

Coincidence detection between apical and basal dendrites drives STDP in cerebellar Golgi cells

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Supplementary Information

List of abbreviations:

Ca²⁺, calcium;

LTP, long-term potentiation;

LTD, long-term depression;

mf, mossy fiber.

GrCs, granule cells;

GoCs, Golgi cells;

pf, parallel fiber;

aa, ascending axon;

EPSC, excitatory post-synaptic current;

EPSP, excitatory post-synaptic potential;

STDP, spike-timing dependent plasticity;

GL, granular layer.

Supplementary note 1.

Modeling of long-term synaptic plasticity

Plasticity was modeled following the approach described in ¹, and ². The equations used below have been adapted mainly from ¹. According to the Ca²⁺ control hypothesis ³, synaptic plasticity is a non-linear [BCM-shaped] function of the activity-dependent rise in postsynaptic Ca²⁺ concentration: large Ca²⁺ transient should lead to LTP, while a moderate increase in Ca²⁺ concentration determines LTD. When the Ca²⁺ concentration change is negligible or null, no synaptic plasticity of any kind takes place. The computational model proposed by Shouval and Bear ¹ for the hippocampus has been adapted to the mf - GrC synapse as follows.

The Ω function

The Ω function expresses the relation between Ca^{2+} concentration and changes in synaptic weight (W).

$$\Omega = 0.5 + \text{sig}(\text{Ca} - \alpha_2, \beta_2) - 0.5 \text{sig}(\text{Ca} - \alpha_1, \beta_1)$$

Where *sig* is a sigmoidal function defined as:

$$\text{sig}(x, \beta) = \exp(\beta x) / (1 + \exp(\beta x))$$

with $\alpha_1 = 0.25$, $\alpha_2 = 0.77$, $\beta_1 = 80$ and $\beta_2 = 80$. These values allowed to fit the plasticity model to existing experimental data ⁴.

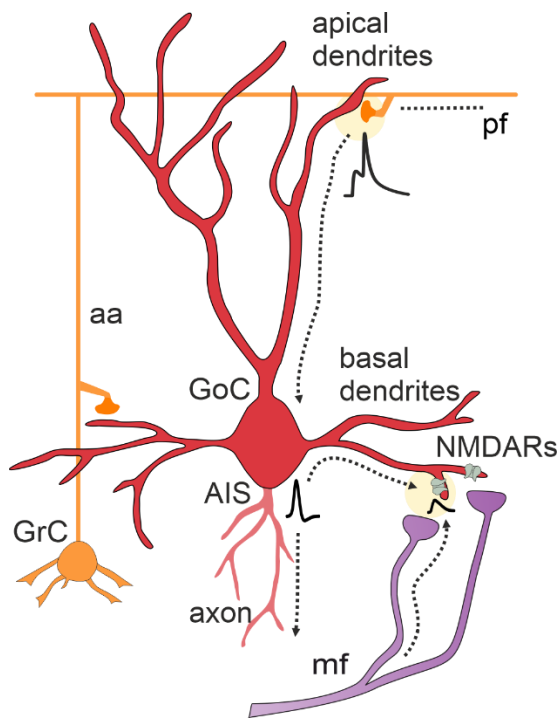
The η function

The η function represents the calcium-dependent learning rate and is inversely related to the learning time constant τ such that $\eta = 1/\tau$, with:

