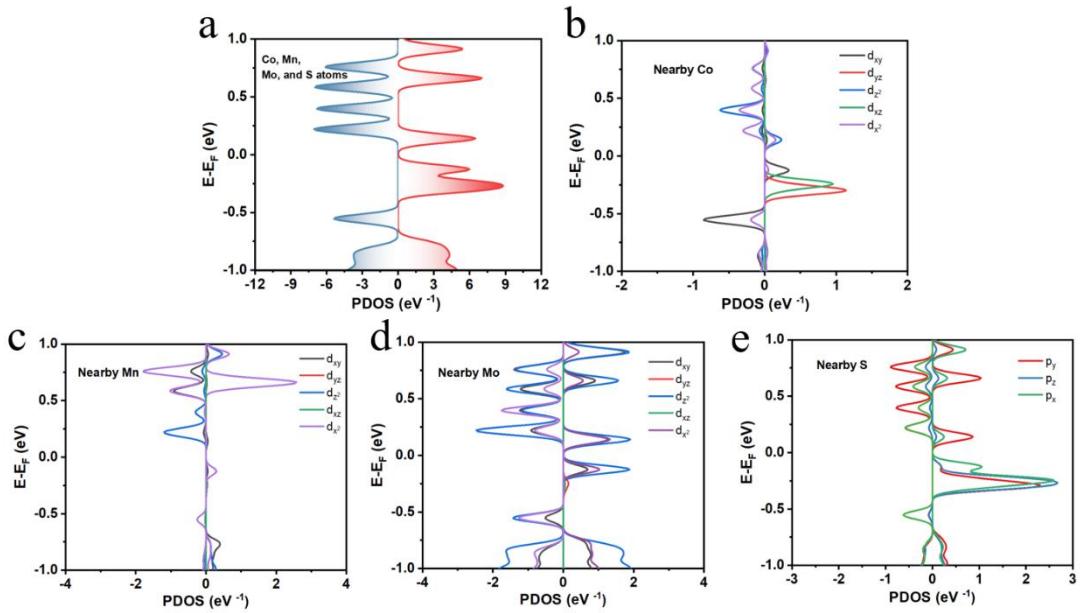


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174 **Supplementary Fig. 25 | a**, The calculated DOS near the Fermi level for Co,Ni-MoS₂.
 175 **b**, Total density of states and projected density of states of individual, **c**, Co_{Mo} and **d**,
 176 Ni_{Mo} sites with **e**, nearby S, and **f**, Mo atoms in Co,Ni-MoS₂.

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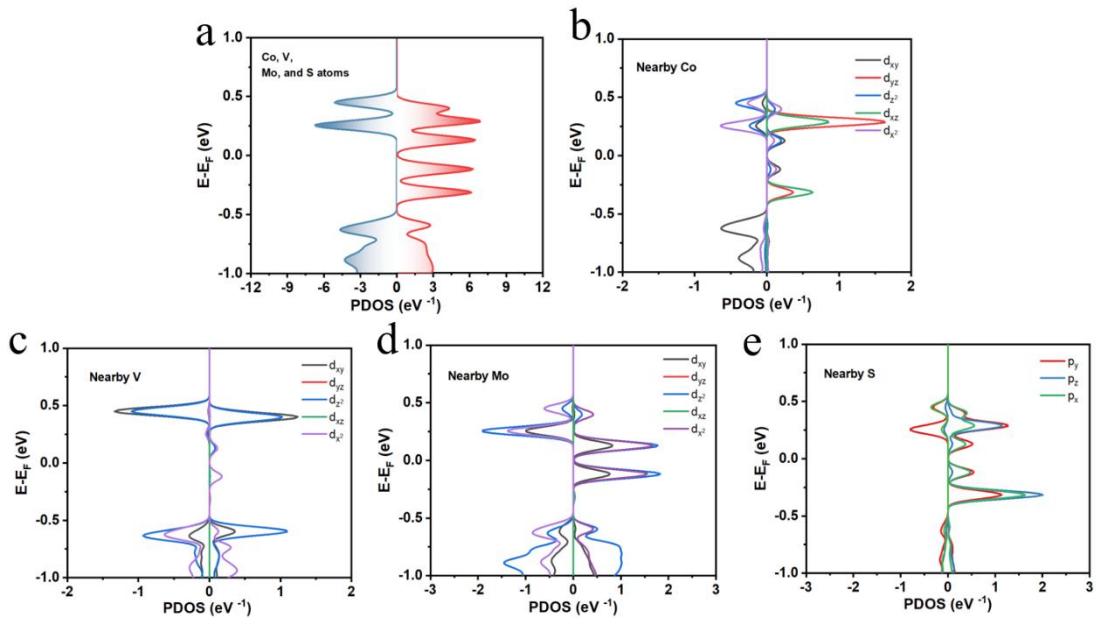


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180 **Supplementary Fig. 26 | a,** The calculated DOS near the Fermi level for
 181 Co,Mn-MoS₂. **b,** Total density of states and projected density of states of individual, **c,**
 182 Co_{Mo} and **d,** Mn_{Mo} sites with **e,** nearby S, and **f,** Mo atoms in Co,Mn-MoS₂.

