

1 **Integrating Machine Learning with**
2 **Metabolic Models for Precision Trauma**
3 **Care:**
4 **Personalized Endotype Stratification**
5 **and Metabolic Target Identification:**
6 **Supplementary material 3**

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20 **1 Introduction**

21 Previous studies have identified four shock-induced endotheliopathy (SHINE)
22 phenotypes [1]. These phenotypes are associated with significant differences
23 in the metabolic profiles from blood samples, which correlate with variations
24 in mortality rates and are independent of the severity of the injury. Using
25 Genome-scale metabolic model (GEM) and flux balance analysis [2] on data
26 from 95 trauma patients, we derived a constraint space of solutions that de-
27 scribe their reaction fluxes. This section goal is to identify patterns in the pa-
28 tients' metabolic flux profiles associated with the different endotypes, allowing
29 for patient stratification and the identification of potential therapeutic targets
30 by applying. To this aim a pipeline combining different approaches based on lin-
31 ear multivariate analysis is developed. The pipeline comprises different steps: i.

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³² data preprocessing, ii. dimensionality reduction [3] and iii. clustering to identify
³³ potential patterns (Figure 1). Tasks in this section were performed using MAT-
³⁴ LAB (version R2022a) and Python (version 3.9.12) with the packages numpy
(1.21.5) and scikit-learn (1.0.2).

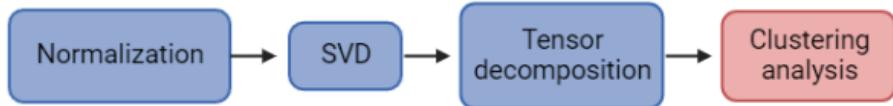


Figure 1: First method summary

³⁵

³⁶ 2 Source Data

³⁷ This study employs a mechanistic genome-scale metabolic model (GEM) inte-
³⁸ grated with flux balance analysis (FBA) to analyze metabolic flux profiles of
³⁹ trauma patients. We use the iEC3006 GEM, which includes 3006 reactions, to
⁴⁰ generate a baseline model. By sampling the baseline model the initial lower and
⁴¹ upper flux boundaries of the exchange reactions were determined (Figure 2).
⁴² Next, these boundaries are adjusted to reflect patient-specific conditions using
⁴³ metabolic concentration data collected from 95 trauma patients relative to a
⁴⁴ control group of healthy individuals. Patient-specific flux boundaries are cal-
⁴⁵ culated by determining the ratio between metabolite concentrations in patients
⁴⁶ and the control group. For example, if a patient exhibits twice the metabolite
⁴⁷ secretion compared to healthy individuals, the corresponding reaction’s mini-
⁴⁸ mum and maximum flux boundaries in the baseline model are doubled. This
⁴⁹ procedure is applied to all reactions in the baseline model to generate trauma-
⁵⁰ specific metabolic boundaries. To account for variability in the control group,
⁵¹ we create three sets of boundaries per patient using the mean, minimum, and
⁵² maximum concentrations. FBA is performed under steady-state conditions,
⁵³ where the mass of substrates equals the mass of products ($A = C + D$; Fig-
⁵⁴ ure 2). Mathematically, this condition is expressed as $S \cdot v = 0$, where S is
⁵⁵ the stoichiometric matrix and v is the flux vector constrained by the adjusted
⁵⁶ boundaries. Since large metabolic models contain more reactions than metabo-
⁵⁷ lites, this system has infinite feasible solutions rather than a single solution. To
⁵⁸ characterize this solution space, we perform random sampling of steady-state
⁵⁹ flux solutions, generating a matrix where rows represent reaction fluxes (3006
⁶⁰ reactions) and columns correspond to sampled solution points. This sampling
⁶¹ defines the constrained solution space of metabolic fluxes for each patient. Each
⁶² patient’s data is stored as three MATLAB structure arrays, corresponding to
⁶³ the flux boundaries derived from the minimum, mean, and maximum values of
⁶⁴ the control group. Each structure contains the lower and upper flux boundaries,
⁶⁵ reaction names, and the sampling output. The resulting matrix for each patient
⁶⁶ has 3006 reaction fluxes and 18036 ($6012 \cdot 3$) randomly sampled solution points,
⁶⁷ optimized to represent the solution space effectively. In total, we generate 95
⁶⁸ patient-specific models, each with three variations, resulting in 285 matrices.
⁶⁹ These matrices provide a comprehensive representation of reaction fluxes and
⁷⁰ their constrained solution spaces, enabling detailed metabolic analysis of trauma
⁷¹ patients.

