# Supplementary Information for strongly-anharmonic gateless gatemon qubits based on InAs/Al 2D heterostructure

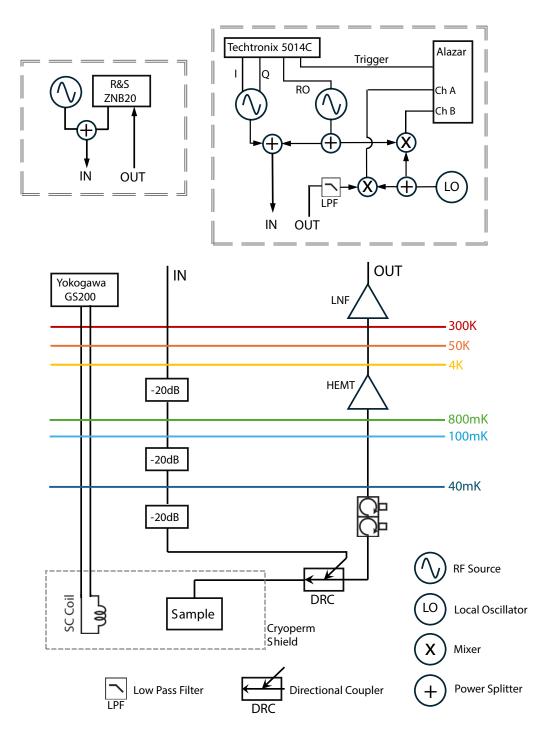
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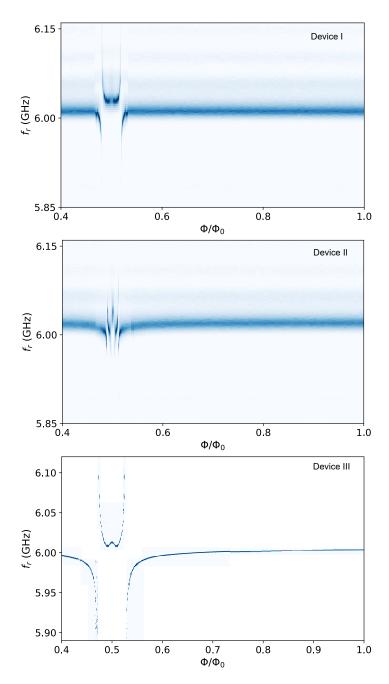
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# Supplementary Information 1: Experimental setup



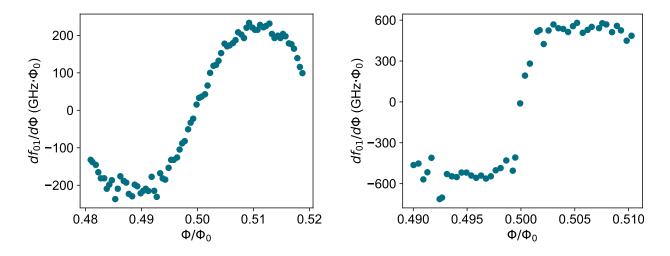
Supplementary Figure 1: Schematics of the experimental setup use for measuring the flux-tunable gatemon qubit.

## Supplementary Information 2: One-Tone Spectroscopy



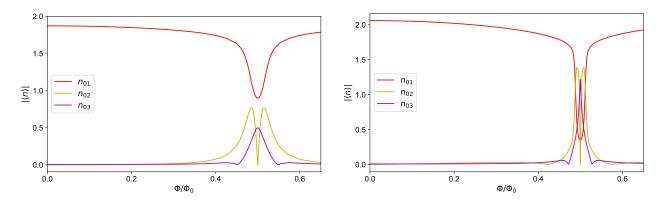
Supplementary Figure 2: One-tone spectroscopy showing  $|S_{11}|$  as a function of the resonator drive frequency  $f_{\rm r}$  and the applied external magnetic flux  $\Phi/\Phi_0$  for device I, II and III, respectively. The resonator response exhibits a vacuum Rabi splitting with a cavity-qubit coupling strength of  $g=122\,{\rm MHz}$  for device I,  $g=101\,{\rm MHz}$  for device II and  $g=170\,{\rm MHz}$  for device III, respectively.

