

Formula 1:

$$S(t) = P(t > T) = 1 - F(t) \quad (1)$$

where:

T – duration time,

$F(T)$ – cumulative distribution function of random variable T .

Formula 2:

$$\hat{S}(t_i) = \prod_{j=1}^i \left(1 - \frac{d_j}{n_j}\right) \text{ dla } i = 1, 2, \dots, k, \quad (2)$$

where:

t_i – the point in time when at least one event occurred, $t_1 < t_2 < \dots < t_k, t_0 = 0$,

d_i – number of events in time t_i ,

n_i – number of units observed in time t_i , $n_i = n_{i-1} - d_{i-1} - z_{i-1}$,

z_i – number of censored observations in time t_i .

To compare the duration of the phenomena, the significance of differences between the two survival curves is tested. We then verify the null hypothesis $H_0: S_1(t) = S_2(t)$. Depending on the research problem, we can consider one of the following alternative hypotheses: $H_1: S_1(t) \neq S_2(t)$, $H_1: S_1(t) > S_2(t)$ or $H_1: S_1(t) < S_2(t)$.

Formula 3:

$$h(t) = \lim_{\Delta t \rightarrow 0} \frac{P(t \leq T < t + \Delta t | T \geq t)}{\Delta t} \quad (3)$$

Formula 4:

$$\hat{h}_j = \frac{d_j}{n_j \tau_j} \text{ dla } j = 1, 2, \dots, k \quad (4)$$

where:

d_j – number of events in the j -th time interval,

n_j – the number of units observed in the j -th time interval,

τ_j – the length of j -th time interval.

Formula 5:

$$h(t: x_1, x_2, \dots, x_n) = h_0(t) \exp(a_1 x_1 + a_2 x_2 + \dots + a_n x_n) \quad (5)$$

where:

$x_1, x_2, \dots, x_n$ – independent variables,
 $h_0(t)$ – base hazard or zero hazard line,
 $a_1, a_2, \dots, a_n$ – model coefficients,
 t – observation period.

Formula 6:

$$\text{logit}(p) = \ln\left(\frac{p}{1-p}\right) = \beta_0 + \sum_{i=1}^n \beta_i x_i \quad (6)$$

where:

$p = P(Y = 1 | x_1, x_2, \dots, x_n)$ – conditional probability of occurrence of an event,
 $x_1, x_2, \dots, x_n$ – independent variables,
 $\beta_1, \beta_2, \dots, \beta_n$ – model coefficients.

The coefficients of the logit model allow to determine the chance (odds/risk) of an event occurring at moment t in the selected group in relation to the reference group. Relative risk is determined by the formula $OR = \exp(\beta_j)$.