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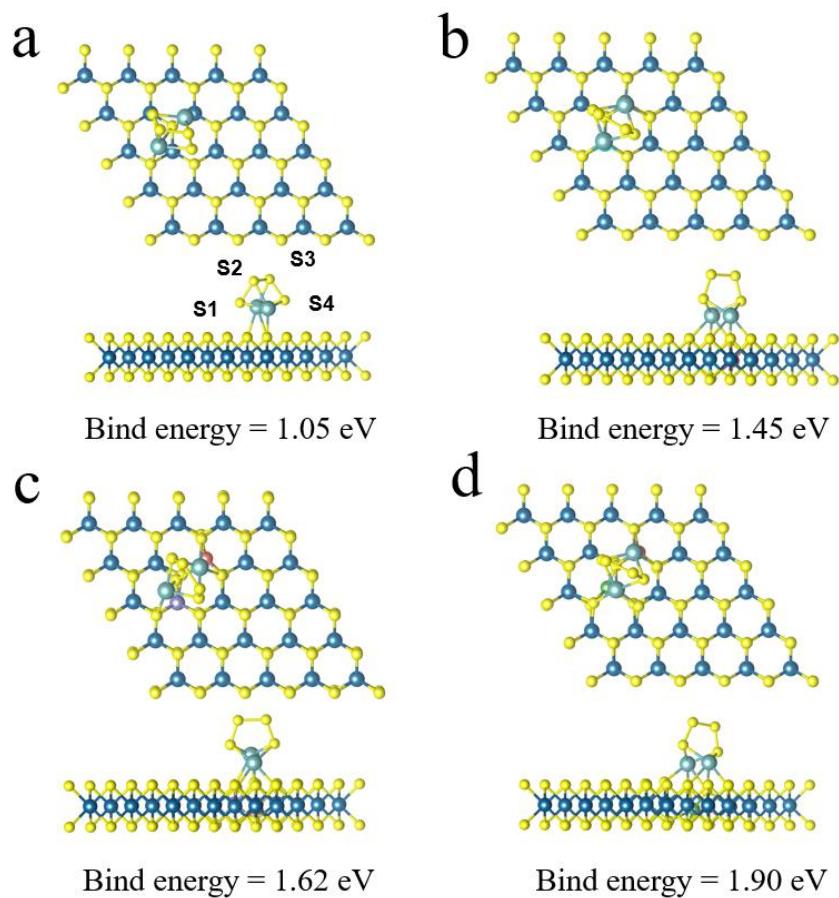


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185

186 **Supplementary Fig. 27 | a**, The calculated DOS near the Fermi level for $\text{Co}_3\text{V}_2\text{MoS}_2$.
 187 **b**, Total density of states and projected density of states of individual, **c**, Co_{Mo} and **d**,
 188 V_{Mo} sites with **e**, nearby S, and **f**, Mo atoms in $\text{Co}_3\text{V}_2\text{MoS}_2$.

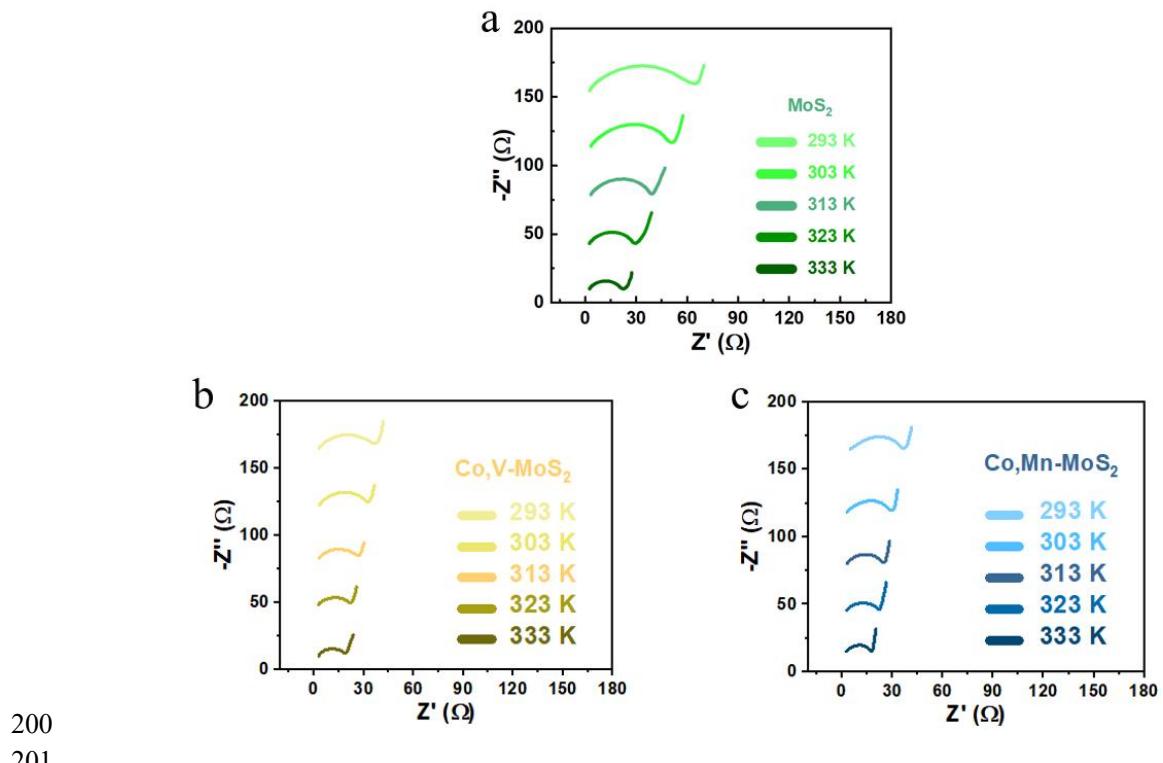
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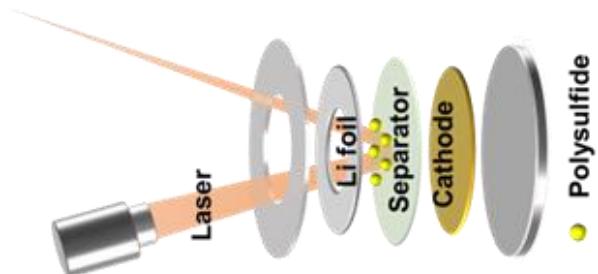
192 **Supplementary Fig. 28** | Top view and side view of the optimized adsorption
193 structures of Li_2S_4 on the **a**, MoS_2 , **b**, Co,V-MoS_2 , **c**, Co,Mn-MoS_2 , and
194 **d**, Co,Ni-MoS_2 surfaces, and the corresponding adsorption energies. Yellow, blue, slight
195 blue, cyan, purple, green, and pink spheres denote S, Mo, Li, V, Mn, Ni, and Co atoms,
196 respectively.

