

## Supplementary Information

### **Role of noncollinear spin texture driven z-torque in deterministic spin-orbit torque induced switching of perpendicular magnetization**

Suhyeok An<sup>1</sup>, Hyeong-Joo Seo<sup>1,†</sup>, Dongryul Kim<sup>1</sup>, Ki-Seung Lee<sup>2</sup>, Eunchong Baek<sup>1</sup>, Jun-Su Kim<sup>1</sup>, Soobeom Lee<sup>3</sup>, Chun-Yeol You<sup>1,\*</sup>

<sup>1</sup> Department of Physics and Chemistry, DGIST, Daegu 42988, South Korea

<sup>2</sup> Emerging Materials Science Research Center, DGIST, Daegu 42988, South Korea

<sup>3</sup> Center for Basic Science, DGIST, Daegu 42988, South Korea

\* Correspondence to [cyyou@dgist.ac.kr](mailto:cyyou@dgist.ac.kr)

† Present address: Department of Materials Science and Engineering, KAIST, Daejeon 34141, South Korea

#### **Contents**

Note I. System energy evaluation depending on the type of chirality of noncollinear spin texture.

Note II. Position dependent magnetization angle distribution and torque calculation.

Note III. Evaluation of perpendicular magnetic anisotropy field varied from helium ion irradiation.

*Note I. System energy evaluation depending on the type of chirality of noncollinear spin texture.*