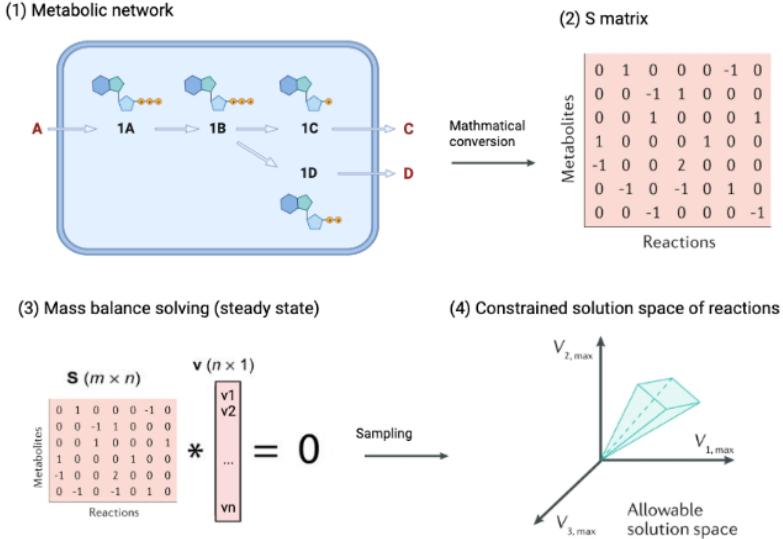


Figure 2: Sampling Solution Points of Reaction Fluxes Using FBA: (1). Modeling of Reactions: The blue line represents the cell membrane, with A (in red) as the substrate, and C and D as the products. (2). Stoichiometric Matrix: This matrix shows the production (1) and elimination (-1) of different metabolites across multiple reactions. (3). Steady State Condition: At steady state, ($S \cdot v = 0$) defines the flux through each reaction. (4). Post-Sampling Matrix: After sampling, we obtain a new matrix (reactions by solution points) that defines the solution space of the reactions for the patient.

72 3 Pre-processing

73 3.1 Normalization

74 After loading the solution points matrices from each patient, we need to nor-
 75 malize the data since the reaction fluxes have different boundaries. Using a
 76 standard scaler, we standardize the reaction fluxes by dividing each value by
 77 the standard deviation (scaling to unit variance) and subtracting the mean (cen-
 78 tering the distribution around 0). We then concatenate the three matrices of
 79 each patient and normalize them using the standard scaler. This process results
 80 in a normalized matrix for each patient, such as the one shown in Figure 2
 81 (Normalized matrix of a patient), which has 3006 reaction fluxes as rows and
 82 18036 solution points (max, mean, and min) as columns.

83 3.2 Impact of the variance of the healthy patients

84 To eliminate the variability within the control group, we compute the ratio of the
 85 trauma patients' values against the minimum, mean, and maximum values of
 86 the healthy individuals. This approach results in three solution points matrices
 87 for each patient. Performing a PCA on the reaction fluxes reveals that the

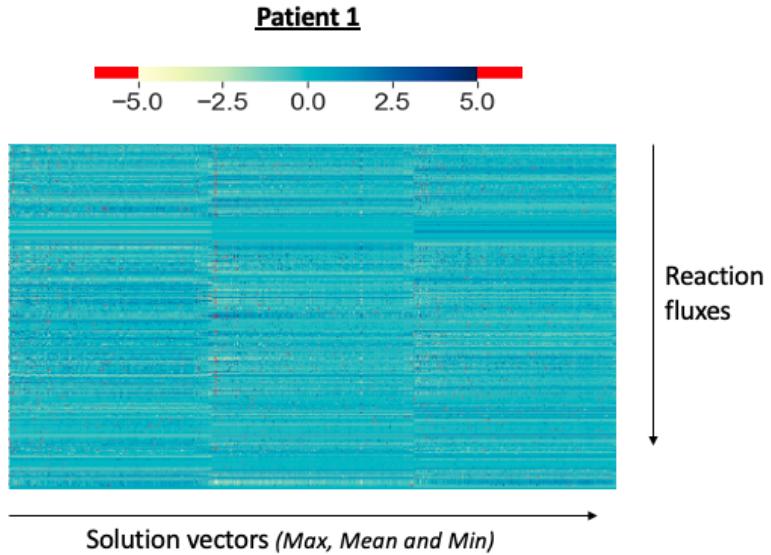


Figure 3: Normalized matrix of a patient

88 minimum, mean, and maximum models form three distinct groups for every
 89 patient in the cohort, as shown in Figure 4. This indicates that all three models
 90 are essential to account for the variability within the control group.

