

# Dual-Scale Controls of Vertical Eddy Diffusivity in Tropical Cyclone Rapid Intensification Forecasts

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## Article

**Keywords:** Tropical Cyclone, rapid intensification, planetary boundary layer scheme, vertical eddy diffusivity, turbulent and mixing process

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**Additional Declarations:** There is **NO** Competing Interest.

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## ABSTRACT

The escalating threat of rapidly intensifying Tropical Cyclones (TCs) to global coastal communities underscores the urgent need to advance TC intensity forecasting. While planetary boundary layer (PBL) processes regulate energy sources and sink essential for TC development, improving vertical eddy diffusivity ( $K_m$ ) parameterization has long been constrained by semi-empirical approaches. Within an unstructured mesh global model framework, we demonstrate that TC rapid intensification (RI) is fundamentally governed by two scaling parameters of  $K_m$ : vertical extent ( $h$ ) and peak magnitude ( $\alpha$ ), which are optimized through validation against previous observations. Mechanistically,  $h$  modulates vortex spin-up efficiency by controlling vertical diffusion and low-level moisture flux gradient, whereas  $\alpha$  regulates boundary layer gradient imbalance during RI stage through downward mixing of tangential momentum. Implementation of the optimized  $K_m$  parameterization reduces maximum wind speed forecasting error by 58.7% (or  $4.5 \text{ m s}^{-1}$ ) averaged over 72-hour leading time, attributing to the enhanced RI forecasting capability. These findings establish the first unified paradigm linking turbulent processes to RI physics, offering transformative potential for refining TC modeling.

**Key Words:** Tropical Cyclone, rapid intensification, planetary boundary layer scheme, vertical eddy diffusivity, turbulent and mixing process

## 57 1. Introduction

58 Tropical cyclone (TC) intensity forecasting has lagged behind advances in track prediction  
59 in recent decades (DeMaria et al. 2014; Cangialosi et al. 2020). Rapid intensification (RI)  
60 occurs when a TC intensifies dramatically over a short period, posing its forecasting challenges  
61 due to the unpredictable onset and duration (Emanuel 2017; Emanuel and Zhang 2017). This  
62 forecasting gap becomes increasingly critical as observational evidence reveals both  
63 accelerated intensification rates of major TCs (Bhatia et al. 2019; Song et al. 2020) and a rising  
64 global RI frequency (Zhao et al. 2018; Liu and Chan 2022). Notably, near-coastal RI  
65 occurrences have tripled from 1980 to 2020 and may continue to increase under a future  
66 warming climate (Li et al. 2023), underscoring an urgent need for improving RI prediction.

67 The Planetary Boundary layer (PBL) mediates energy exchanges critical for TC  
68 intensification, facilitating upward heat and moisture fluxes from the ocean surface while  
69 transferring momentum downward through turbulent mixing (Ooyama 1969; Emanuel 1986;  
70 Smith and Montgomery 2010). However, these subgrid-scale processes remain inadequately  
71 constrained in the vertical eddy diffusivity parameterization within the PBL scheme. As the  
72 PBL is conventionally divided into the surface layer and the overlying mixed layer, efforts have  
73 been devoted to improving the parameterization of surface fluxes in the surface layer scheme  
74 (Powell et al. 2003; Montgomery et al. 2010). In contrast, determining the turbulent momentum  
75 and enthalpy fluxes in the mixed layer proves more challenging due to the presence of roll-like  
76 vortex structures (Lorsolo et al. 2008). Moreover, turbulence in TC conditions exhibits distinct  
77 characteristics from typical convective boundary layer, attributing to the influence of extreme  
78 winds and strong inertial stability (Eliassen 1971; Kepert 2001).

79 Recent progresses in eddy diffusivity parameterization for TC modeling originate from  
80 National Oceanic and Atmospheric Administration (NOAA) WP-3D aircraft observations  
81 during TC inner-core penetrations. Pioneering work by Zhang et al. (2011) first quantified the  
82 vertical momentum flux and corresponding vertical eddy diffusivity for momentum ( $K_m$ ) in the  
83 inflow layers of intense hurricanes Hugo (1989) and Allen (1980). Their findings revealed a  
84 positive correlation between  $K_m$  and wind speed at 450-m altitude. Subsequent analyses by  
85 Zhang and Drennan (2012) extended these observations to four intense hurricanes, providing  
86 the first estimates of the vertical distribution of eddy diffusivities. These findings informed

87 improvements in the  $K_m$  formulation to the nonlocal K-profile parametrization (KPP) scheme  
88 by introducing an empirical parameter  $\alpha$  into the original form of  $K_m$  (O'Brien 1970).

$$89 \quad K_m = ku_*z \left[ \alpha \left( 1 - \frac{z}{h} \right)^2 \right], \quad (1)$$

90 where  $k = 0.4$ ,  $u_*$  is the velocity scale,  $z$  is the departure from the surface,  $h$  is the  
91 diagnosed PBL height, and  $\alpha$  is the parameter to control the magnitude of  $K_m$ . Operational  
92 implementation in the operational Hurricane Weather Research and Forecasting (HWRF) model  
93 demonstrated that reducing  $K_m$  by setting  $\alpha = 0.25-0.5$  yields the best match with the  
94 observations (Gopalakrishnan et al. 2013; Tallapragada et al. 2014). This reduced  $K_m$  results  
95 in a shallower PBL and more intense radial inflow (Gopalakrishnan et al. 2013;  
96 Gopalakrishnan et al. 2021), leading to improvements in TC boundary layer structure (Zhang  
97 et al. 2015) and intensity forecasts (Zhang et al. 2017), particularly for RI events (Zhang and  
98 Rogers 2019). Nevertheless, since the TC vortex may amplify small changes in the boundary  
99 layer through nonlinear feedback processes, the extent to which  $K_m$  parametrization advances  
100 fully explain TC simulation improvements remains unclear.

101 In addition, the parameterized  $K_m$  exhibits strong dependence on the diagnosed PBL  
102 height  $h$  (Eq. 1), which varies substantially with definition criteria. Analysis of 794 GPS  
103 dropsonde profiles within 13 hurricane core regions reveals that the well-mixed layer depth  
104 approximates half the inflow layer depth, while Richardson-number-based definitions yield  
105 intermediate PBL heights (Zhang et al., 2011). This PBL height sensitivity critically impacts  
106 TC forecasts through its influence on the vertical structure of  $K_m$ , inflow layer depth, inflow  
107 strength, and thereby TC intensity (Kepert 2012). Given that the magnitude parameter ( $\alpha$ ) and  
108 the PBL height scale ( $h$ ) contribute differently to the parameterized  $K_m$  (Eq. 1), their  
109 fundamental roles in TC intensification require clarification.

110 Here we aim to optimize the scaling parameters  $\alpha$  and  $h$  in the  $K_m$  parameterization  
111 for TC modeling, ensuring optimal consistency with observational benchmarks from Zhang et  
112 al. (2011) and Zhang and Drennan (2012). We will further demonstrate, for the first time to our  
113 knowledge, that the dual-scale impacts of  $K_m$  on RI are essential but mechanistically distinct,  
114 with physical explanations on how parameterized turbulent fluxes govern fundamental RI  
115 physics. Finally, we show the implementation potential of the optimized  $K_m$  for improving RI

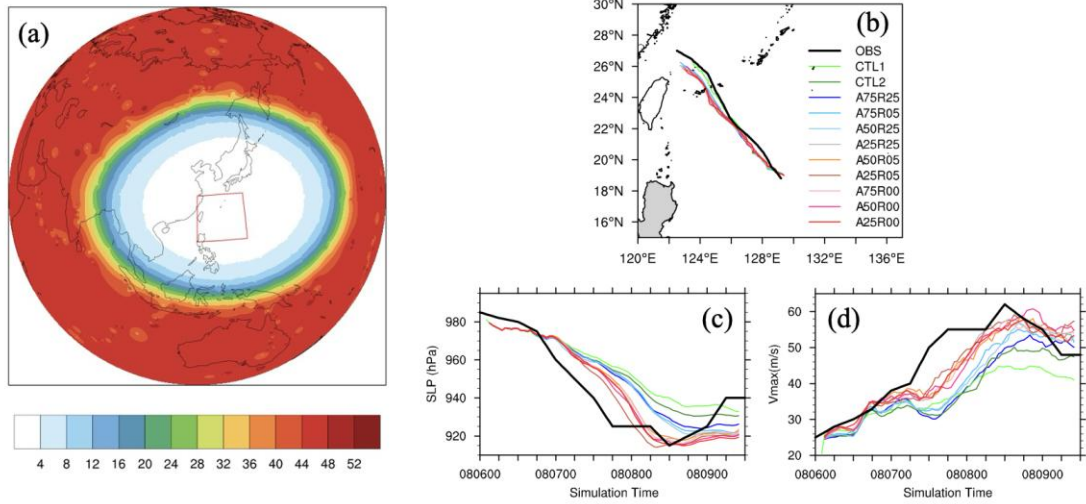
116 forecasting. The rest of this paper is organized as follows. Section 2 details model configuration  
117 and  $K_m$  optimization. Section 3 describes the dual-scale controls on RI and the related physical  
118 mechanisms. The results and discussions are summarized in section 4.

## 119 **2. Methods**

### 120 *a. Model setup*

121 The Global-to-Regional Integrated Forecast System (GRIST), an unstructured mesh global  
122 model (Zhang et al. 2019, 2020, 2021, 2022; Li et al. 2022, 2023) was originally developed  
123 with the purpose to investigate the unified global weather and climate modeling, with flexibly  
124 resolution adjustment and multi-physics package configurations. Recently, the GRIST  
125 mesoscale weather-climate prediction configuration (GRIST-MWP) has been employed to  
126 conduct high-resolution storm-resolving simulations with a global uniform resolution of 3–5  
127 km (Zhang et al. 2022; Huang et al. 2025).

