

# b-move: Faster Lossless Approximate Pattern Matching in a Run-Length Compressed Index

## Additional File

**Lore Depuydt** ✉ 

Corresponding author  
Ghent University - imec, Technologiepark 126, 9052 Ghent, Belgium

**Luca Renders** ✉ 

Ghent University - imec, Technologiepark 126, 9052 Ghent, Belgium

**Simon Van de Vyver** ✉ 

Ghent University, Technologiepark 126, 9052 Ghent, Belgium

**Lennart Veys** ✉

Ghent University, Technologiepark 126, 9052 Ghent, Belgium

**Travis Gagie** ✉ 

Dalhousie University, 6050 University Avenue, PO BOX 15000, Halifax, NS B3H 4R2, Canada

**Jan Fostier** ✉ 

Corresponding author  
Ghent University - imec, Technologiepark 126, 9052 Ghent, Belgium

■ **Table S1** Example index for reverse search text  $T^{\text{rev}} = \text{"\$CTGGTTGTATACTGTATC"}$  with BWT run details.

| $i$ | $T^{\text{rev}}$ | $\text{SA}^{\text{rev}}$ | $\text{BWT}^{\text{rev}}$ | $\text{LF}^{\text{rev}}$ | $T^{\text{rev}}_{\text{SA}^{\text{rev}}[i]}$ |
|-----|------------------|--------------------------|---------------------------|--------------------------|----------------------------------------------|
| 0   | \$               | 0                        | C                         | 4                        | \$CTGGTTGTATACTGTATC                         |
| 1   | C                | 11                       | T                         | 11                       | ACTGTATC                                     |
| 2   | T                | 9                        | T                         | 12                       | ATACTGTATC                                   |
| 3   | G                | 16                       | T                         | 13                       | ATC                                          |
| 4   | G                | 18                       | T                         | 14                       | C                                            |
| 5   | T                | 1                        | \$                        | 0                        | CTGGTTGTATACTGTATC                           |
| 6   | T                | 12                       | A                         | 1                        | CTGTATC                                      |
| 7   | G                | 3                        | T                         | 15                       | GGTTGTATACTGTATC                             |
| 8   | T                | 7                        | T                         | 16                       | GTATACTGTATC                                 |
| 9   | A                | 14                       | T                         | 17                       | GTATC                                        |
| 10  | T                | 4                        | G                         | 7                        | GTTGTATACTGTATC                              |
| 11  | A                | 10                       | A                         | 2                        | TACTGTATC                                    |
| 12  | C                | 8                        | G                         | 8                        | TATACTGTATC                                  |
| 13  | T                | 15                       | G                         | 9                        | TATC                                         |
| 14  | G                | 17                       | A                         | 3                        | TC                                           |
| 15  | T                | 2                        | C                         | 5                        | TGGTTGTATACTGTATC                            |
| 16  | A                | 6                        | T                         | 18                       | TGTATACTGTATC                                |
| 17  | T                | 13                       | C                         | 6                        | TGTATC                                       |
| 18  | C                | 5                        | G                         | 10                       | TTGTATACTGTATC                               |

Reverse search text  $T^{\text{rev}} = \text{"\$CTGGTTGTATACTGTATC"}$  with its suffix array  $\text{SA}^{\text{rev}}$ , Burrows-Wheeler transform  $\text{BWT}^{\text{rev}}$ , LF mapping  $\text{LF}^{\text{rev}}$ , and suffixes. BWT runs are delineated by horizontal lines.

■ **Table S2** Overview of the components in the bidirectional r-index and the bidirectional move structure.