91 3.3 Singular value decomposition (SVD)

92 The solution points are intended to define the solution space of the reaction
 93 fluxes. However, due to sampling, some points may be highly correlated with
 94 others. Singular value decomposition (SVD) helps summarize these solution
 95 points into components that explain most of the variance. For the average
 96 of the 95 patients, 350 SVD components account for more than 95% of the
 97 variance. Consequently, we obtain a reduced matrix of 3006 reaction fluxes by
 98 350 SVD components for each patient (Figure 5). To compare different patients
 99 and identify patterns, we need to organize our data into a 3-way tensor. We
 100 combine each patient's matrix into a tensor (as shown in Figure 6) with three
 101 dimensions:

- 102 • Patients
- 103 • Reaction fluxes
- 104 • Solution points

105 Originally, since the solution points are randomly distributed, the columns
 106 in the different patient's matrix doesn't explain the same thing. Using SVD,
 107 instead of the solution points, we will have components that are sorted by their
 108 explained variance which means that each patient's matrix has columns sorted
 109 from the component that explained most of the variance to the one that ex-
 110 plained the less. This way the solution points dimension isn't randomly dis-
 111 tributed from a patient to another anymore and we can concatenate all the
 112 matrices in one 3-way tensor.

Patient 73 :

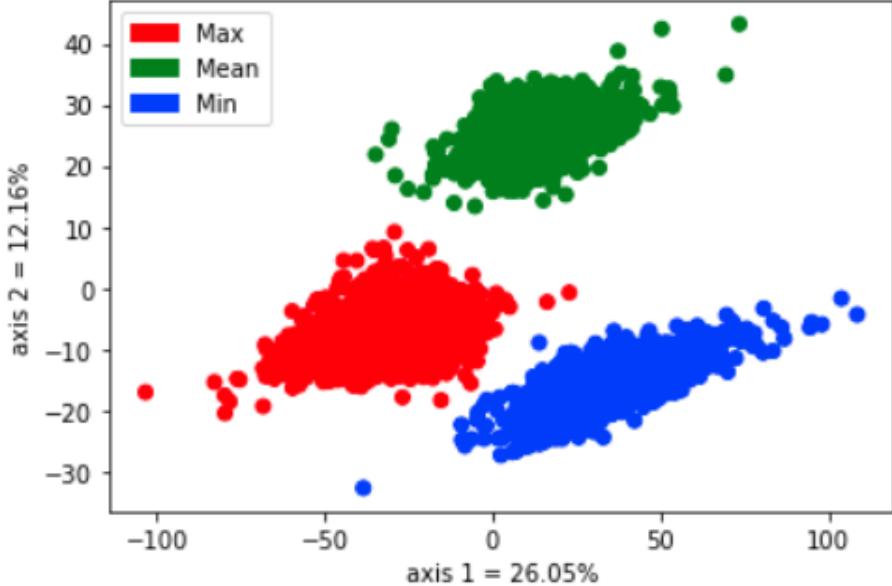


Figure 4: Example of distribution of the solution points (patient 73)

113 3.4 Tensor decomposition

114 Once we have our tensor, we reduce it into multiple components to identify pat-
115 terns (feature extraction) in each dimension. This method has been previously
116 studied on simulated metabolomics data (low dimension) [3] and has shown that
117 we can effectively distinguish different groups of patients using the decomposed
118 vectors. To determine the optimal number of components, we compute the
119 reconstructed tensor and then calculate the percentage difference between the
120 original and reconstructed tensor (Figure 7). We evaluate this reconstruction
121 error on the tensor with 350 SVD components for various numbers of tensor
122 decomposition components, as shown in Figure 8. Our results indicate that
123 approximately 99% of the data is explained by the model when the number
124 of tensor decomposition components matches the number of SVD components
125 (e.g., the model with 350 tensor decomposition components explains 98% of the
126 tensor with 350 SVD components).