128 Following our recent research (Huang et al. 2025), we adopt the GRIST-MWP with a  
129 variable resolution grid ranging from 4 to 50 km. Figure 1a shows that the finest resolution of  
130 4 km covers most of the western North Pacific and South China Sea, and eastern China, with a  
131 rapid transition to 50-km resolution for the rest global domain. Each grid has 31 vertical levels  
132 with 5 within the lowest 1.0 km of the model atmosphere. We have utilized the dataset from the  
133 National Center for Environmental Prediction Global Forecast System (GFS), which features a  
134 resolution of 0.5 degrees. The daily SST is updated from the GFS data. The parameterization  
135 schemes used in the control run (CTL1) include the eddy-diffusivity mass-flux (EDMF; Han et  
136 al. 2016) PBL scheme, the new version of the rapid radiative transfer model for longwave and  
137 shortwave radiation schemes (Iacono et al. 2008), the Tiedkle-Bechtold convective scheme  
138 (Bechtold et al. 2008, 2014), Xu-Randall cloud-fraction parameterization (Xu and Randall  
139 1996), and the single-moment 6-class microphysics scheme (Hong et al. 2006).



140

141 Fig.1. (a) The variable resolution grid adopted in GRIST model, with shading denoting the  
 142 horizontal resolution ranging from 4 to 50 km. Simulation results within the red box are shown  
 143 for (b) tracks, (c) minimum sea level pressure (hPa), and (d) 10-m maximum wind speed ( $\text{m s}^{-1}$ )  
 144 of Super Typhoon Lekima (2019). The black lines in (b-d) represent the best-track data from  
 145 China Meteorological Administration, while colored lines are simulation results from numerical  
 146 experiments as will be described in Table 1.

147 *b. Modifications in EDMF scheme under TC conditions*

148 Two modifications are introduced to the original version of EDMF scheme. Considering  
 149 the effect of in-cloud mixing above the PBL in improving TC structure and track simulation,  
 150 the eddy diffusivity ( $K_m$ ) in the free atmosphere is modified according to our research (Huang  
 151 et al. 2025). In the original EDMF scheme, the local diffusion scheme (Louis 1979) is utilized  
 152 for free atmospheric diffusion above the PBL ( $z > h$ ). The eddy diffusivity  $K_m$  for momentum  
 153 and mass above the PBL is defined as:

154 
$$K_m = l^2 f_{m,t}(Rig) \left( \frac{\partial U}{\partial z} \right) \quad (2)$$

155 where  $l$  is the mixing length, the stability functions  $f_{m,t}(Rig)$  are represented by the local  
 156 gradient Richardson number  $Rig$ , and  $\frac{\partial U}{\partial z}$  represents the vertical wind shear.

157 For the noncloudy layer,

158 
$$Rig = \frac{g}{\theta_v} \left[ \frac{\partial \theta_v / \partial z}{(\partial U / \partial z)^2} \right] \quad (3)$$

159 To include the effect of in-cloud mixing, for the cloudy air,  $Rig$  is modified for reduced  
 160 stability within cloudy air (Durran and Klemp 1982),

$$161 \quad Rig_c = \left(1 + \frac{L_v q_v}{R_d T}\right) \left[ Rig - \frac{g^2}{(\partial U / \partial z)^2} \frac{1}{c_p T} \frac{(L_v^2 q_v / c_p R_v T^2 - L_v q_v / R_d T)}{(1 + L_v^2 q_v / c_p R_v T^2)} \right] \quad (4)$$

162 For cloudy air,  $Rig$  in Eq. 3 is replaced by  $Rig_c$  in Eq. 4 in computing Eq. 2. This  
 163 modification of local gradient Richardson number considers the effects of clouds on turbulent  
 164 mixing through enhancing the diffusivity coefficient.

165 Additionally, the diagnosed boundary layer height in the original EDMF scheme is defined by  
 166 the bulk stability between the surface layer and levels above. The bulk Richardson number ( $Rib$ )  
 167 between the surface layer and a level  $z$  is defined as:

$$168 \quad Rib = \frac{g[\theta_v - \theta_s]z}{\theta_{va} U^2} \quad (5)$$

169 where the  $\theta_v$  is the virtual potential temperature, and  $\theta_s$  is the appropriate temperature near the  
 170 surface.  $\theta_{va}$  is the virtual potential temperature at the lowest model level,  $U$  is the horizontal wind  
 171 speed.

172 Given that the definition of PBL height may not work properly in TC conditions (Chen 2022),  
 173 we use a different PBL height definition that works well in all stability conditions, especially  
 174 for TC strong winds (Vogelezang and Holtslag 1996). The Richardson number is calculated  
 175 from the bottom model layer to PBL height  $h$ ,

$$176 \quad Rib = \frac{\frac{g}{\theta_{vs}}(\theta_{vh} - \theta'_{vs})(h - z_s)}{(u_h - u_s)^2 + (v_h - v_s)^2 + 100u_*^2} \quad (6)$$

177 where  $z_s$  is the height of the bottom model level, and  $u_s$  and  $v_s$  denote zonal and meridional  
 178 winds at  $z = z_s$ , respectively. For stable and neutral boundary layers,  $\theta'_{vs} = \theta_{vh}$ , where  $\theta_{vs}$   
 179 is the virtual potential temperature at  $z = z_s$ ; for unstable conditions,  $\theta'_{vs} = \theta_{vs} + \theta_T$  (Troen  
 180 and Mahrt 1986), where  $\theta_T$  is virtual temperature excess near the surface.  $u_*$  denotes surface  
 181 frictional velocity.

### 182 *c. Optimizing the two scaling parameters in $K_m$*

183 The numerical experiments conducted in this study are summarized in Table 1. CTL2 shares  
 184 the same configurations with CTL1, except for the use of the modified EDMF in the TC region  
 185 recognized as the 10-m maximum wind speed no less than  $17.2 \text{ m s}^{-1}$  and sea level pressure  
 186 less than 1000 hPa within the finest domain. CTL2 provides the benchmark for experiments 3–

187 15. Experiments 3–11 are designed with varying parameters  $\alpha$  and  $Rib$  to produce the best match  
 188 of  $K_m$  with the observations. The sensitivity of the simulated TC intensity to parameters  $\alpha$  and  
 189  $Rib$  is further investigated in experiments 12–15.

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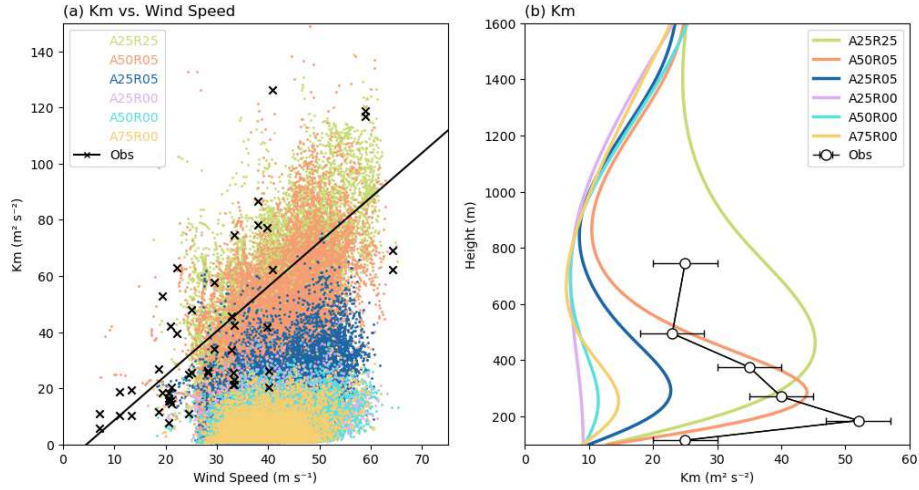
Table 1. Numerical experiments design

No.	Experiment	Description
1	CTL1	Original EDMF PBL scheme
2	CTL2	As in CTL1, but switches to the modified EDMF in TC conditions
3	A75R25	As in CTL2, but for $\alpha=0.75$ , $Rib=0.25$
4	A50R25	As in CTL2, but for $\alpha=0.5$ , $Rib=0.25$
5	A25R25	As in CTL2, but for $\alpha=0.25$ , $Rib=0.25$
6	A75R05	As in CTL2, but for $\alpha=0.75$ , $Rib=0.05$
7	A50R05	As in CTL2, but for $\alpha=0.5$ , $Rib=0.05$
8	A25R05	As in CTL2, but for $\alpha=0.25$ , $Rib=0.05$
9	A75R00	As in CTL2, but for $\alpha=0.75$ , $Rib=0$
10	A50R00	As in CTL2, but for $\alpha=0.5$ , $Rib=0$
11	A25R00	As in CTL2, but for $\alpha=0.25$ , $Rib=0$
12	A50R05-A50R25_12h	As in A50R05, but switches to A50R25 since 12h
13	A50R25-A50R05_12h	As in A50R25, but switches to A50R05 since 12h
14	A50R25-A75R25_24h	As in A50R25, but switches to A75R25 since 24h
15	A75R25-A50R25_24h	As in A75R25, but switches to A50R25 since 24h

191

192 Figures 1b-d present simulation results for experiments 1–11 in track and intensity of Super  
 193 Typhoon Lekima (2019). Lekima originated as a tropical storm at 1200 UTC 4 August in the  
 194 western North Pacific. It subsequently underwent RI, reaching the intensity of a Super Typhoon  
 195 at 1800 UTC 7 August and achieving its maximum wind speed (MWS) of  $62 \text{ m s}^{-1}$  at 1200 UTC  
 196 8 August. This study focuses on the period between 0000 UTC 6 August and 1200 UTC 9  
 197 August. Since the modifications in these experiments are only confined within TC regions, the  
 198 TC environmental circulations are similar. Consequently, the simulated TC tracks almost  
 199 overlap (Fig. 1b). In contrast, the simulated intensities are obviously divergent (Figs. 1c,d).