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202 **Supplementary Fig. 29** | EIS measurements for **a**, MoS_2 , **b**, Co,V-MoS_2 , and **c**,
203 Co,Mn-MoS_2 catalysts at different temperatures.

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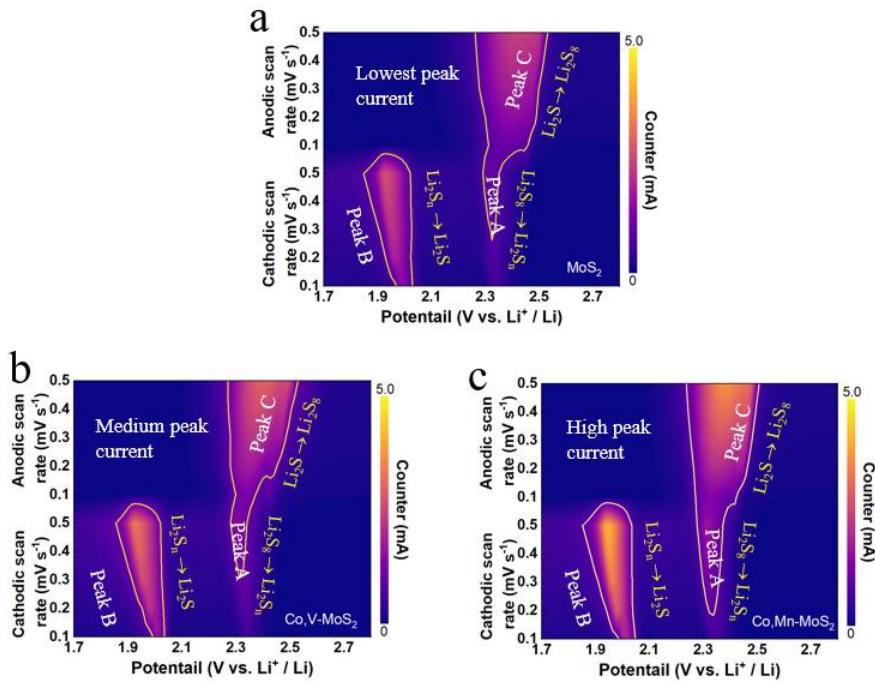


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207 **Supplementary Fig. 30** | Setup used for *in-situ* Raman spectroscopy analyses of the
208 cell configuration.

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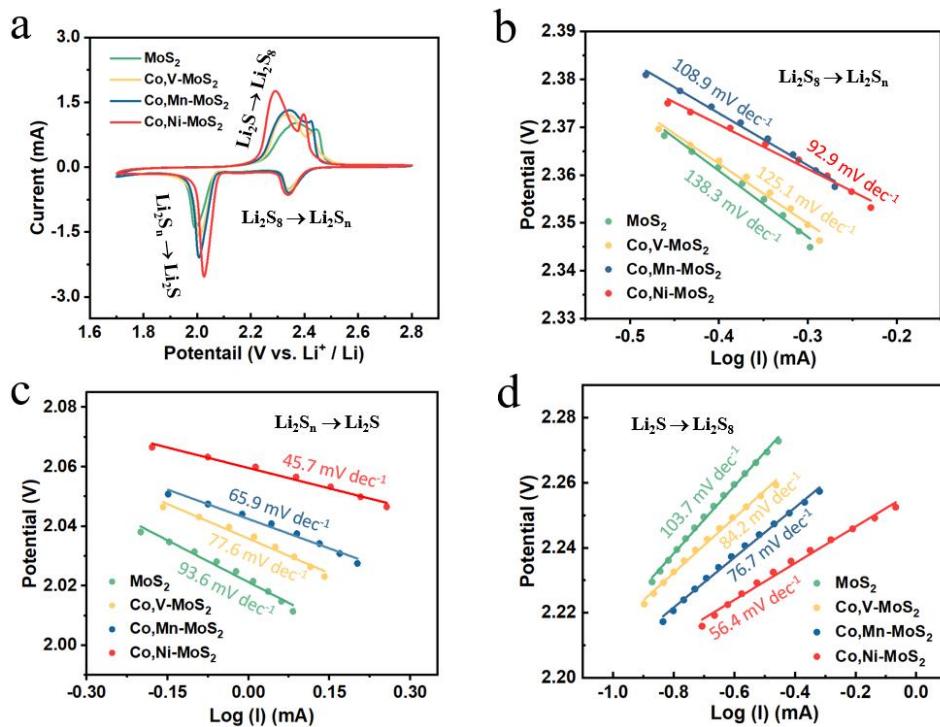


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212 **Supplementary Fig. 31** | CV profiles of **a**, MoS₂, **b**, Co,V-MoS₂, and **c**,
 213 Co,Mn-MoS₂-based cells were investigated at the different scan rates.