127 4 Results

128 4.1 Clustering analysis

129 As shown in Figure 7, the tensor decomposition yields three vectors (represent-
130 ing the dimensions of our tensor) with multiple components. From a tensor
131 decomposition with 350 components, we obtain three vectors, each with 350
132 components. Using this preprocessed data, we can perform a clustering analysis
133 on the patient vectors to identify any correlations among patients. By grouping

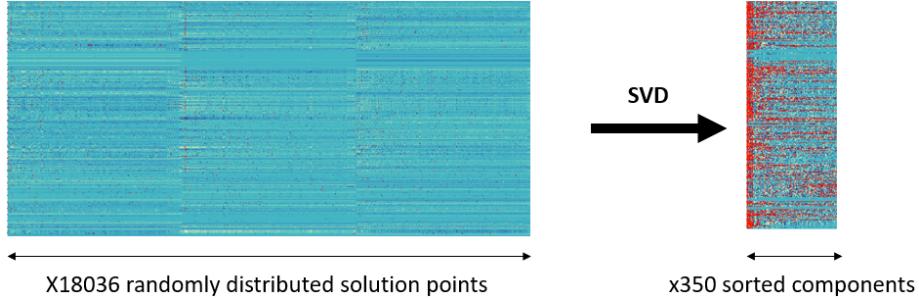


Figure 5: SVD 350 components

¹³⁴ these patients, we can then analyze the reaction fluxes to uncover pathways that
¹³⁵ explain their correlations.

¹³⁶ 4.2 Compute the number of clusters

¹³⁷ Using the K-means clustering method, we computed the SSE (Figure 9) and
¹³⁸ identified an optimal number of clusters at 3 (elbow point). The silhouette curve
¹³⁹ (Figure 9) also indicates that the highest similarity within each cluster occurs
¹⁴⁰ at 3 clusters. However, this optimal number of clusters does not align with the
¹⁴¹ original number of metabolic groups (4), suggesting that our distribution does
¹⁴² not accurately represent the original groups.

¹⁴³ 4.3 Compare computed clusters with the original metabolic ¹⁴⁴ groups

¹⁴⁵ The original clinical data contained 4 clusters (metabolic groups). When we
¹⁴⁶ compare them to the distribution of our patient vectors on 2 components us-
¹⁴⁷ ing PCA for visualization (Figure 10 – a), we see that they appear randomly
¹⁴⁸ distributed. To compare the metabolic groups, we need to compute 4 clusters
¹⁴⁹ (instead of 3, which was the optimal number of clusters) and find the permuta-
¹⁵⁰ tion with the highest percentage of identity. With the K-means clusters sorted
¹⁵¹ as [1; 2; 0; 3], we achieve 37.89% identity with the metabolic groups (Figure 10
¹⁵² – b shows the distribution of the computed clusters with this permutation). As
¹⁵³ shown in Figure 10 – (c) Distribution of the clusters, this permutation results
¹⁵⁴ in different distributions for the computed clusters and the metabolic groups.
¹⁵⁵ However, it is homogeneous when we look at the identity within each cluster
¹⁵⁶ (Figure 10 – (d) Patients with identical clusters). From these results, we can
¹⁵⁷ conclude that the identity between the two sets of clusters is random, indicating
¹⁵⁸ no correlation between our distribution of patients from the tensor decomposi-
¹⁵⁹ tion and the metabolic groups. Instead, this distribution is correlated with the
¹⁶⁰ explained variance of the SVD for each patient. In Figure 11 - Visualization
¹⁶¹ of the patients (350 SVD components), the clusters represented are computed
¹⁶² (using K-means) from the list of variances explained by the SVD with 350 com-
¹⁶³ ponents for each patient. The first component of the PCA (x-axis on the plot)
¹⁶⁴ explains more than 80% of the variance, and there is a correlation between the
¹⁶⁵ clusters of variances explained for each patient and this axis. In Figure 12 -
¹⁶⁶ Visualization of the patients (500 SVD components), we observe the same cor-