200 Experiments CTL1, CTL2, A75R25, A75R05, and A50R25, colored in green and blue produce  
 201 weaker intensities (Figs. 1c,d), whereas the intensities for A25R25, A50R05, A25R05, A75R00,  
 202 A50R00, and A25R00 shown in warmer colors are significantly improved.



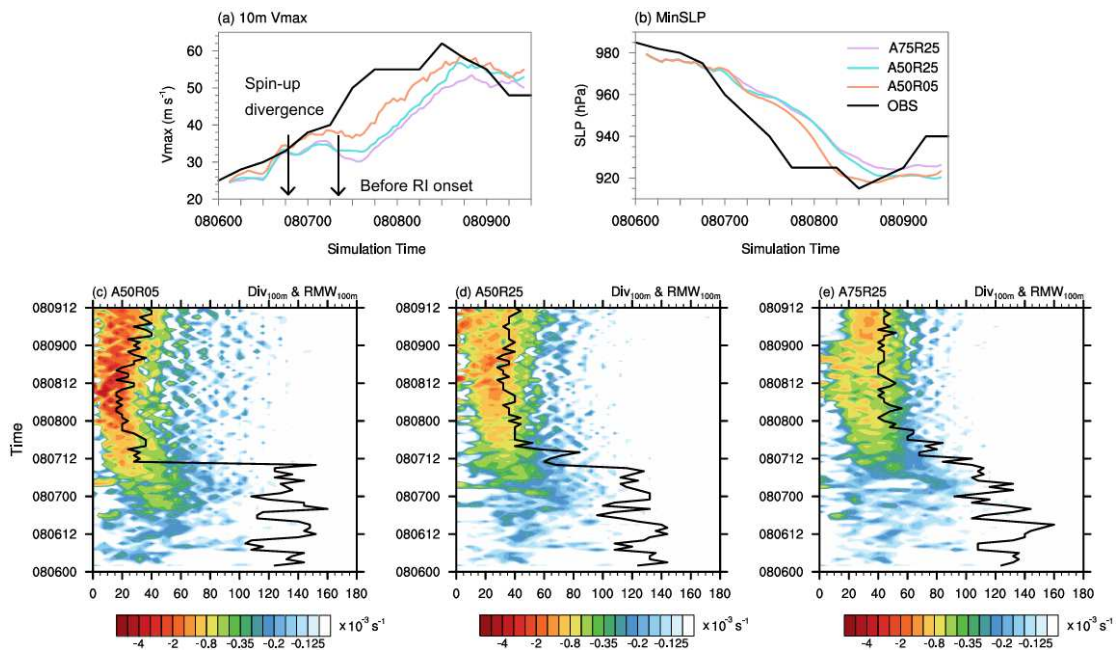
203  
 204 Figure 2. (a) Variations of simulated eddy diffusivity ( $K_m$ ) with wind speed averaged between  
 205 400–500 m heights within the radius of 200 km at 1200 UTC 8 August, compared with  
 206 observations at 450-m altitude (Zhang et al. 2011). (b) Vertical profiles of the simulated  $K_m$   
 207 averaged within 200-km radius compared with observations in Zhang and Drennan (2012).  
 208

209 The  $K_m$  in the six improved simulations is further evaluated and compared with  
 210 observations from Zhang et al. (2011) and Zhang and Drennan (2012). Figures 2a depicts the  
 211 modeled  $K_m$  in relation with wind speed averaged at 400-500 m heights, as compared to flight-  
 212 level (450-m altitude) observations from Hurricanes Hugo and Allen (Zhang et al. 2011). The  
 213 modeled  $K_m$  in A25R05, A25R00, A50R00, and A75R00 is far less diffusive than the  
 214 observation. Figure. 2b compares the vertical profile of the modeled  $K_m$  with estimations in  
 215 Zhang and Drennan (2012). Clearly, A50R05 with  $\alpha=0.5$  and  $Rib=0.05$  yields a reasonable  
 216 shape for the vertical profile of  $K_m$  within the inner-core region, which matches well with the  
 217 observation (Fig. 2b). The increasing trend of the observed  $K_m$  above 500-m height may imply  
 218 the mixing effect above the PBL, which is also captured in A50R05 (Fig. 2b). Therefore, the  
 219 configuration of A50R05 is considered to be the optimized parameterization of  $K_m$  in the  
 220 present study.

### 221 3. Dual-Scale controls of $K_m$ in RI

222 *a. Impacts on TC intensity evolution*

223 To examine how the two scaling parameters  $\alpha$  and  $Rib$  influence TC intensification, we  
 224 compare two pairs of experiments between A50R25 and A50R05, as well as between A75R25  
 225 and A50R25 in simulating Typhoon Lekima. The simulated RI and maximum intensity in the  
 226 optimized configuration of A50R05 is generally closer to the best-track (Figs. 3a,b). In  
 227 comparison, A75R25 and A50R25 produce the weaker intensities during the simulation time.  
 228 A clear divergence in MWS emerges between A50R25 and A50R05 around 2000 UTC 6 August,  
 229 while the intensity evolution remains consistent between A50R25 and A75R25. During this  
 230 vortex spin-up period, TC slowly decays due to the ocean surface friction (including the  
 231 diffusion), but spins up as a result of the boundary layer moistening (Smith et al. 2009). This  
 232 suggests that A50R05 likely experiences either reduced frictional dissipation or enhanced  
 233 moistening in the boundary layer, compared with the other two experiments. As vortex spin-up  
 234 continues, a discrepancy in MWS between A50R25 and A75R25 becomes evident near 0900  
 235 UTC 7 August, just prior to the simulated RI onset. Meanwhile, the radius of maximum wind  
 236 (RMW) in A50R05 contracts rapidly at 1000 UTC 7 August to a stagnant radius of 30 km (Fig.  
 237 3c). In comparison, RMW in either A50R25 or A75R25 moves inward slowly and maintains at  
 238 a larger radius when RI occurs (Figs. 3d,e).

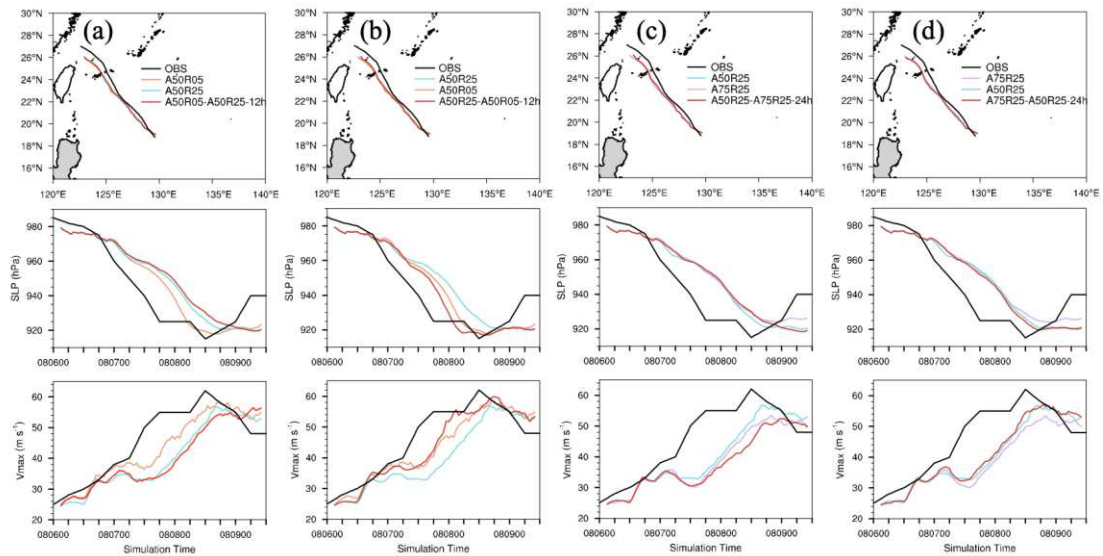


239  
 240 Figure 3. Time evolution of the simulated (a) 10-m maximum wind speed ( $\text{m s}^{-1}$ ) and (b) minimum  
 241 sea level pressure (hPa) for A50R05, A50R25, and A75R25. Radial-time plot of azimuthal-mean

242 low-level horizontal convergence (shading;  $10^{-3} \text{ s}^{-1}$ ) and RMW (contour) at 100-m height for (c)  
 243 A50R05, (d) A50R25, and (e) A75R25.

244

245 To investigate the sensitivity of TC intensification to scaling parameters  $\alpha$  and  $Rib$ ,  
 246 experiments 12–15 are conducted. In experiment 12, we switch  $Rib=0.05$  in A50R05 to  
 247  $Rib=0.25$  at 1200 UTC 6 August (denoted as A50R05-A50R25-12h), approximately 8 hours  
 248 prior to the intensity divergent observed in Fig. 3a. This modification immediately decelerates  
 249 the MWS growth and elevates the surface level pressure, exhibiting intensity trend analogous  
 250 to A50R25 (Fig. 4a). Similarly, reversing  $Rib=0.25$  to  $Rib=0.05$  in A50R25 at 1200 UTC 6  
 251 August (A50R25-A50R05-12h) produces intensity trajectory largely consistent with A50R05,  
 252 despite minor discrepancies during 1800 UTC 7 August and 0600 UTC 8 August (Fig. 4b).  
 253 Besides, simulations with varying parameter  $\alpha$  since 00 UTC 7 August in experiments 14  
 254 (A50R25-A75R25-24h) and 15 (A75R25-A50R25-24h) show comparable intensity evolution  
 255 with A75R25 and A50R25, respectively (Figs. 4c,d). These results consistently show that TC  
 256 intensity changes can be largely explained by changes in parameters  $Rib$  and  $\alpha$ , suggesting  
 257 that the two scaling parameters of  $K_m$  are the main controlling factors in the simulated TC  
 258 intensity, with  $Rib$  governing the vortex spin-up process while  $\alpha$  regulates subsequent RI  
 259 occurrence.