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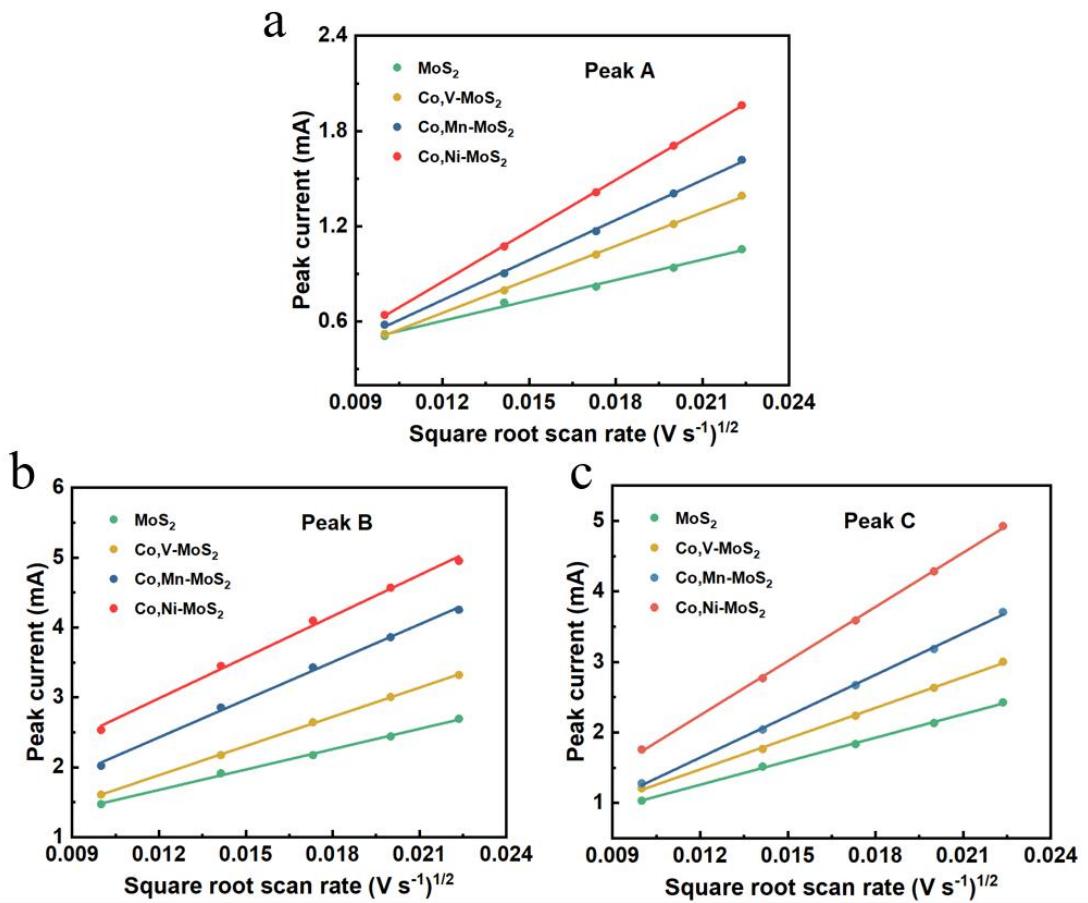


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217 **Supplementary Fig. 32 | a**, CV profiles of the cells with different catalysts. The
 218 corresponding Tafel slopes of **b**, peak A, **c**, peak B, and **d**, peak C, from the CV
 219 profiles.

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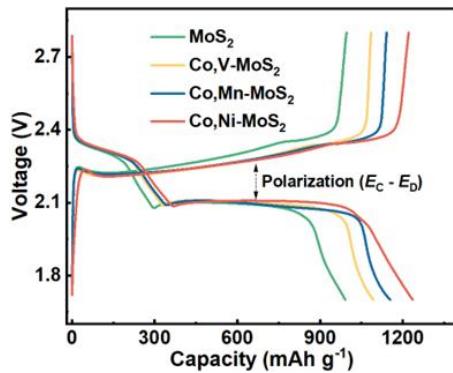


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223 **Supplementary Fig. 33 | a-c**, Li-ion diffusion properties of MoS₂, Co,V-MoS₂,
224 Co,Mn-MoS₂, and Co,Ni-MoS₂-based cell investigated by analyzing the CV peak
225 currents for peaks **(a)** A, **(b)** B, and **(c)** C as a function of the square root of the scan
226 rates.

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230 **Supplementary Fig. 34** | Galvanostatic charge-discharge profiles with cells with the
 231 different catalysts and the corresponding polarization ($E_C - E_D$). E_C , charge voltage;
 232 E_D , discharge voltage.