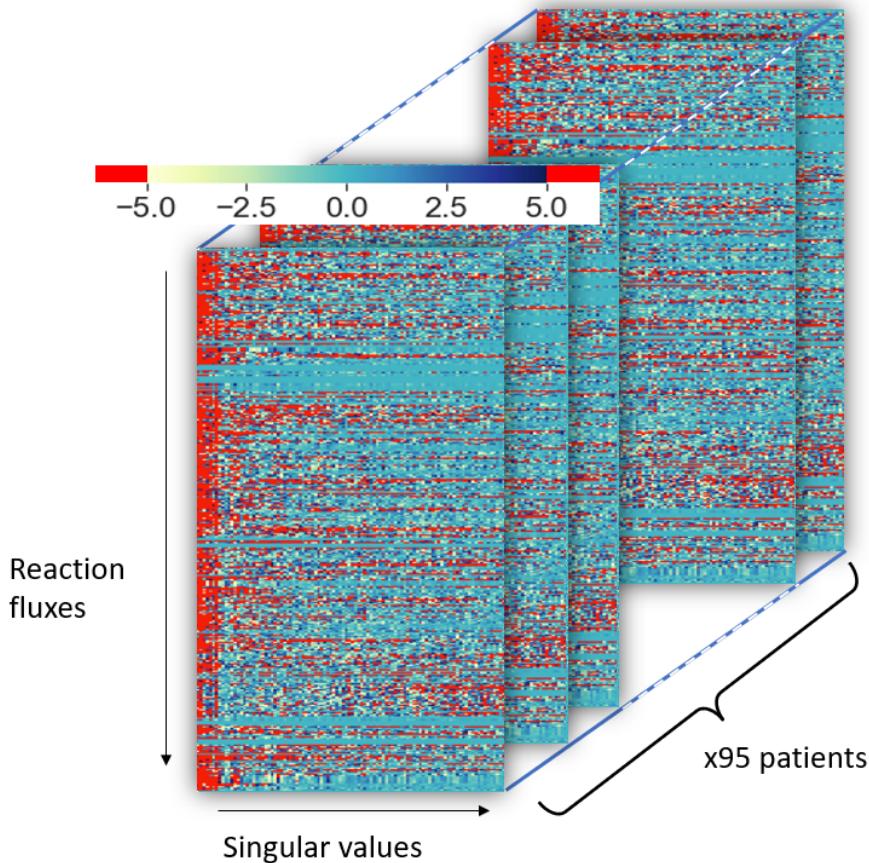


Figure 6: 3 dimensions tensor (patients, reaction fluxes and solution points)

¹⁶⁷ relation with 500 SVD components, which explain on average more than 99%
¹⁶⁸ of the variance for each patient compared to 95

¹⁶⁹ 5 Conclusion

¹⁷⁰ In this study, we utilized a genome-scale metabolic model (GEM) integrated
¹⁷¹ with flux balance analysis (FBA) to analyze the metabolic flux profiles of
¹⁷² 95 trauma patients. By adjusting the baseline model with patient-specific
¹⁷³ metabolic data, we generated a comprehensive set of patient-specific models.
¹⁷⁴ The sampled metabolic flux profile of the patients were normalized and reduced
¹⁷⁵ using singular value decomposition (SVD) to facilitate pattern recognition and
¹⁷⁶ clustering analysis. Our analysis revealed that the variability within the con-
¹⁷⁷ trol group necessitated the use of three distinct models (minimum, mean, and
¹⁷⁸ maximum) for each patient. This approach ensured a robust representation of
¹⁷⁹ the metabolic flux profiles. The tensor decomposition and subsequent clustering
¹⁸⁰ analysis identified three optimal clusters, although this did not align with the