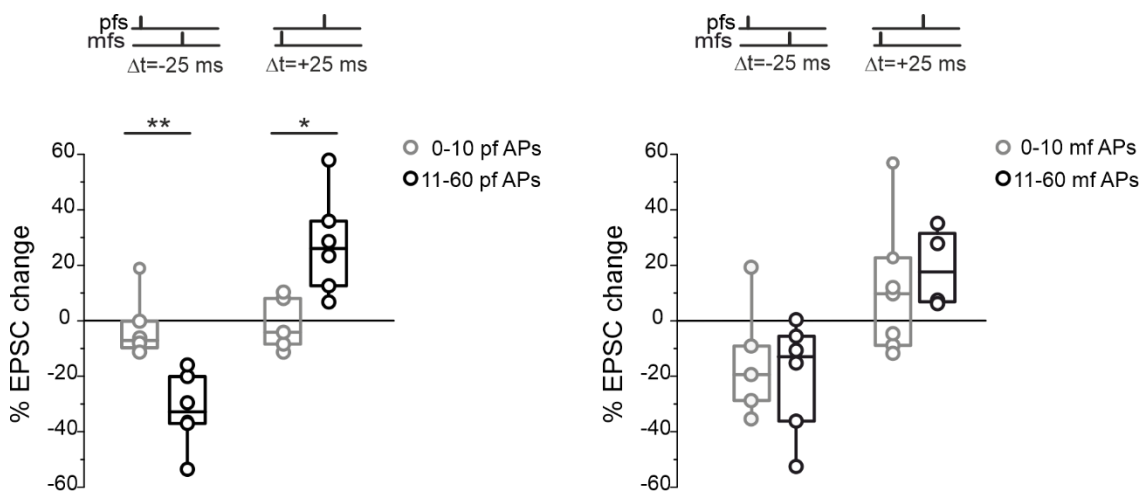
$$\tau = \frac{P_1}{P_2 + (\text{Ca})^{P_3}} + P_4$$

The values of parameters have been taken from ²: $P_1 = 100$ ms, $P_2 = 0.002$, $P_3 = 4$, $P_4 = 1000$ msec.

Supplementary Tables and Figures

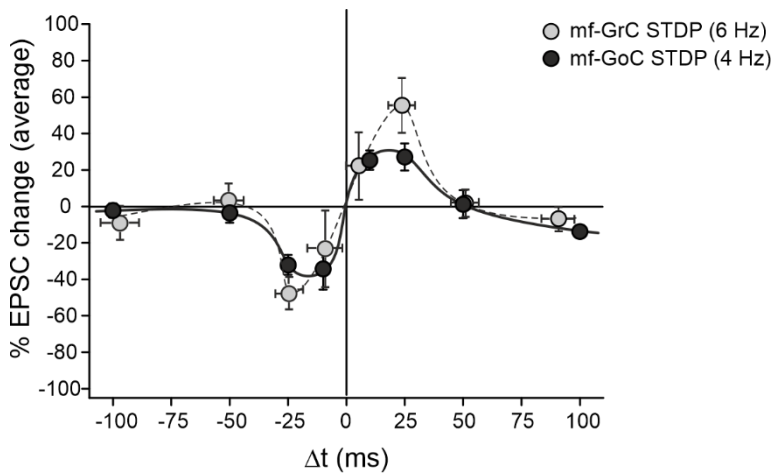


Supplementary Figure 1. Schematic representation of a GoC. Enlargement of the GoC microcircuit, illustrating the afferent excitatory inputs from pfs/aas and mfs onto apical and basal dendrites, respectively, and the process of dendritic integration revealed by previous experimental and modelling works ⁵.



Supplementary Figure 2. STDP requires the action potential elicited by parallel fiber stimulation.

Box-and-whisker plots show the changes in EPSC amplitude based on the number of APs evoked by pf stimulation (left; ≤ 10 out of 60 stimuli, gray circles; > 10 out of 60 stimuli, black circles) or by mf stimulation (right; ≤ 10 out of 60 stimuli, gray circles; > 10 out of 60 stimuli, black circles) during STDP induction. *, $p < 0.05$, **, $p < 0.01$, ***, $p < 0.001$; Student's unpaired t -test.



Supplementary Figure 3. STDP in the GL. mf-GoC STDP timing curve obtained following pf-EPSP \rightarrow mf-EPSP and mf-EPSP \rightarrow pf-EPSP pairing ($\Delta t = \pm 25$ ms; black circles) compared with that obtained from ⁶ (gray circles). Data in the plot indicates mean \pm SEM.

Supplementary References

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