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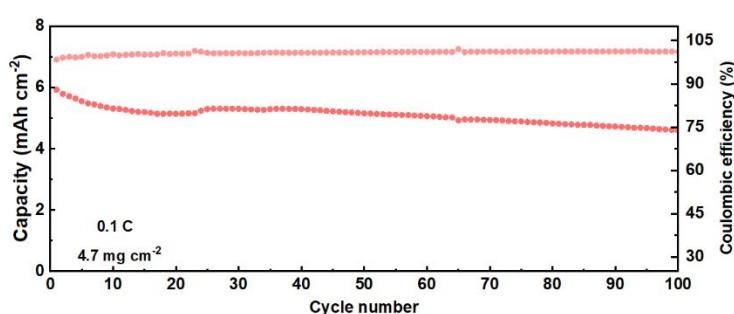
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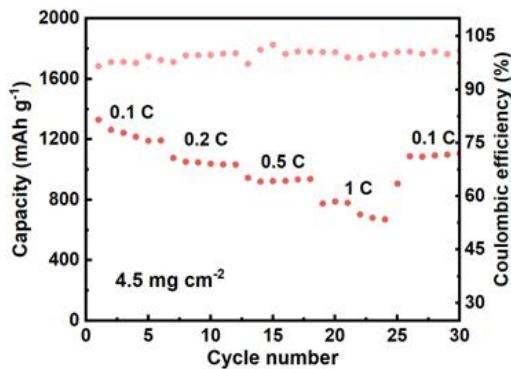


240

241 **Supplementary Fig. 35** | Cycling performance of Co,Ni-MoS₂-based cells with a
 242 high sulfur loading of 4.7 mg cm⁻² at 0.1 C.

243

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247 **Supplementary Fig. 36** | Rate performance of a Co,Ni-MoS₂-based cell with a high
248 sulfur loading of 4.5 mg cm⁻² at 0.1 C to 1 C.

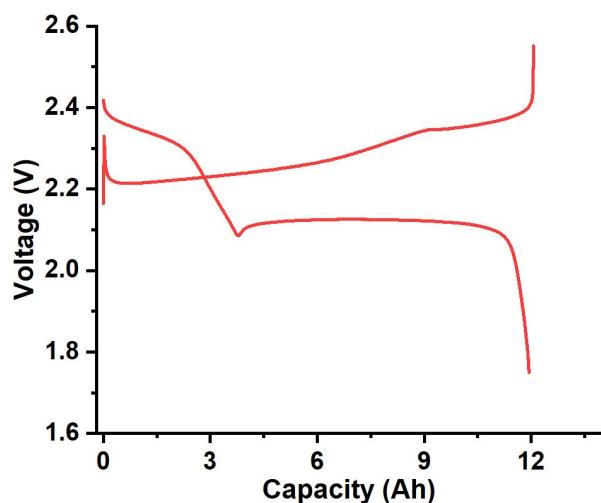
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256 **Supplementary Fig. 37** | Corresponding charge-discharge profiles of the 13.2
257 Ah-level pouch cells containing the Co,Ni-MoS₂ catalyst during the first cycle.

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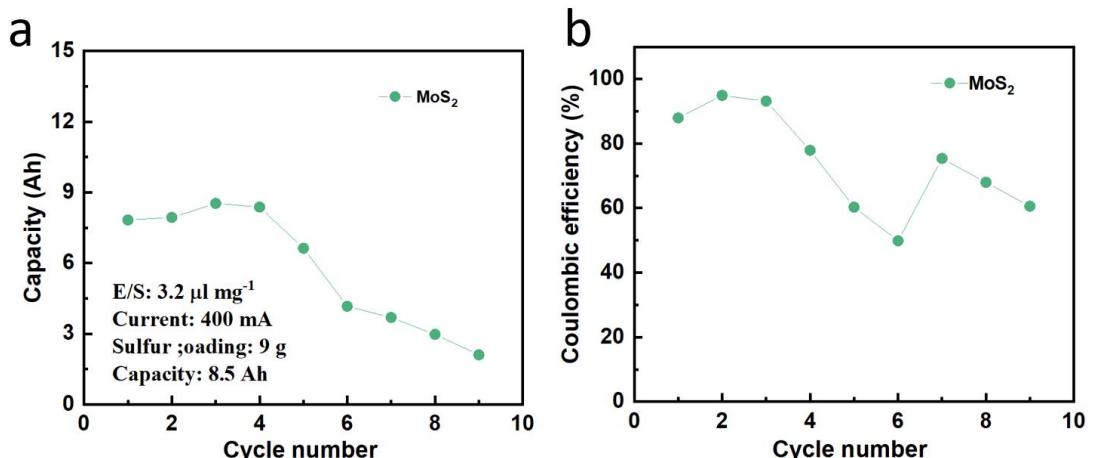


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260 **Supplementary Fig. 38** | Dimensions (length and width) of the pouch cell.

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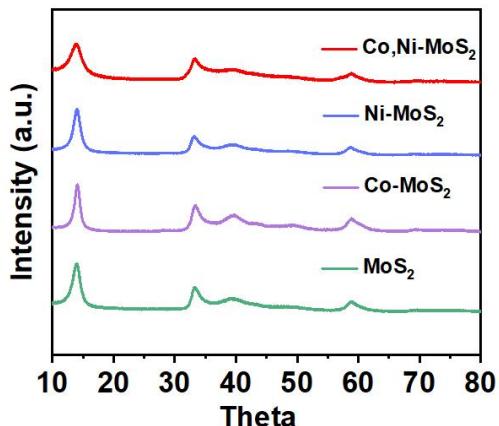


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264 **Supplementary Fig. 39 | a**, Cycling performance and **b**, Coulombic efficiency of a
 265 MoS_2 -based pouch cell with a high sulfur loading of 9 g at 400 mA.