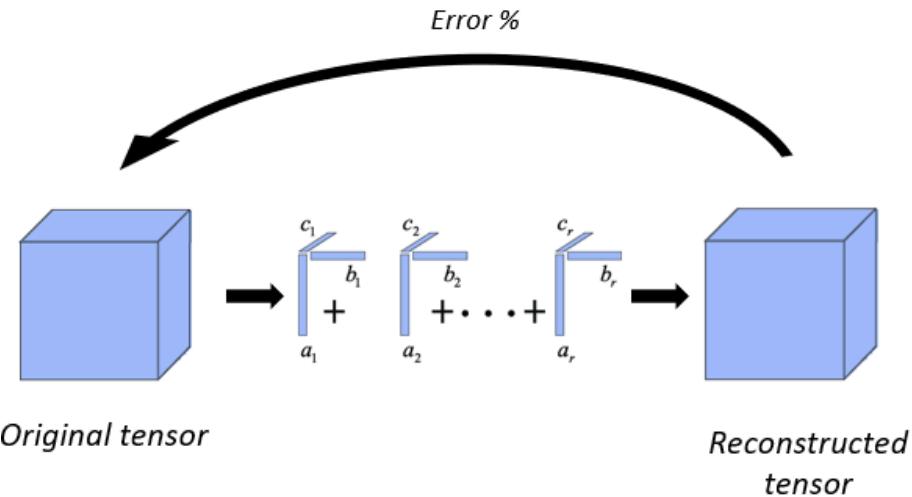


Figure 7: Reconstruction error

181 original four metabolic groups identified in clinical data. This discrepancy sug-
 182 gests that the metabolic profiles derived from the GEM and FBA approach may
 183 capture different aspects of patient variability compared to traditional clinical
 184 classifications. Furthermore, the clustering analysis indicated that the distribu-
 185 tion of patients was more closely correlated with the explained variance of the
 186 SVD components rather than the original metabolic groups. This finding under-
 187 scores the importance of considering the underlying data structure and variance
 188 when interpreting clustering results. Overall, our study demonstrates the po-
 189 tential of combining GEM, FBA, and advanced multivariate analysis techniques
 190 to uncover metabolic patterns in trauma patients. These insights could inform
 191 patient stratification and the identification of therapeutic targets, ultimately
 192 contributing to improved clinical outcomes.