260

261 Figure 4. Simulation results of TC track, minimum sea level pressure (hPa), and 10-m maximum  
 262 wind speed ( $\text{m s}^{-1}$ ) for experiments (a) A50R05-A50R25-12h, (b) A50R25-A50R05-12h, (c)  
 263 A50R25-A75R25-24h, and (d) A75R25-A50R25-24h.

264 *b. Diffusion and moisture flux gradient during vortex spin-up*

265 To explore why the low-Rib (A50R05) and high-Rib (A50R25) experiments produce  
 266 divergence, but low- $\alpha$  (A50R25) and high- $\alpha$  (A75R25) show convergence in intensity  
 267 evolution around 2000 UTC 6 August (Fig. 3a), the roles of the momentum diffusion and  
 268 moisture fluxes due to  $K_m$  are evaluated and compared during the vortex spin-up period.

269 TC spin-up refers to the acceleration of the mean tangential circulation during initial  
 270 intensification. Within an axisymmetric framework, the tangential momentum equation in  
 271 cylindrical coordinates can be expressed as (Montgomery et al. 2020):

$$272 \quad \frac{\partial \bar{v}}{\partial t} = -\bar{u}\bar{\xi}_a - \bar{w}\frac{\partial \bar{v}}{\partial z} - \overline{u'\xi'_a} - \overline{w'\frac{\partial v'}{\partial z}} + \bar{F}_\lambda, \quad (7)$$

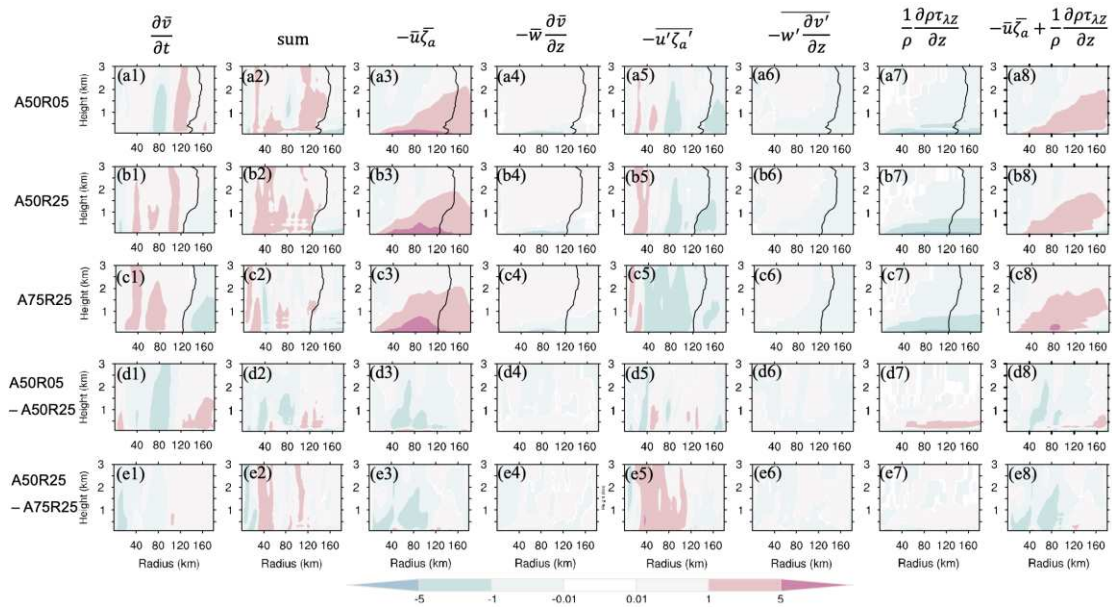
$$273 \quad F_\lambda = \frac{1}{r^2\rho}\frac{\partial r^2\rho\tau_{r\lambda}}{\partial z} + \frac{1}{\rho}\frac{\partial \rho\tau_{\lambda z}}{\partial z}, \quad (8)$$

$$274 \quad \tau_{\lambda z} = K_m \left( \frac{1}{r}\frac{\partial w}{\partial \lambda} + \frac{\partial v}{\partial z} \right), \quad (9)$$

275 where  $u$ ,  $v$ , and  $w$  are radial, tangential, and vertical motion;  $(r, \lambda, z)$  represents the  
 276 cylindrical coordinates;  $\xi_a$  is absolute vertical vorticity;  $\rho$  is the air density;  $F_\lambda$  is  
 277 represented by horizontal and vertical diffusive tendency of tangential momentum as shown in  
 278 Eq. 8. The overbar denotes the azimuthal mean, and the prime means the deviation from the  
 279 azimuthal mean. The horizontal diffusion term is ignored because of its much smaller value  
 280 than other terms. The stress tensor  $\tau_{\lambda z}$  in Eq. 8 is expressed as the function of  $K_m$  as shown  
 281 in Eq. 9.

282 Figure 5 shows tangential wind tendency and its budget terms integrated from every 10-min  
 283 output during 2000–2200 UTC 6 August. The budget-derived tendency patterns (Figs.  
 284 5a2,b2,c2) are basically consistent with direct model outputs (Figs. 5a1,b1,c1), showing  
 285 positive tendencies in the lower troposphere inside the RMW. The mean radial advection term  
 286 (Figs. 5a3,b3,c3) dominates the budget, contributing largely to the positive tangential wind  
 287 tendencies (Figs. 5a1,b1,c1). The diffusion (Figs.5a7,b7,c7) and eddy radial advection  
 288 (Figs.5a5,b5,c5) terms are negative in the boundary layer and lower troposphere, respectively.

289 In contrast to high-Rib experiment A50R25 (Fig. 5b7), the negative contribution of vertical  
 290 diffusion in A50R05 (Fig. 5a7) becomes weaker below the height of 1 km (Fig. 5d7). This  
 291 weaker diffusion, together with the weaker eddy radial advection (Fig. 5d5) facilitates the  
 292 positive value in the budget difference (Fig. 5d2), and thus can explain the faster tangential  
 293 wind acceleration outside the radius of 100 km in the low-Rib experiment (Fig. 5d1).  
 294 Comparing between the low- $\alpha$  (A50R25) and high- $\alpha$  (A75R25) experiments, the vertical  
 295 diffusion terms are nearly identical (Fig. 5e7) at the beginning of spin-up period, when the  
 296 horizontal wind is relative weak (30–40 m s<sup>-1</sup>). This results in a comparable budget around the  
 297 RMW (Fig. 5e2) and therefore an equal tangential wind tendency (Fig. 5e1).

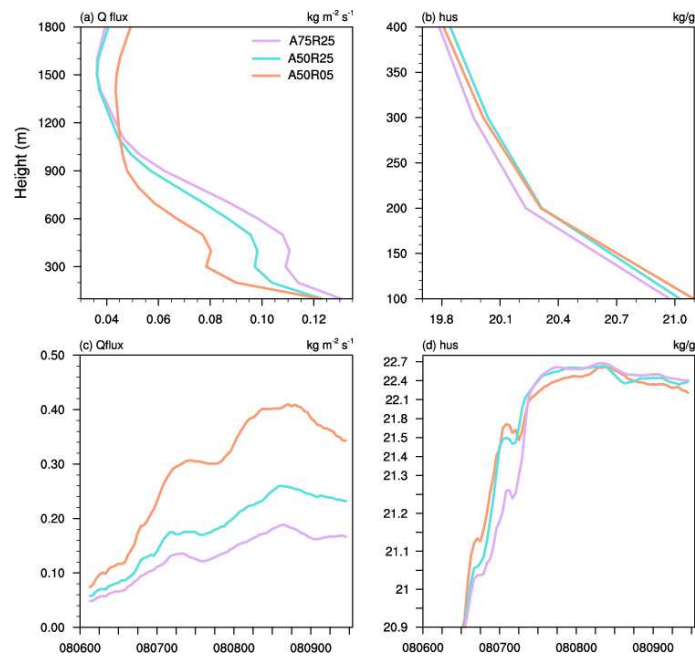


298  
 299 Fig. 5. (a1) Hourly change in the azimuthal-mean tangential wind (shaded; m s<sup>-1</sup> h<sup>-1</sup>) and (a2)  
 300 the sum of the tangential wind budget (shaded; m s<sup>-1</sup> h<sup>-1</sup>) averaged over 2000–2200 UTC 6  
 301 August for A50R05. The individual budget terms (shaded; m s<sup>-1</sup> h<sup>-1</sup>) are (a3) mean radial  
 302 advection, (a4) mean vertical advection, (a5) eddy radial advection, (a6) eddy vertical advection,  
 303 and (a7) vertical diffusion. (a8) sum of mean radial advection and vertical diffusion. (b1–b8)  
 304 and (c1–c8) As in (a1–a8), but for A50R25 and A75R25. (d1–d8) and (e1–e8) are differences  
 305 between (a1–a8) and (b1–b8), and (b1–b8) and (c1–c8), respectively. Black contour shows the  
 306 location of RMW.