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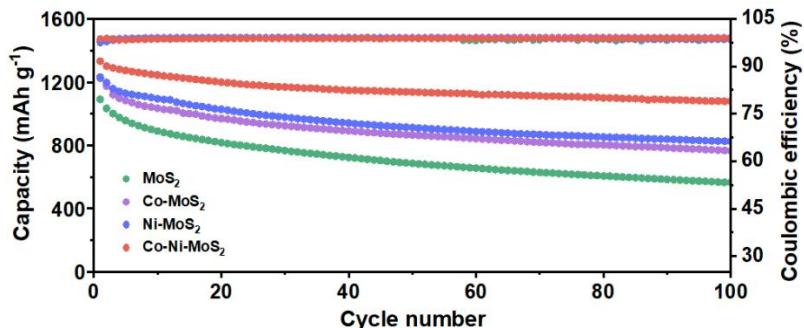
269

270 **Supplementary Fig. 40 |** XRD patterns of the catalysts doped with only Co or Ni.

271

272 In order to verify the advantage of Co,Ni-MoS₂ over MoS₂ doped with only Co or Ni,
 273 a series of experiments was performed. The materials were synthesized using the
 274 same methods as for Co,Ni-MoS₂, and XRD patterns were obtained. All the patterns
 275 agree with the data for MoS₂ (JCPDS card no. 37-1492).

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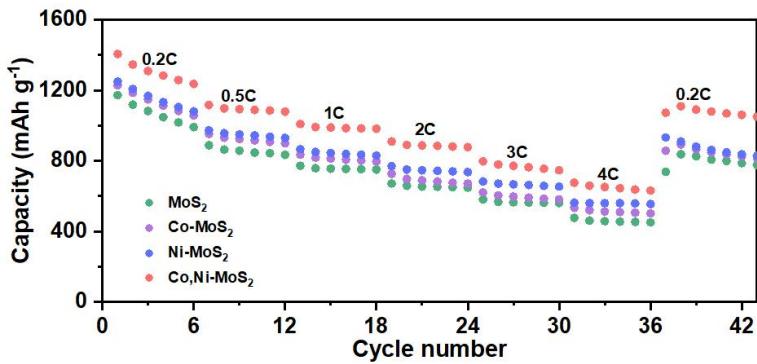
279 **Supplementary Fig. 41** | Cycling performances of cells with the MoS₂, Co-MoS₂,
280 Ni-MoS₂, and Co,Ni-MoS₂ catalysts at 0.3 C during the 100 cycles.

281

282 The electrochemical performance of the batteries using Co or Ni, or Co,Ni-MoS₂
283 catalysts has been thoroughly assessed. Subsequent cycling tests were conducted to
284 evaluate the durability of the batteries. After 100 cycles at 0.3 C, the cells with Co or
285 Ni doped MoS₂ retained a higher reversible discharge capacity than that with pure
286 MoS₂. However, the Co,Ni-MoS₂-based cells had a much better performance,
287 maintaining a capacity of 1077.5 mAh g⁻¹ after 100 cycles. This clear contrast
288 underscores the substantial performance improvements produced by the higher SRR
289 catalytic activity.

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294 **Supplementary Fig. 42** | Rate performance of MoS₂, Co-MoS₂, Ni-MoS₂, and
295 Co,Ni-MoS₂ based-cells from 0.2 C to 4 C.

296

297 The rate performance of Li-S batteries using the different catalysts was tested at rates
298 ranging from 0.2 C to 4 C and then back to 0.5 C. The Co,Ni-MoS₂-based cell had
299 distinct charge and discharge plateaus, even at a high current rate of 4 C, and had
300 outstanding reversible capacities of 1235, 982, and 631 mAh g⁻¹ at 0.2 C, 1 C, and 4 C,
301 respectively. In contrast, due to their lower catalytic efficiency, Co-MoS₂, Ni-MoS₂,
302 and pure MoS₂-based cells had significantly lower capacities, particularly under
303 high-rate conditions. These results are ascribed to differences in catalytic efficiency
304 introduced by the incorporation of different metal cation pairs into MoS₂.

305

306 **Supplementary Table 1** | The parameters considered in this study.

307

Number	Component features
1	Spin moment
2	Adsorption Li ₂ S
3	Adsorption Li ₂ S ₂
4	Distance between metals
5	M1S min distance
6	M1S max distance
7	M1S avg distance
8	M2S min distance
9	M2S max distance
10	M2S avg distance
11	M1 covalent radius
12	M2 covalent radius
13	M1 atomic mass
14	M2 atomic mass
15	M1 melting point
16	M2 melting point
17	M1 ionization energy
18	M2 ionization energy
19	M1 valence electrons
20	M2 valence electrons
21	P band center
22	D band center
23	M1 D band center
24	M2 D band center
25	Mo D band center
26	M1 electronegativity
27	M2 electronegativity
28	Electronegativity of Mo in the active center
29	Electronegativity of S in the active center

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309

310 **Supplementary Table 2** | Metal contents in the MoS₂ host determined by ICP-MS
 311 analysis.