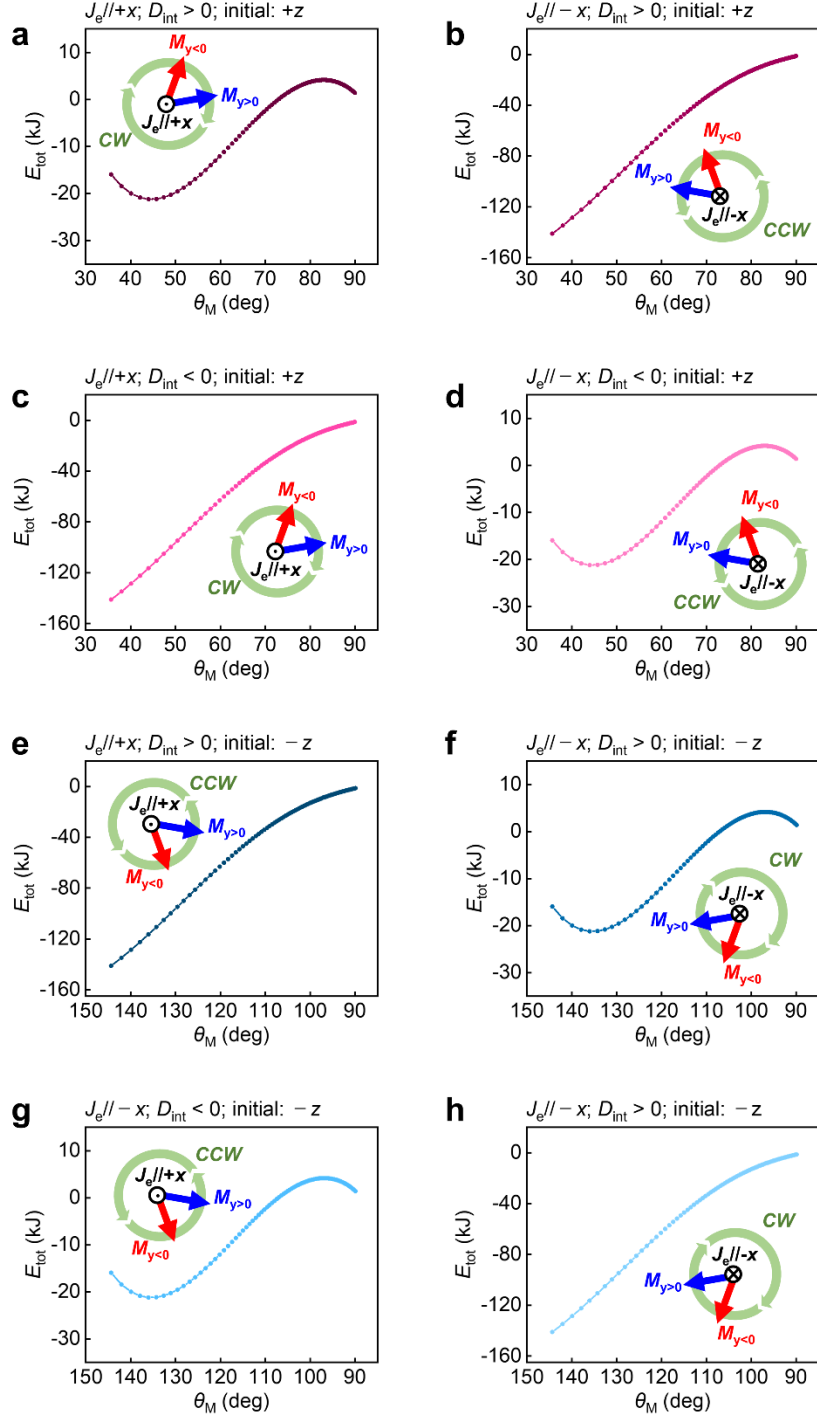


Fig. S1.  $E_{\text{tot}}$  calculations according to initialization,  $J_e$  direction, and sign of  $D_{\text{int}}$  at **a,b,c,d**  $+z$  initialization and **e,f,g,h**  $-z$  initialization case. **a,c,e,g**  $J_e // +x$  and **b,d,f,h**  $J_e // -x$ . **a,b,e,f**  $D_{\text{int}} > 0$  and **c,d,g,h**  $D_{\text{int}} < 0$ . In the whole figure, the schematic diagram of magnetization appears, and the chirality of spin texture is determined based on the spatial variation of magnetization distribution from  $-y$  to  $+y$  position.

The correlation between the chiral type of noncollinear spin texture (NST) and the sign of interfacial Dzyaloshinskii-Moriya interaction (DMI) energy density ( $D_{\text{int}}$ ) plays a critical role in torque generation. In this context, the chiral type of NST is determined by the magnetization ( $M$ ) initialization direction and the electric current ( $J_e$ ) direction, while the sign of  $D_{\text{int}}$  is an intrinsic property established when the system is formed. We will define the chiral type considering all possible initialization and  $J_e$  directions and examine its correlation between the  $D_{\text{int}}$  sign and torque generation.

Suppose there exists lateral direction perpendicular magnetic anisotropy (PMA) symmetry breaking within the system. In this case, spin-orbit torque (SOT) injection can lead to the formation of NST. To make it easier to understand, we will use the notation  $(+z, +x)$  to represent the ( $M$  initialization direction,  $J_e$  direction). Fig. S1 illustrates the different chiral types, where  $(+z, +x)$  and  $(-z, -x)$  have the same chirality, while  $(+z, -x)$  and  $(-z, +x)$  have the same chirality but opposite direction with  $(+z, +x)$  and  $(-z, -x)$ .

The reason for opposite chiral types of NST can be understood through schematic diagrams within each figure. In the case of  $+z$  initialization, where NST has  $0 < M \leq 90$ ,  $M$  in  $y < 0$  has higher PMA energy density, causing it to tilt less comparing with  $M$  in  $y > 0$ . When  $J_e$  is directed along  $+x$ , SOT aligns  $M$  in the  $+y$  direction, resulting in clockwise (CW) chirality. Conversely, when  $J_e$  is directed along  $-x$ ,  $M$  aligns in the  $-y$  direction, leading to counter-clockwise (CCW) chirality. However, for  $-z$  initialization, the situation is entirely reversed. Here, NST has  $90 \leq M < 180$ , which results in CCW chirality when  $J_e$  is directed along  $+x$  and CW chirality when  $J_e$  is directed along  $-x$ . Therefore,  $(+z, +x)$  and  $(-z, -x)$  exhibit the same chiral type, as do  $(+z, -x)$  and  $(-z, +x)$ .