307

308 Consistent with the  $K_m$  profile (Fig. 2b), the subgrid-scale moisture flux in A50R05 is  
 309 generally weaker within the boundary layer and decreases more rapidly in the lower 300-m

310 altitude (Fig. 6a). This rapidly weakening of moisture flux implies that less moisture is transferred  
 311 upward to higher layers and thus more is left within the bottom of the boundary layer.  
 312 Consequently, the moistening tendency generated by PBL scheme is more pronounced within  
 313 the lower 300-m height in A50R05 (Figure not shown), contributing to a moister inner-core  
 314 environment within the lower boundary layer in low-*Rib* experiment (Fig. 6b). Time evolution  
 315 of low-level moisture flux gradient between 100–200 m heights and specific humidity at 100-  
 316 m height averaged within 200-km radius are shown in Figs. 6c,d. Notably, the subgrid moisture  
 317 flux gradient is more evident in A50R05 (Fig. 6c). As the gradient strengthens since 1200 UTC  
 318 6 August and peaks around 0600 UTC 7 August (Fig. 6c), the low-level specific humidity  
 319 increases more dramatically than in A50R25 and A75R25 (Fig. 6d). This is consistent with the  
 320 MWS evolution as shown in Fig. 2a, highlighting the linkage between near-surface humidity  
 321 and TC intensity during vortex spin-up stage.



322  
 323 Figure 6. Vertical profile of azimuthal-mean (a) subgrid-scale moisture flux ( $\text{kg m}^{-2} \text{s}^{-1}$ ), and  
 324 (b) specific humidity ( $10^3 \text{ kg kg}^{-1}$ ) at 2000 UTC 6 August within 200-km radius from TC center  
 325 for A50R05, A50R25, and A75R25. Time evolution of (c) moisture flux gradient within the lower  
 326 200 m levels and (d) 200-m height specific humidity averaged within the radius of 200 km for  
 327 A50R05, A50R25, and A75R25.

328

329 Considering the above, the reduced vertical extent of eddy diffusivity contributes to the  
330 suppressed momentum diffusion and enhanced moisture flux gradient. This, in turn, results in  
331 the stronger tangential wind tendency and moister near-surface environment. This scenario  
332 meets the assumption of the evaporation-wind intensification mechanism, known as wind-  
333 induced surface heat exchange (WISHE). WISHE proposes a positive feedback between the  
334 increase of the near-surface mixing ratio in the core region, an enhanced radial gradient of  
335 equivalent potential temperature throughout the boundary layer, and the axisymmetric  
336 tangential wind acceleration (Emanuel 1986, 2003; Montgomery and Smith 2014).

337 *c. Boundary layer imbalance during RI onset*

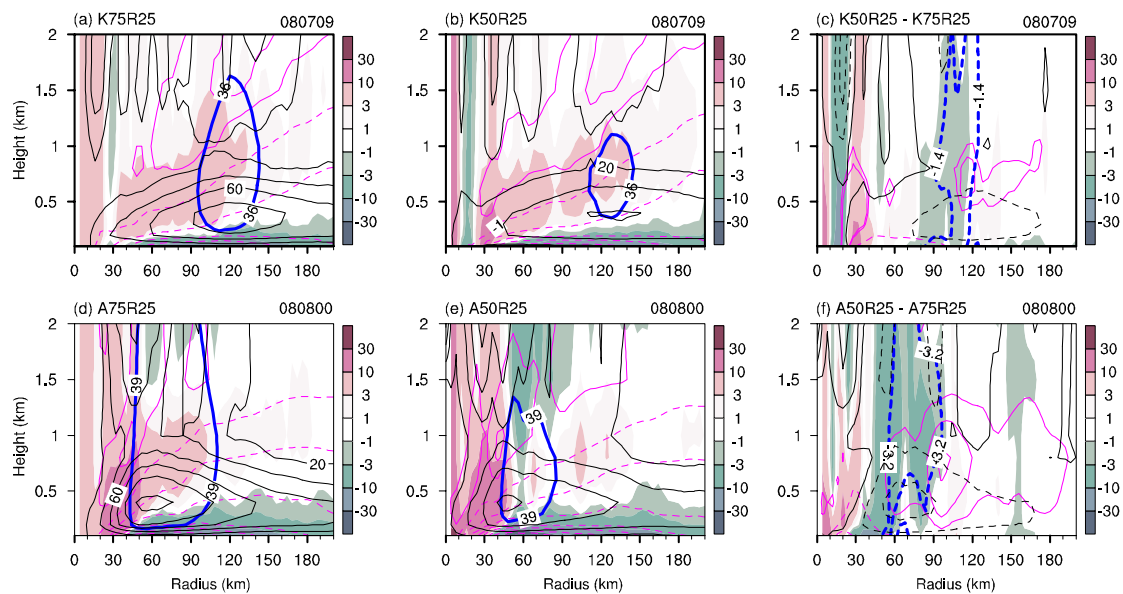
338 To gain insights into the impact of the parameter  $\alpha$  on TC intensification around RI onset,  
339 we conduct a comparative analysis of downward momentum mixing and its role in the  
340 development of the secondary circulation between A50R25 and A75R25. The net radial forcing  
341 (NRF) is defined as the sum of the Coriolis force, the centrifugal force, and the radial component  
342 of pressure gradient force (Smith et al. 2009):

$$343 \quad NRF = fv + \frac{v^2}{r} - \frac{1}{\rho} \frac{\partial p}{\partial r} \quad (10)$$

344 where  $f$  is the Coriolis parameter, and  $p$  is air pressure. Note that if  $NRF = 0$ , the tangential  
345 flow is in gradient wind balance; if  $NRF < 0$ , it is supergradient wind, and if  $NRF > 0$ , the  
346 flow is subgradient. An air parcel will undergo a radially inward acceleration when the NRF is  
347 negative or radially outward acceleration if the NRF is positive. Thus, the NRF governs the  
348 radial flow and hence the secondary circulation.

349 Figure 7 illustrates the azimuthally averaged eddy diffusivity, radial and tangential flows,  
350 along with the NRF during the initial (Figs. 7a,b) and mature (Figs. 7d,e) RI stages. The eddy  
351 diffusivity within the boundary layer has a maximum of 60–80  $\text{m}^2 \text{s}^{-1}$  for A50R25 (Figs. 7b,e),  
352 compared to 80–100  $\text{m}^2 \text{s}^{-1}$  for A75R25 (Figs. 7a,d). These eddy diffusivity maxima locate  
353 around the radii where the maximum tangential winds appear. Beneath these diffusivity maxima,  
354 a negative NRF is found within the lower boundary layer, where the radial inflow is accelerated.  
355 Travelling inward, the radial flow decelerates because the NRF turns to be positive around the  
356 radius of 40 km. Consequently, an outflow that relates to the supergradient wind is observed at  
357 the top of the boundary layer, just above the positive NRF core. In contrast to A75R25, A50R25

358 exhibits a stronger subgradient (supergradient) flow, resulting in a stronger radial inflow  
 359 (outflow) and a stronger secondary circulation (Figs. 7c,f). The results are consistent with  
 360 previous studies, which indicated that reducing  $\alpha$  in the boundary layer parameterization  
 361 causes enhanced boundary layer inflow, stronger secondary circulation, and stronger  
 362 convergence closer to the TC center (Zhang et al. 2017). Interestingly, the tangential velocity  
 363 core in A50R25 (Figs. 7b,e) occupies a shorter vertical extent than that in A75R25 (Figs. 7a,d),  
 364 although the maximum tangential velocities are comparable between them. As a result, a  
 365 negative difference in tangential wind is evident both above and at the bottom of the boundary  
 366 layer, coinciding with the negative NRF difference (Figs. 7c,f).

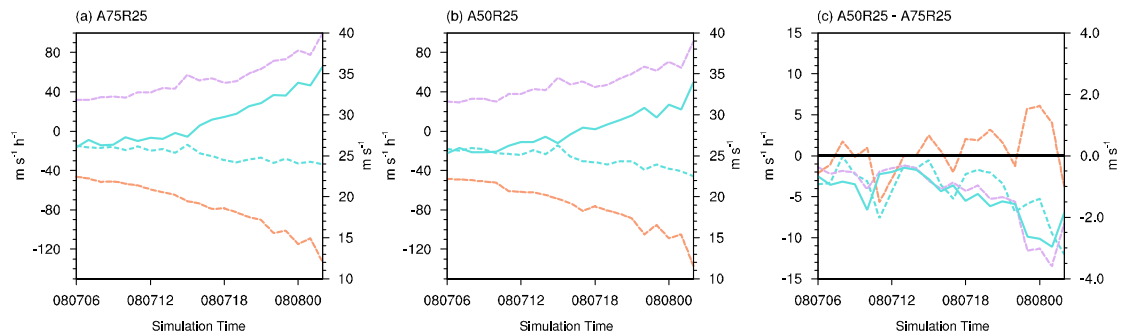


367  
 368 Figure 7. Radial-height plot of azimuthal-mean eddy diffusivity (black contour interval  $20 \text{ m}^2$   
 369  $\text{s}^{-1}$ ), the radial inflow (pink dashed contour interval  $2 \text{ m s}^{-1}$ ;  $-11$  to  $-1 \text{ m s}^{-1}$ ) and outflow (pink  
 370 solid contour interval  $0.5 \text{ m s}^{-1}$ ;  $0.5$  to  $2 \text{ m s}^{-1}$ ), tangential wind core (blue contour;  $\text{m s}^{-1}$ ),  
 371 and the net radial force (shading;  $\text{m s}^{-1} \text{h}^{-1}$ ) at 0900 UTC 7 August for (a) A75R25, (b) A50R25,  
 372 and (c) the difference between A50R25 and A75R25; (d–f) As in (a–c), but for 0000 UTC 8  
 373 August.