| Component                                                                 | Description                                                                                | Memory usage for 3 264 <i>E. coli</i> genomes [MB] |
|---------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|----------------------------------------------------|
| Bidirectional r-index as described in [1]: character extension support    |                                                                                            |                                                    |
| Reg. bv. runs                                                             | Sparse bitvector with $r$ 1-bits indicating run endings in the BWT of $T$                  | 78.56                                              |
| Reg. bv. runs-per-letter                                                  | Division of the runs bitvector into $ \Sigma $ shorter sparse bitvectors per character     | 142.37                                             |
| Reg. run heads                                                            | Characters corresponding to runs in the BWT of $T$                                         | 49.13                                              |
| Rev. bv. runs                                                             | Analogous for $T^{\text{rev}}$                                                             | 78.56                                              |
| Rev. bv. runs-per-letter                                                  | Analogous for $T^{\text{rev}}$                                                             | 142.37                                             |
| Rev. run heads                                                            | Analogous for $T^{\text{rev}}$                                                             | 49.13                                              |
| Total                                                                     | -                                                                                          | 540.13                                             |
| Bidirectional move structure (this paper): character extension support    |                                                                                            |                                                    |
| Reg. move table $M_{\text{LF}}$                                           | Bit-packed LF move table for $T$                                                           | 1 535.97                                           |
| Rev. move table $M_{\text{LF}}^{\text{rev}}$                              | Bit-packed LF move table for $T^{\text{rev}}$                                              | 1 535.95                                           |
| Total                                                                     | -                                                                                          | 3 071.92                                           |
| Bidirectional r-index as described in [1]: $\phi$ and $\phi^{-1}$ support |                                                                                            |                                                    |
| Text to run mappings                                                      | Mappings to link a $\phi/\phi^{-1}$ run index back to its BWT run                          | 797.53                                             |
| $\phi/\phi^{-1}$ run bv.'s                                                | Bitvectors to indicate the $\phi/\phi^{-1}$ runs                                           | 284.60                                             |
| Total                                                                     | -                                                                                          | 1 082.13                                           |
| Bidirectional move structure (this paper): $\phi$ and $\phi^{-1}$ support |                                                                                            |                                                    |
| $\phi$ move table $M_{\phi}$                                              | Bit-packed $\phi$ move table                                                               | 2 146.95                                           |
| $\phi^{-1}$ move table $M_{\phi^{-1}}$                                    | Bit-packed $\phi^{-1}$ move table                                                          | 2 146.64                                           |
| $\phi/\phi^{-1}$ run bv.'s                                                | Bitvectors to indicate the $\phi/\phi^{-1}$ runs, necessary to initiate the locate process | 406.32                                             |
| Total                                                                     | -                                                                                          | 4 699.91                                           |
| Both indexes: toehold update and locate support [1]                       |                                                                                            |                                                    |
| SA samples                                                                | SA and $\text{SA}^{\text{rev}}$ samples for toehold updates                                | 2 008.56                                           |
| PLCP                                                                      | PLCP for locate support                                                                    | 196.99                                             |
| Total                                                                     | -                                                                                          | 2 205.55                                           |

■ **Algorithm S1** Update intervals  $([s, e], R_s, R_e)$  and  $([s^{\text{rev}}, e^{\text{rev}}], R_s^{\text{rev}}, R_e^{\text{rev}})$  corresponding to  $P$ , to intervals  $([s', e'], R_s, R_e)$  and  $([s^{\text{rev}'}, e^{\text{rev}'}], R_s^{\text{rev}'}, R_e^{\text{rev}'})$  that correspond to  $Pc$ .

---

```

1 def addCharToRight( $([s, e], R_s, R_e), ([s^{\text{rev}}, e^{\text{rev}}], R_s^{\text{rev}}, R_e^{\text{rev}}), c$ ):
2    $([s^{\text{rev}'}, e^{\text{rev}'}], R_s^{\text{rev}'}, R_e^{\text{rev}'}) \leftarrow M_{\text{LF}}^{\text{rev}}.\text{addChar}([s^{\text{rev}}, e^{\text{rev}}], R_s^{\text{rev}}, R_e^{\text{rev}}, c)$ 
3   if  $s^{\text{rev}'} = -1$  then
4     return empty intervals
5   if  $e^{\text{rev}'} - s^{\text{rev}'} = e^{\text{rev}} - s^{\text{rev}}$  then
6     return  $([s, e], R_s, R_e), ([s^{\text{rev}'}, e^{\text{rev}'}], R_s^{\text{rev}'}, R_e^{\text{rev}'})$ 
7    $x \leftarrow 0$ 
8   for  $a$  where  $a \prec c$  do
9      $([s^{\text{rev}''}, e^{\text{rev}''}], R_s^{\text{rev}''}, R_e^{\text{rev}''}) \leftarrow M_{\text{LF}}^{\text{rev}}.\text{addChar}([s^{\text{rev}}, e^{\text{rev}}], R_s^{\text{rev}}, R_e^{\text{rev}}, a)$ 
10    if  $s^{\text{rev}''} \neq -1$  then
11       $x \leftarrow x + e^{\text{rev}''} - s^{\text{rev}''} + 1$ 
12   $s' \leftarrow s + x$ 
13   $e' \leftarrow s + x + (e^{\text{rev}'} - s^{\text{rev}'})$ 
14  return  $([s', e'], R_s, R_e), ([s^{\text{rev}'}, e^{\text{rev}'}], R_s^{\text{rev}'}, R_e^{\text{rev}'})$ 

```

---

## References

- 1 Yuma Arakawa, Gonzalo Navarro, and Kunihiko Sadakane. Bi-Directional r-Indexes. In *33rd Annual Symposium on Combinatorial Pattern Matching (CPM 2022)*, volume 223 of *Leibniz International Proceedings in Informatics (LIPIcs)*, pages 11:1–11:14, Dagstuhl, Germany, 2022. Schloss Dagstuhl – Leibniz-Zentrum für Informatik. doi:10.4230/LIPIcs.CPM.2022.11.