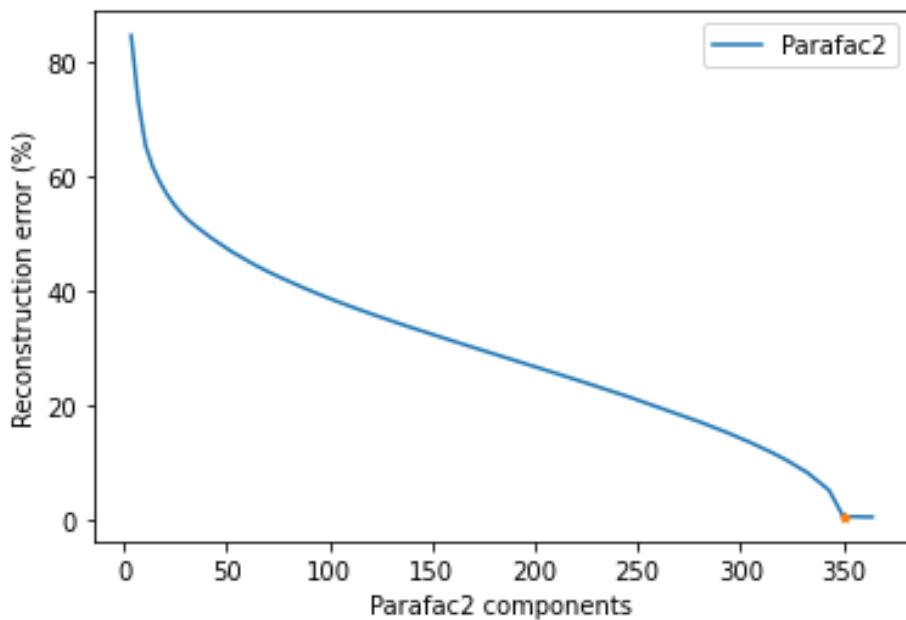


Figure 8: Find the optimal number of tensor decomposition components

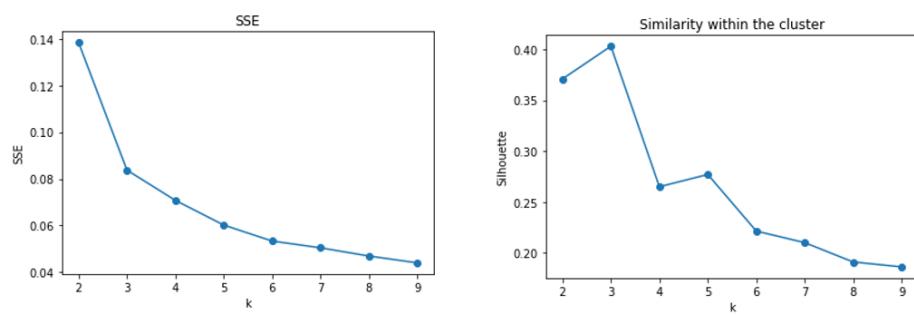


Figure 9: Kmean optimal number of clusters

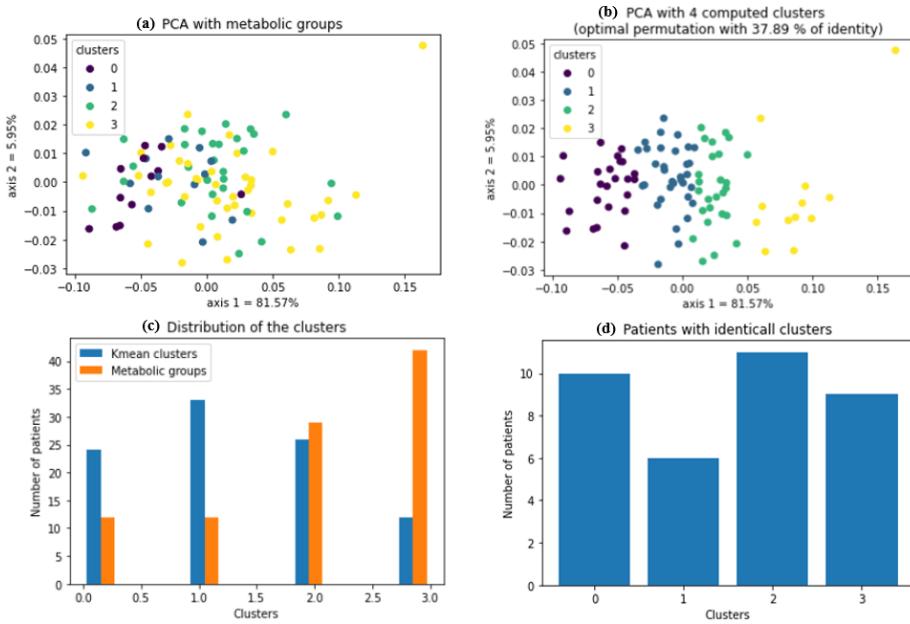


Figure 10: Distribution of the 95 patients

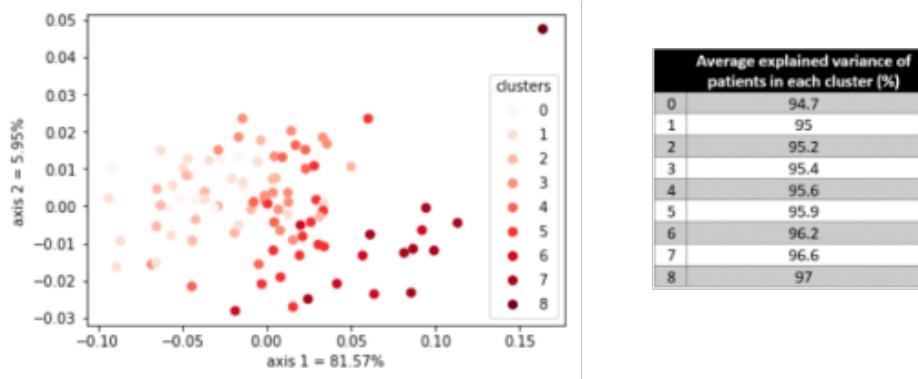


Figure 11: Visualization of the patients (350 SVD components)

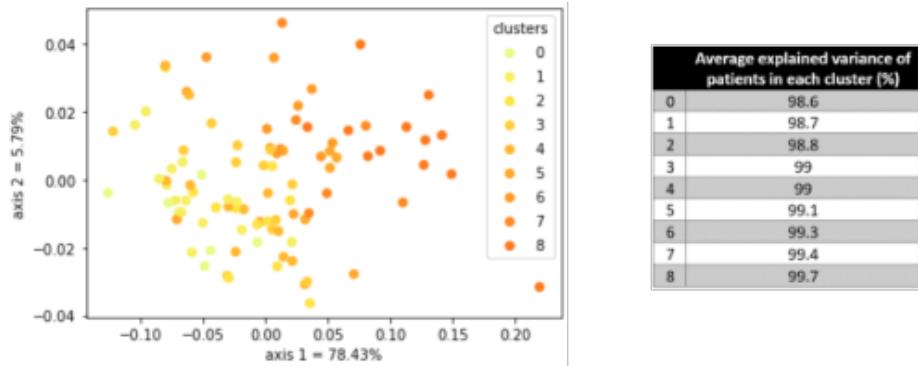


Figure 12: Visualization of the patients (500 SVD components)