374

375 To illustrate the connection between the reduction of  $\alpha$  and the enhanced boundary layer  
 376 subgradient flow during RI period (Figs. 7c,f), we explore the origin of the subgradient flow in  
 377 the boundary layer. Since  $NRF$  is determined by the inward-pointing pressure gradient force  
 378  $(-\frac{1}{\rho} \frac{\partial p}{\partial r})$  and the outward Coriolis and centrifugal forces  $(fv + \frac{v^2}{r})$ , we calculate these terms at

379 100-m height, averaged within 0.5–1.0 RMW, where the negative NRF difference is obvious  
 380 (Figs. 7c,f). The calculation results during 0600 UTC 7 August and 0200 UTC 8 August for  
 381 A75R25 and A50R25 are shown in Figs. 8a,b, respectively. Given the increasing trend of the  
 382 positive Coriolis and centrifugal terms, the negative NRF continues to decrease during the  
 383 simulation time. This implies the dominant role of the radial pressure gradient force in  
 384 generating the negative NRF for A75R25 and A50R25 (Figs. 8a,b). Additionally, we compare  
 385 these terms between the two experiments in Fig. 8c. It shows that the radial pressure gradients  
 386 of the two experiments are approximately equal, as their difference varies around zero during  
 387 this period. This can be explained by the comparable tangential velocities at the top of the  
 388 boundary layer as indicated in Figs. 7c,f. However, the difference in NRF becomes obvious  
 389 towards the mature stage of RI, sharing the similar tendency as that of the sum of the Coriolis  
 390 and centrifugal forces (Fig. 8c). This means that in comparison with A75R25, A50R25 produces  
 391 the stronger subgradient due to the reduced Coriolis and centrifugal forces, which further results  
 392 from the weaker tangential winds (Figs. 7c,f, and 8c).



393  
 394 Figure 8. Evolution of azimuthal-mean radial pressure gradient force (orange;  $\text{m s}^{-1} \text{h}^{-1}$ ), sum  
 395 of the outward Coriolis and centrifugal forces (purple;  $\text{m s}^{-1} \text{h}^{-1}$ ), the net radial force (dashed  
 396 green;  $\text{m s}^{-1} \text{h}^{-1}$ ), and tangential velocity (green; right coordinates;  $\text{m s}^{-1}$ ), radially averaged  
 397 within the 0.5–1.0 RMW for (a) A75R25, (b) A50R25, and (c) the difference between A50R25  
 398 and A75R25.

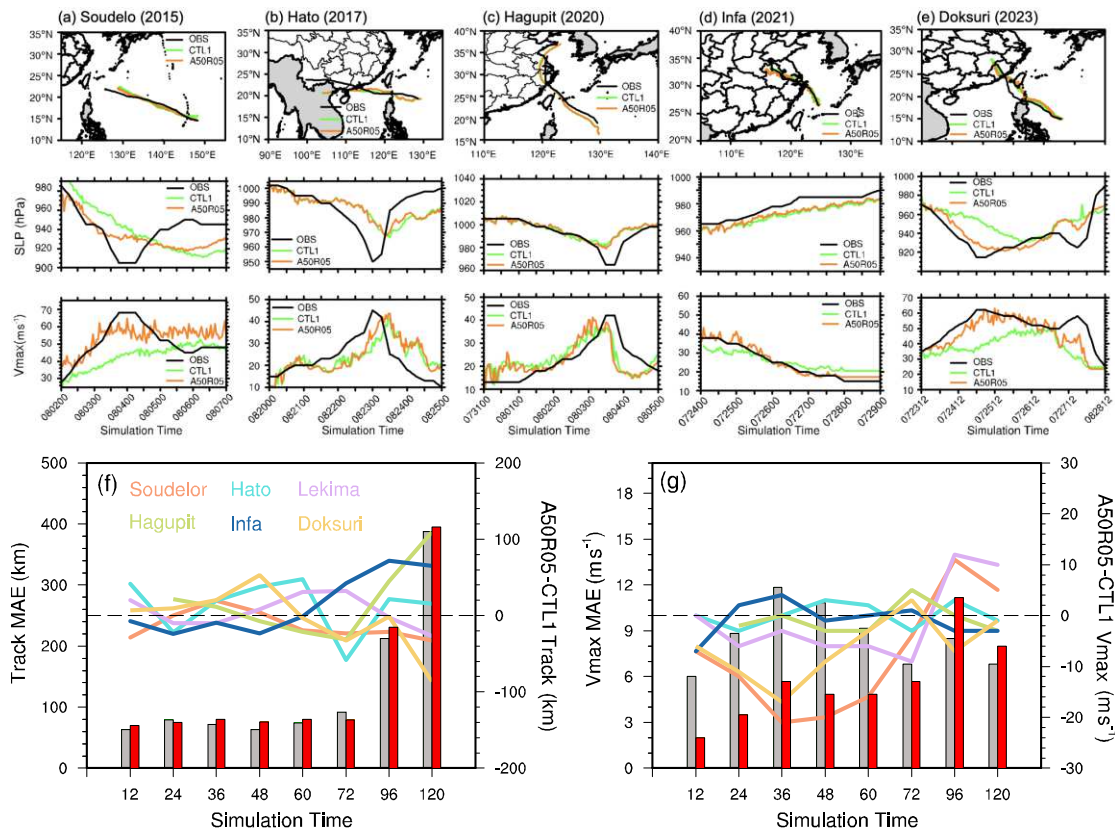
399

400 Therefore, a larger  $\alpha$  induces a larger vertical gradient of eddy diffusion, which more  
 401 efficiently mixes azimuthal momentum down to the surface, enhancing the low-level tangential  
 402 wind (Figs. 7c,f), and thereby strengthening the outward Coriolis and centrifugal forces in the  
 403 lower boundary layer (Fig. 8c). On the contrary, a reduced  $\alpha$  leads to weaker tangential wind

404 and weaker outward Coriolis and centrifugal forces (Figs. 7c,f), and thus a larger gradient wind  
405 imbalance in the lower boundary layer. This stronger imbalance, in turn, drives stronger inflow  
406 and strengthens the overturning circulation in the inner core. Previous studies (Gopalakrishnan  
407 et al. 2013; Gopalakrishnan et al. 2021) considered that larger (smaller) diffusion has a deeper  
408 (shallower) boundary layer and negates (enhances) the gradients between the surface layer and  
409 the PBL, and therefore leads to weaker (stronger) frictional forces and weaker (stronger) inflow.  
410 Here we raises a new pathway by which the peak magnitude of vertical diffusivity influences  
411 boundary layer unbalanced dynamics and intensification process under identical PBL height  
412 condition.

#### 413 *d. Implementation on RI events*

414 To evaluation the performance of the optimized  $K_m$  parameterization (A50R05) in TC  
415 forecasting, simulations of five additional TCs over the western North Pacific are conducted  
416 and compared between configurations with the CTL1 and A50R05 (see Table 1). These TC  
417 cases include Super Typhoons Soudelor (2015), Hato (2017), and Doksuri (2023), as well as  
418 Strong Typhoons Hagupit (2020) and In-fa (2021). Note that these cases are chosen due to the  
419 poor performance of the control run (CTL1) in TC intensity simulation (Fig. 9). Clearly, CTL1  
420 fails to capture the RI trends for Soudelor (Fig. 9), Doksuri (Fig. 9), and Lekima (Fig. 1).  
421 Additionally, discrepancies exist between the simulated intensity and best-track for Hato (Fig.  
422 9b) and Hagupit (Fig. 9c). For In-fa, the CTL1 simulated intensity is weaker initially but  
423 stronger later (Fig. 9d). In comparison, A50R05 substantially improves the simulated TC  
424 intensities, particularly during RI periods for Soudelor (Fig. 9a) and Doksuri (Fig. 9e). The  
425 simulated intensity during the weaking stage of In-fa is more consistent with the observation  
426 (Fig. 9d). however, simulated intensities for Hato (Fig. 9b) and Hagupit (Fig. 9c) show limited  
427 improvement, possibly due to the inadequate progress in track simulations.



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Figure 9. The track, minimum sea level pressure and 10-m maximum wind in experiments CTL1 and A50R05, compared with the best-track from China Meteorological Administration for Typhoons (a) Soudelor, (b) Hato, (c) Hagupit, (d) In-fa, and (e) Doksuri. Absolute errors composited by six typical TC cases at given time interval for experiments CTL1 (gray bar) and A50R05 (red bar), and relative errors for each TC between A50R05 and CTL1 in (f) track (km) and (g) maximum wind speed ( $\text{m s}^{-1}$ ). Note that Typhoon Hagupit was recorded in the best track 24 h after the initiation of the simulation. Thus, the errors at 12 h are not included here.

Absolute errors of the simulated tracks and intensities are composited for the six TC cases and presented at specific time intervals in Figs. 9f,g, accompanied by relative errors between A50R05 and CTL1 for each TC. A negative relative error indicates reduction absolute error or improved simulation, while a positive value denotes deterioration. As shown in Fig.9f, the simulated tracks are rarely improved in A50R05. Absolute track errors remain comparable to those in CTL1, ranging from 80 to 95 km prior to 72-hour, but significantly increase to 200 and 400 km over the subsequent two days. Notably, composite intensity errors are significantly reduced by 58.7% (or  $4.5 \text{ m s}^{-1}$ ) averaged within 72-hour in the simulation time (Fig. 9g).

446 Consistent with results in Figs. 9a-e, this reduction in intensity error is primarily attributed to  
447 the improved RI simulations for Typhoons Soudelor, Lekima, and Doksuri, as indicated by their  
448 negative relative errors (Fig. 9g).

## 449 **5. Summary and discussion**

450 We have proposed an improved eddy diffusivity ( $K_m$ ) parameterization for the eddy-  
451 diffusivity mass-flux (EDMF) scheme considering Tropical Cyclone (TC) conditions. Based on  
452 the observational constraints from Zhang et al. (2011) and Zhang and Drennan (2012), we  
453 optimize two scaling parameters in association with the vertical extent ( $h$ ) and peak magnitude  
454 ( $\alpha$ ) of the modeled  $K_m$ . Further examination reveals that the dual-scale controls of  $K_m$  play  
455 essential and distinct roles in TC rapid intensification (RI).