Samples	n _M :n _{Mo} (~at%)
Co,Ni-MoS ₂	n _{Co} :n _{Mo} (4/100), n _{Ni} :n _{Mo} (4/100)
Co,Mn-MoS ₂	n _{Co} :n _{Mo} (4/100), n _{Mn} :n _{Mo} (4/100)
Co,Ni-MoS ₂	n _{Co} :n _{Mo} (4/100), n _V :n _{Mo} (4/100)

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 315
 316 **Supplementary Table 3** | Structural parameters and atomic positions of MoS₂ from
 317 Rietveld refinement.

Atom	Site	x	y	z
Mo	2c	0.33333	0.66667	0.25000
S	4f	0.33333	0.66667	0.62719

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 322 **Supplementary Table 4** | Structural parameters and atomic positions of Co_xV-MoS₂
 323 from Rietveld refinement.

Atom	Site	x	y	z
Mo	2c	0.33333	0.66667	0.25000
S	4f	0.33333	0.66667	0.62162
Co	2c	0.33333	0.66667	0.25000
V	2c	0.33333	0.66667	0.25000

325
 326
 327
 328 **Supplementary Table 5** | Structural parameters and atomic positions of Co_xMn-MoS₂
 329 from Rietveld refinement.

Atom	Site	x	y	z
Mo	2c	0.33333	0.66667	0.25000
S	4f	0.33333	0.66667	0.62388
Co	2c	0.33333	0.66667	0.25000
Mn	2c	0.33333	0.66667	0.25000

333 **Supplementary Table 6** | Structural parameters and atomic positions of Co_xNi-MoS₂
334 from Rietveld refinement.

335

Atom	Site	x	y	z
Mo	2c	0.33333	0.66667	0.25000
S	4f	0.33333	0.66667	0.62393
Co	2c	0.33333	0.66667	0.25000
Ni	2c	0.33333	0.66667	0.25000

336

337

338 **Supplementary Table 7** | Structural parameters extracted from the M K-edge EXAFS
339 fitting.

340

Samples	Path	R (Å)	σ^2 (10 ⁻³ Å ²)	ΔE_0 (eV)	R-factor
Co _x Ni-MoS ₂	Co-S	2.22 ± 0.02	4.7	-9.73	0.006
Co _x Ni-MoS ₂	Ni-S	2.23 ± 0.01	8.2	-9.7	0.016
Co _x Mn-MoS ₂	Co-S	2.23 ± 0.05	4.9	-6.63	0.015
Co _x Mn-MoS ₂	Mn-S	2.26 ± 0.03	1.0	-6.24	0.014
Co _x V-MoS ₂	Co-S	2.22 ± 0.01	1.4	-9.9	0.009
Co _x V-MoS ₂	V-S	2.27 ± 0.07	5.6	-9.7	0.018

341

342

343 **Supplementary Table 8** | The value of each parameter of the Ah level Li-S pouch
344 cell.

345

Parameters	Value
Length (mm)	72
Width (mm)	113
Number of cathodes	18
Sulfur mass (g)	10.2
E/S ratio ($\mu\text{l mg}^{-1}$)	3.2
Thickness of separator (μm)	9
Thickness of lithium anode (μm)	100
Total weight of battery (g)	67
Current density (mA)	1000
Capacity (Ah)	13.2
Energy density (Wh kg^{-1})	435

346

347

348 **Supplementary Table 9** | Comparison of the electrochemical performances of various
349 catalyst-based pouch cells between this work and other reported studies.

350

Areal S loading, mg cm ⁻²	E/S ratio, μl mg ⁻¹	Total capacity, Ah	Specific energy density Wh kg ⁻¹	Ref
9	3.2	13.2	435	This work
6.1	3.0	1.6	300	R ^[1]
NA	NA	1.17	313	R ^[2]
6	4	1.51	317	R ^[3]
12	5	2.5	330	R ^[4]
7.0	3.0	1.5	343	R ^[5]
6.0	2.3	6.2	351	R ^[6]
7.3	3.5 (g g _s ⁻¹)	2	353	R ^[7]
6.5	3.0	1.8	359	R ^[8]
10	1.2	NA	366	R ^[9]
17.3	4	1.82	402	R ^[10]
10	2.6	10	417	R ^[11]

351

352

353 **Supplementary Note 1: Interpretable Multi-View Machine-Learned Framework**

354 **Data Collection**

355 In this study, data collection was carried out based on first-principles calculations.

356 The two atom doping configurations of MoS₂ are illustrated in Supplementary Fig. 1.

357 Using density functional theory (DFT), we calculated the energy barriers of the

358 rate-determining step (ΔG) for the Li₂S₂-to-Li₂S conversion on various dual-doped

359 MoS₂ surfaces.

360 **Parameter Selection**

361 To ensure effective model construction and enable interpretable insights into

362 underlying chemical principles, we established three core criteria for feature selection:

363 (1) features must be closely related to the catalytic performance of the material to

364 ensure clear physical meaning; (2) features should accurately represent the geometric

365 structure of the material; and (3) features should be easily obtainable and reproducible,

366 facilitating data extension and model transferability.

367 Building upon previous research, we further expanded the feature space. Previous

368 studies have demonstrated a strong correlation between adsorption energy and

369 catalytic activity; thus, the adsorption energies of Li₂S₂ and Li₂S on catalyst surfaces

370 were included as key features. According to the Sabatier principle, the electronic

371 structure of active catalytic sites plays a pivotal role in determining catalytic behavior.

372 Therefore, we incorporated several electronic descriptors, including spin density, the

373 d-band center of transition metals, the p-band center of non-transition metals, and the

374 charge transfer induced by doping.