## Supplementary Information 3: First-order flux insensitivity at $\Phi = 0.5 \Phi_0$



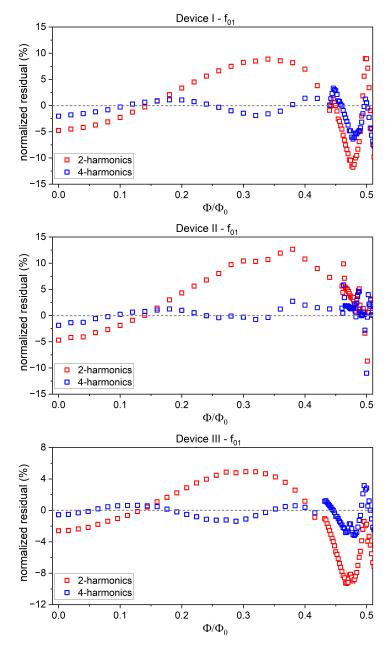
Supplementary Figure 3: Derivative of the  $|0\rangle - |1\rangle$  transition qubit frequency  $df_{01}/d\Phi$  as a function of the applied external magnetic flux  $\Phi/\Phi_0$  for device I (left) and device II (right), indicating a first-order insensitivity to flux at the half-flux quanta  $\Phi = 0.5 \Phi_0$ .

#### Supplementary Information 4: Charge-matrix elements



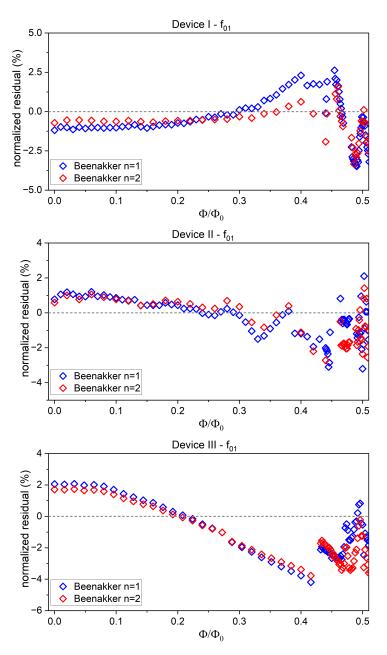
Supplementary Figure 4: Charge matrix elements vs flux  $\Phi/\Phi_0$  for device I (left) and device II (right).

## Supplementary Information 5: Higher-harmonic model comparison



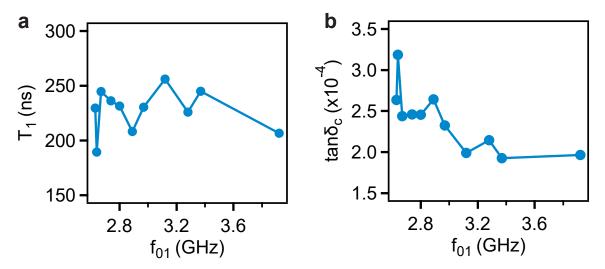
Supplementary Figure 5: Normalized residual  $(f_{\text{model}} - f_{\text{meas}})/f_{\text{meas}}$  as a function of  $\Phi/\Phi_0$  for the  $|0\rangle - |1\rangle$  qubit transition using the higher-harmonic model for device I, II and III, respectively. Here, k refers to the number of leading Fourier harmonic terms used to approximate the Josephson potential energy in  $U = \sum_k E_{\text{J}}^k \cos{(k\varphi)}$ .

## Supplementary Information 6: Multi-transparency model



Supplementary Figure 6: Normalized residual  $(f_{\text{model}} - f_{\text{meas}})/f_{\text{meas}}$  as a function of  $\Phi/\Phi_0$  for the  $|0\rangle - |1\rangle$  qubit transition using the single and multiple transparency model for device I, II and III, respectively. Here, n refers to the number of characteristic channel transparencies for each Josephson junction. We observe that increasing n from a single (n=1) characteristic channel transparency to two (n=2) channel transparencies does not lead to any significant reduction in the residuals.

# Supplementary Information 7: $T_1$ flux dependence



Supplementary Figure 7: **a.**  $T_1$  as a function of the  $|0\rangle - |1\rangle$  transition qubit frequency  $f_{01}$  in the vicinity of half-flux quanta  $\Phi = 0.5 \, \Phi_0$ . **b.** The effective dielectric loss tangent  $\tan \delta_{\rm c}$  vs the qubit frequency  $f_{01}$  extracted from (**a**) using  $\tan \delta_{\rm c} = \frac{1}{T_1 \omega_{01}}$ , where  $\omega_{01} = 2\pi f_{01}$ .