456 The vertical extent scale  $h$  determines the early vortex spin-up through momentum  
457 diffusion and moisture flux processes. Dynamically, a decrease in  $h$  leads to the reduced  
458 diffusion and hence the faster tangential wind acceleration. Thermodynamically, more moisture  
459 is retained within the bottom of the boundary layer due to the rapid weakening of moisture flux  
460 with height in the reduced  $h$ . Consequently, the increased near-surface moisture and the  
461 enhanced tangential wind may cooperate in the similar way as the positive feedback process in  
462 the wind-induced surface heat exchange (WISHE) intensification mechanism.

463 The magnitude scale parameter  $\alpha$  modulates the gradient imbalance within the boundary  
464 layer and hence the secondary circulation during RI onset by downward momentum mixing. As  
465 the axisymmetric tangential winds accelerate at the top of the TC boundary layer due to the  
466 gradient wind balance dynamics, the eddy diffusivity mixes azimuthal momentum down to the  
467 surface, thereby enhancing the outward Coriolis and centrifugal forces. Consequently, the  
468 gradient imbalance between the Coriolis, centrifugal, and the radially inward pressure gradient  
469 forces is reduced. Therefore, a reduced  $\alpha$  leads to a smaller increase in tangential wind near  
470 surface, and hence the larger gradient imbalance. The resulting stronger radial acceleration and  
471 stronger secondary circulation in the reduced  $\alpha$  account for a faster and earlier contraction of  
472 the radius of maximum wind during RI period.

473 To our knowledge, the present study presents a first look into key process in association  
474 with the parameterized  $K_m$  leading to RI of a TC. We believe that the results are also important

475 for providing a framework for further improving parameterization schemes. It should be noted  
476 that more computing resources are still needed to test the robustness of the results with more  
477 TC cases. This is a topic for future studies.

478

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484

485 *Author contributions.* Xue-Song Zhu conceived the study and analyzed the initial results. Xu  
486 Zhang analyzed the subgrid-scale parameterization. Bowen Zhao contributed to the mapping  
487 and calculating. Wei Huang and Hui Yu prepared the modeling framework. Qijun Huang and  
488 Shanghong Wang discussed the TC intensification process.

489

490 *Data availability statement.* The numerical model simulations upon which this study were based  
491 are too large to archive or to transfer. Instead, the datasets are available from Xue-Song Zhu  
492 ([zhuxs@typhoon.org.cn](mailto:zhuxs@typhoon.org.cn)) upon request. The TC best-track data in this study was provided from  
493 China Meteorological Administration and can be downloaded from  
494 <https://tcdata.typhoon.org.cn/zjljsjj.html>. GFS data was downloaded from  
495 <https://rda.ucar.edu/datasets/d084001/>.

496

497 *Code available statement.* The code for the analysis and mapping used in this study is available  
498 via Zenodo (<https://zenodo.org/records/15812533>).

499

## 500 **Reference**

501 Bechtold, P., M. Köhler, T. Jung, D.-R. Francisco, L. Martin, J. R. Mark, V. Frederic, and B.  
502 Gianpaolo, 2008: Advances in simulating atmospheric variability with the ECMWF model:  
503 From synoptic to decadal time-scales. *Quart. J. Roy. Meteor. Soc.*, 134(634): 1337–1351,  
504 <https://doi.org/10.1002/qj.289>.

505 Bechtold, P., N. Semane, P. Lopez, J. P. Chaboureau, and N. Bormann, 2014: Representing  
506 equilibrium and nonequilibrium convection in large-scale models. *J. Atmos. Sci.*, 71(2): 734–  
507 753, <https://doi.org/10.1175/JAS-D-13-0163.1>.

508 Bhatia, K. T., G. A. Vecchi, T. R. Knutson, H. Murakami, C. E. Whitlock, 2019: Recent increases  
509 in tropical cyclone intensification rates. *Nat. Commun.* 10, 635,  
510 <https://doi.org/10.1038/s41467-019-08963-y>.

511 Cangialosi, J. P. , E. Blake, M. Demaria, A. Penny, A. Latto, and E. Rappaport, and V. Tallapragada,  
512 2020: Recent progress in tropical cyclone intensity forecasting at the national hurricane center.  
513 *Weather and Forecasting*, 35(5), 1913-1922, <https://doi.org/10.1175/WAF-D-20-0059.1>.

514 Chen, X. (2022). How do planetary boundary layer schemes perform in hurricane conditions: A  
515 comparison with large-eddy simulations. *J. Adv. Model. Earth Syst.*, 14, e2022MS003088,  
516 <https://doi.org/10.1029/2022MS003088>.

517 DeMaria, M., C. R. Sampson, J. A. Knaff, and K. D. Musgrave, 2014: Is tropical cyclone intensity  
518 guidance improving? *Bull. Am. Meteorol. Soc.* 95, 387–398 (2014),  
519 <https://doi.org/10.1175/BAMS-D-12-00240.1>.

520 Durran, D.R., J. B. Klemp, 1982: The effects of moisture on trapped mountain lee waves. *J. Atmos.*  
521 *Sci.* 39, 2490–2506. [https://doi.org/10.1175/1520-0469\(1982\)039<2490:TEOMOT>2.0.CO;2](https://doi.org/10.1175/1520-0469(1982)039<2490:TEOMOT>2.0.CO;2).

522 Eliassen, A., 1971: On the Ekman layer in a circular vortex. *J. Meteor. Soc. Japan*, 49, 784–789,  
523 [https://doi.org/10.2151/jmsj1965.49A.0\\_784](https://doi.org/10.2151/jmsj1965.49A.0_784).

524 Emanuel, K., 1986: An air-sea interaction theory for tropical cyclones. Part I: Steady state  
525 maintenance. *J. Atmos. Sci.*, 43, 585–604, [https://doi.org/10.1175/1520-0469\(1986\)043<0585:aasitf>2.0.co;2](https://doi.org/10.1175/1520-0469(1986)043<0585:aasitf>2.0.co;2).

527 Emanuel, K., 2003: Tropical cyclones. *Annu. Rev. Earth Planet. Sci.*, 31, 75–104,  
528 <https://doi.org/10.1146/annurev.earth.31.100901.141259>.

529 Emanuel, K., 2017: Will global warming make hurricane forecasting more difficult? *Bull. Am.*  
530 *Meteorol. Soc.* 98, 495–501, <https://doi.org/10.1175/BAMS-D-16-0134.1>

531 Emanuel, K., and F. Zhang, 2017: The role of inner-core moisture in tropical cyclone predictability  
532 and practical forecast skill. *J. Atmos. Sci.* 74, 2315–2324, [https://doi.org/10.1175/JAS-D-17-](https://doi.org/10.1175/JAS-D-17-0008.1)  
533 [0008.1](https://doi.org/10.1175/JAS-D-17-0008.1).

534 Gopalakrishnan, S., A. Hazelton, and J. A. Zhang, 2021: Improving hurricane boundary layer  
535 parameterization scheme based on observations. *Earth and Space Science*, 8, e2020EA001422.  
536 <https://doi.org/10.1029/2020EA001422>.

537 Gopalakrishnan, S., F. Marks, J. A. Zhang, X. Zhang, J.-W. Bao, and V. Tallapragada, 2013: A  
538 study of the impacts of vertical diffusion on the structure and intensity of tropical cyclones  
539 using the high resolution HWRF system. *J. Atmos. Sci.*, 70(2), 524–541,  
540 <https://doi.org/10.1175/JAS-D-11-0340.1>.

541 Han, J., M. Witek, J. Teixeira, R. Sun, H. Pan, J. Fletcher, and C. Bretherton, 2016: Implementation  
542 in the NCEP GFS of a Hybrid Eddy-Diffusivity Mass-Flux (EDMF) Boundary Layer  
543 Parameterization with Dissipative Heating and Modified Stable Boundary Layer Mixing.  
544 *Weather and Forecasting*, 2016, 31:341–352, <https://doi.org/10.1175/WAF-D-15-0053.1>.

545 Hong, S. Y., Y. Noh, J. Dudhia, 2006: A new vertical diffusion package with an explicit treatment  
546 of entrainment processes. *Mon. Wea. Rev.*, 134(9), 2318–2341,  
547 <https://doi.org/10.1175/MWR3199.1>.

548 Huang, Q., X. Zhang, X. Zhu, Y. Zhu, and Y. Yang, 2025: The impact of the representation of in-  
549 cloud mixing effect in the planetary boundary layer scheme on the simulated track of tropical  
550 cyclone Infa (2021). *Atmos. Res.*, 326, 108274,  
551 <https://doi.org/10.1016/j.atmosres.2025.108274>.

552 Iacono, M. J., J. S. Delamere, E. J. Mlawer, M. W. Shephard, S. A. Clough, and W. D. Collins, 2008:  
553 Radiative forcing by long-lived greenhouse gases: Calculations with the AER radiative transfer  
554 models. *J. Geophys. Res. Atmos.*, 113(D13), <https://doi.org/10.1029/2008JD009944>.

555 Kepert, J. D., 2001: The dynamics of boundary layer jets within the tropical cyclone core. Part I:  
556 Linear theory. *J. Atmos. Sci.*, 58, 2469–2484, [https://doi.org/10.1175/1520-0469\(2001\)058<2469:TDOBLJ>2.0.CO;2](https://doi.org/10.1175/1520-0469(2001)058<2469:TDOBLJ>2.0.CO;2).

558 Kepert, J. D., 2012: Choosing a boundary layer parameterization for tropical cyclone modeling.  
559 *Mon. Wea. Rev.*, 140, 1427–1445, <https://doi.org/10.1175/MWR-D-11-00217.1>.

560 Li, X., Y. Zhang, X. Peng, W. Chu, Y. Lin, and J. Li, 2022: Improved climate simulation by using  
561 a double-plume convection scheme in a global model. *J. Geophys. Res. Atmos.*, 127(11):  
562 e2021JD036069. <https://doi.org/10.1029/2021JD036069>.