375 In addition, various fundamental physicochemical properties potentially affecting

376 catalytic performance were considered, such as the first ionization energy of the metal
377 atoms and the Pauling electronegativity of active-site elements (including both metals
378 and non-metals). To more comprehensively capture the structural characteristics of the
379 materials, geometric and electronic structure parameters such as bond lengths, charge
380 distributions, and d-band centers corresponding to different doping elements were
381 also included.

382 We also augmented the feature set with elemental properties sourced from the
383 Mendeleev database, incorporating descriptors such as atomic mass, valence electron
384 count, and melting point. These physicochemical features were used to construct
385 machine learning models targeting the reaction free energy change (ΔG), with the aim
386 of uncovering the key factors influencing catalytic performance. Details and
387 definitions of the elemental property data can be found at:
388 <https://mendeleev.readthedocs.io/en/stable/data.html>.

389 **Selection of Machine Learning Methods**

390 In this study, multiple machine learning algorithms were employed to analyze and
391 predict target features, including Random Forest Regressor, Least Absolute Shrinkage
392 and Selection Operator (LASSO) regression, Ridge Regression, and eXtreme
393 Gradient Boosting (XGBoost) Regressor. By comparing the predictive performance of
394 these models, the objective was to identify the most suitable algorithm for the specific
395 tasks of this research.

396 To increase the robustness of model evaluation, the Leave-One-Out
397 Cross-Validation approach was adopted. In each iteration of this method, a single data

398 point was held out as the validation set while the remaining samples were used for
399 training. This process was repeated until every sample has served once as the
400 validation set. This validation strategy effectively reduces model bias and improves
401 generalization performance.

402 **Hyperparameter Optimization of Regression Models**

403 To improve the regression models, a hybrid strategy combining automated search
404 and manual tuning was employed for hyperparameter optimization. Initially, potential
405 optimal hyperparameter combinations were identified using automated techniques
406 such as Grid Search. Subsequently, fine-tuning was performed manually based on
407 model performance on the validation set, aiming to improve both generalization
408 ability and predictive accuracy.

409 Specifically, for the Random Forest Regressor, key parameters such as the number
410 of data and the maximum data depth were optimized. For the LASSO Regressor, a
411 systematic exploration of different regularization strengths (α) was conducted to
412 determine the most appropriate level of sparsity. Similarly, for the Ridge Regressor,
413 the regularization parameter (α) was optimized through a combination of automated
414 and manual tuning to achieve a balanced performance across both training and
415 validation datasets. For the XGBoost Regressor, a joint optimization of critical
416 parameters such as the number of estimators, maximum depth, and learning rate was
417 carried out to maximize predictive accuracy.

418 During each round of cross-validation, model performance was quantitatively
419 assessed by recording the Mean Squared Error (MSE) and the Coefficient of

420 Determination (R^2). These metrics were used to compare and evaluate the
421 effectiveness of each regression model.

$$R^2 = 1 - \frac{\sum_i (Y_i - y_i)^2}{\sum_i (Y_i - \bar{Y})^2}$$

422

$$MSE = \frac{1}{N} \sum_i^n (Y_i - y_i)^2$$

423 Y_i represents the true values obtained from DFT calculations, while y_i denotes the
424 predictions made by the machine learning models, and \bar{Y} is the mean value of the
425 DFT data. An ideal model should have an R^2 value close to 1 and an MSE value close
426 to 0. Ultimately, the hyperparameter combination that performs best on the validation
427 set is selected as the final configuration for each model. The performance of the
428 different models across various metrics is shown in Supplementary Fig. 13.

429 **Feature Importance Analysis**

430 The SHapley Additive exPlanations (SHAP) method, proposed by Lundberg and Lee

431 in 2017, is based on the Shapley values from cooperative game theory and is designed
432 to provide interpretable explanations for model predictions. In this study, we used
433 SHAP to perform a posteriori quantitative assessment of feature importance, aiming
434 to estimate the contribution of each input feature to the model’s predictive outcomes.

435 For each individual data point, SHAP perturbs the input features and computes their
436 marginal contributions to the prediction, resulting in a corresponding “importance
437 value.” By aggregating SHAP values across all samples and calculating the mean, we
438 can further evaluate the global importance of each feature within the entire dataset.

439 This dual capability enables SHAP to offer both local interpretability (explaining
440 individual predictions) and global interpretability (assessing feature impact across the
441 entire model), making it a powerful and widely applicable tool. Features with higher
442 importance exhibit larger SHAP values, while less influential features tend to have
443 smaller or near-zero SHAP values.

444 As a model-agnostic interpretation framework, SHAP can be applied to various
445 machine learning models, allowing for a transparent visualization and understanding
446 of how input features influence the model's decision-making process. In this work, we
447 used SHAP to analyze six key features in our model, thereby identifying the variables
448 with the most significant impact on prediction outcomes.

449 The SHAP value for a feature was computed using the following formula:

$$450 \quad \Phi_i = \sum_{S \subseteq F, \{i\}} \frac{|S|!(|F| - |S| - 1)!}{|F|!} [f_{S \cup \{i\}}(x_{S \cup \{i\}}) - f_S(x_S)]$$

451 Φ_i denotes the SHAP value of feature i , S is a subset of the full feature set F , x_S
452 represents the input values corresponding to subset S , and f_S is the output function of
453 the trained model. By evaluating the change in model output when feature i is added
454 to subset S , the marginal contribution of feature i can be quantitatively determined.

455
456

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