563 Li, X., Y. Zhang, Y. Lin, X. Peng, B. Zhou, P. Zhai and J. Li, 2023: Impact of revised trigger and  
564 closure of the double-plume convective parameterization on precipitation simulations over east  
565 Asia. *Adv. Atmos. Sci.*, 40(7): 1225–1243, <https://doi.org/10.1007/s00376-022-2225-9>.

566 Li, Y., Y. Tang, S. Wang, R. Toumi, X. Song, and Q. Wang, 2023: Recent increases in tropical  
567 cyclone rapid intensification events in global offshore regions. *Nat. Commun.* 14, 5167,  
568 <https://doi.org/10.1038/s41467-023-40605-2>.

569 Liu, K. S., and J. C. L. Chan, 2022: Growing threat of rapidly-intensifying tropical cyclones in East  
570 Asia. *Adv. Atmos. Sci.* 39, 222–234, <https://doi.org/10.1007/s00376-021-1126-7>.

571 Lorsolo, S., J. L. Schroeder, P. Dodge, and F. Marks Jr., 2008: An observational study of hurricane  
572 boundary layer small-scale coherent structures. *Mon. Wea. Rev.*, 136, 2871–2893,  
573 <https://doi.org/10.1175/2008MWR2273.1>.

574 Louis, J.F., 1979. A parametric model of vertical eddy fluxes in the atmosphere. *Bound. Layer*  
575 *Meteorol.* 17, 187–202. <https://doi.org/10.1007/BF00117978>.

576 Ming, J., and J. A. Zhang, 2016: Effects of surface flux parameterization on the numerically  
577 simulated intensity and structure of Typhoon Morakot (2009). *Adv. Atmos. Sci.*, 33, 58–72,  
578 <https://doi.org/10.1007/s00376-015-4202-z>.

579 Montgomery, M. T., and R. K. Smith, 2014: Paradigms for tropical cyclone intensification.  
580 *Australian Meteorological and Oceanographic Journal*, 64 37–66,  
581 <https://doi.org/10.22499/2.6401.005>.

582 Montgomery, M. T., R. K. Smith, and S. Nguyen, 2010: Sensitivity of tropical cyclone models to  
583 the surface drag coefficient. *Quart. J. Roy. Meteor. Soc.*, 136, 1945–1953,  
584 <https://doi.org/10.1002/qj.702>.

585 Montgomery, M. T., G. Kilroy, R. K. Smith, and N. Ćrnivec, 2020: Contribution of eddy  
586 momentum processes to tropical cyclone intensification. *Quart. J. Roy. Meteor. Soc.*, 146,  
587 3101–3117, <https://doi.org/10.1002/qj.3837>.

588 O’Brien, J. J., 1970: A note on the vertical structure of the eddy exchange coefficient in the planetary  
589 boundary layer. *J. Atmos. Sci.*, 27, 1213–1215, [https://doi.org/10.1175/1520-0469\(1970\)027<1213:ANOTVS>2.0.CO;2](https://doi.org/10.1175/1520-0469(1970)027<1213:ANOTVS>2.0.CO;2).

590

591 Ooyama, K. V., 1969: Numerical simulation of the life cycle of tropical cyclones. *J. Atmos. Sci.*,  
592 26, 3–40, [https://doi.org/10.1175/15200469\(1969\)026%3C0003:NSOTLC%3E2.0.CO;2](https://doi.org/10.1175/15200469(1969)026%3C0003:NSOTLC%3E2.0.CO;2).

593 Powell, M. D., P. J. Vickery, and T. A. Reinhold, 2003: Reduced drag coefficient for high wind  
594 speeds in tropical cyclones. *Nature*, 422, 279–283, <https://doi.org/10.1038/nature01481>.

595 Smith, R. K., and M. T. Montgomery, 2010: Hurricane boundary layer theory. *Quart. J. Roy. Meteor.*  
596 *Soc.*, 136A, 1665–1670, <https://doi.org/10.1002/qj.679>.

597 Smith, R. K., M. T. Montgomery, and S. V. Nguyen, 2009: Tropical cyclone spin-up revisited. *Quart.*  
598 *J. Roy. Meteor. Soc.*, 135, 1321–1335, <https://doi.org/10.1002/qj.428>.

599 Song, J., Y. Duan, and P. J. Klotzbach, 2020: Increasing trend in rapid intensification magnitude of  
600 tropical cyclones over the western North Pacific. *Environ. Res. Lett.* 15, 084043,  
601 <https://doi.org/10.1088/1748-9326/ab9140>.

602 Tallapragada, V., C. Kieu, Y. Kwon, S. Trahan, Q. Liu, Z. Zhang, and I. Kwon, 2014: Evaluation  
603 of storm structure from the operational HWRf model during 2012 implementation. *Mon. Wea.*  
604 *Rev.*, 142(11), 4308–4325, <https://doi.org/10.1175/MWR-D-13-00010.1>.

605 Troen, I. B., & Mahrt, L. (1986). A simple model of the atmospheric boundary layer; sensitivity to  
606 surface evaporation. *Boundary-Layer Meteorology*, 37(1), 129–148.  
607 <https://doi.org/10.1007/BF00122760>.

608 Vogelesang, D. H. P., and A. A. M. Holtslag, 1996: Evaluation and model impacts of alternative  
609 boundary-layer height formulations. *Boundary-Layer Meteorology*, 81(3), 245–269.  
610 <https://doi.org/10.1007/BF02430331>.

611 Xu, K. M., and D. A. Randall, 1996: A semiempirical cloudiness parameterization for use in climate  
612 models. *J. Atmos. Sci.*, 53(21), 3084–3102, [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0469(1996)053<3084:ASCPFU>2.0.CO;2)  
613 [0469\(1996\)053<3084:ASCPFU>2.0.CO;2](https://doi.org/10.1175/1520-0469(1996)053<3084:ASCPFU>2.0.CO;2)

614 Zhang, J. A., and F. D. Marks, M. T. Montgomery, and S. Lorsolo, 2011: An estimation of turbulent  
615 characteristics in the low-level region of intense Hurricanes Allen (1980) and Hugo (1989).  
616 *Mon. Wea. Rev.*, 139, 1447–1462, <https://doi.org/10.1175/2010MWR3435.1>.

617 Zhang, J. A., and W. M. Drennan, 2012: An observational study of vertical eddy diffusivity in the  
618 hurricane boundary layer. *J. Atmos. Sci.*, 69, 3223–3236, [https://doi.org/10.1175/JAS-D-11-](https://doi.org/10.1175/JAS-D-11-0348.1)  
619 [0348.1](https://doi.org/10.1175/JAS-D-11-0348.1).

620 Zhang, J. A., and R. T. Rogers, 2019: Effects of Parameterized Boundary Layer Structure on  
621 Hurricane Rapid Intensification in Shear. *Mon. Wea. Rev.*, 147, 853–871,  
622 <https://doi.org/10.1175/MWR-D-18-0010.1>.

623 Zhang, J. A., D. S. Nolan, R. F. Rogers, and V. Tallapragada, 2015: Evaluating the impact of  
624 improvements in the boundary layer parameterization on hurricane intensity and structure  
625 forecasts in HWRF. *Mon. Wea. Rev.*, 143, 3136–3155, [https://doi.org/10.1175/MWR-D-14-](https://doi.org/10.1175/MWR-D-14-00339.1)  
626 [00339.1](https://doi.org/10.1175/MWR-D-14-00339.1).

627 Zhang, J. A., R. F. Rogers, and V. Tallapragada, 2017: Impact of parameterized boundary layer  
628 structure on tropical cyclone rapid intensification forecasts in HWRF. *Mon. Wea. Rev.*, 145,  
629 1413–1426, <https://doi.org/10.1175/MWR-D-16-0129.1>.

630 Zhang, Y., J. Li, R. Yu, et al. 2020. A multiscale dynamical model in a dry-mass coordinate for  
631 weather and climate modeling: Moist dynamics and its coupling to physics. *Mon. Wea. Rev.*,  
632 148(7): 2671–2699, <https://doi.org/10.1175/mwr-d-19-0305.1>.

633 Zhang, Y., X. Li, Z. Liu, X. Rong, J. Lin, Y. Zhou, and S. Chen, 2022: Resolution  
634 sensitivity of the GRIST nonhydrostatic model from 120 to 5 km (3.75 km)  
635 during the DYAMOND winter. *Earth and Space Science*, 9(9): e2022EA002401,  
636 <https://doi.org/10.1029/2022EA002401>.

637 Zhang, Y., J. Li, R. Yu, S. Zhang, Z. Liu, J. Huang, and Y. Zhou, 2019: A layer-averaged  
638 nonhydrostatic dynamical framework on an unstructured mesh for global and regional  
639 atmospheric modeling: Model description, baseline evaluation, and sensitivity exploration. *J.*  
640 *Adv. Model. Earth Syst.*, 11(6): 1685–1714, <https://doi.org/10.1029/2018MS001539>.

641 Zhang, Y, R. Yu, J. Li, X. Li, X. Rong, X. Peng, and Y. Zhou, 2021: AMIP simulations of a global  
642 model for unified weather–climate forecast: Understanding precipitation characteristics and  
643 sensitivity over East Asia. *J. Adv. Model. Earth Syst.*, 13(11): e2021MS002592,  
644 <https://doi.org/10.1029/2021MS002592>.

645 Zhao, H., X. Duan, G. B. Raga, and P. J. Klotzbach, 2018: Changes in characteristics of rapidly  
646 intensifying Western North Pacific tropical cyclones related to climate regime shifts. *J. Clim.*  
647 31, 8163–8179, <https://doi.org/10.1175/jcli-d-18-0029.1>.