However, it's essential to note that while NST have the same chiral type, what actually determines the system energy and torque is the interaction between DMI and NST. Even when systems exhibit the same chiral type as like Fig. S1a and Fig. S1c, a change in the sign of  $D_{\text{int}}$  results in the opposite energy change. This is similar to the change resulting from the difference in the chiral type of NST when  $D_{\text{int}}$  remains the same, Fig. S1a and Fig. S1b. It is because the sign of  $D_{\text{int}}$  determines the preferred chiral type of NST, resulting in different energy forms and torque distributions although the chirality of NST

is same.[S1] It confirms that the chiral type of NST and the sign of  $D_{\text{int}}$  determine the system's torque direction, even when the initialization direction is reversed as seen in the comparison between Fig. S1e vs Fig. S1f and Fig. S1e vs Fig. S1g.

## II. Position dependent magnetization angle distribution and torque calculation.

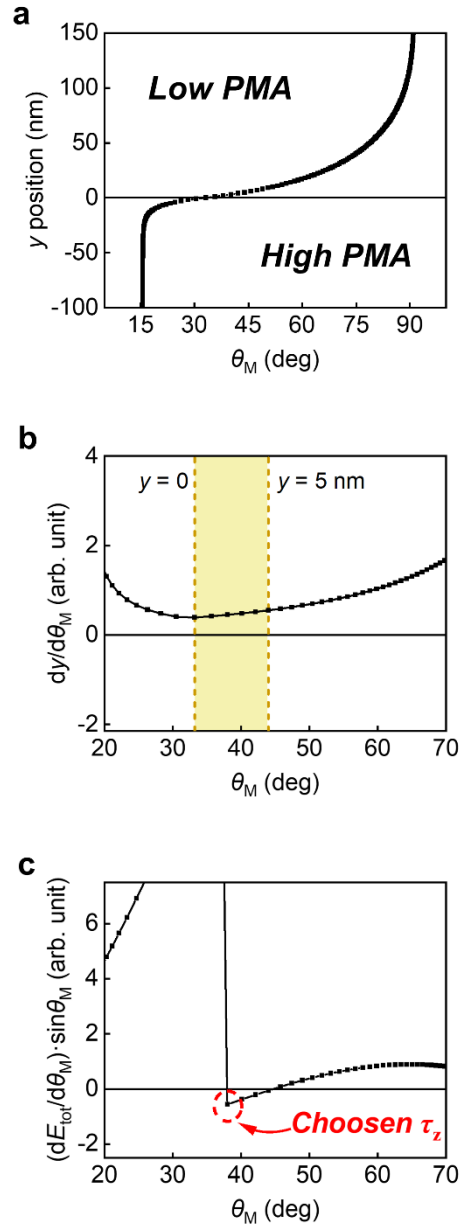


Fig. S2. **a** Graph about  $y$  position versus  $\theta_M$ . **b** Calculated 1st derivative of  $y$  position about  $\theta_M$ . Here, the yellow region indicates the range of negative slope in inset figure of Fig. 4a of main text and each dashed line is case of  $y = 0$  and 5 nm, respectively. **c** Calculated  $z$  directional torque component ( $\tau_z$ ). The dashed circle indicates the example of determined  $\tau_z$  for its tendency analysis in Fig. 5 of main text.

In Fig. 4 of the main text, we conducted  $y$  position dependent derivatives of  $E_{\text{tot}}$  to examine its relationship with spatial  $\tau_z$  distribution. However, for actual torque calculations, we require angular derivatives of  $E_{\text{tot}}$ . And it is reason that we prepared this Note II. Fig. S2a illustrates the relationship between  $y$  position and  $\theta_M$ . This relationship can be directly understood from Fig. 3d in the main text using the expression  $m_z = \cos \theta_M$ . As observed in the results, the high PMA region ( $y < 0$ ) has a smaller degree of tilting compared to the low PMA region ( $y > 0$ ). When you take the first derivative of this graph with respect to  $\theta_M$ , the results indicate that the change in magnetization is primarily prominent in the regions where the change is abrupt, as shown in Fig. S2b, and all values are positive.

Therefore, based on the relationship of  $dE_{\text{tot}}/d\theta_M = (dE_{\text{tot}}/dy) \cdot (dy/d\theta_M)$ , we can speculate that the sign of the torque is determined solely by  $dE_{\text{tot}}/dy$ , and  $dy/d\theta_M$  only affects its magnitude on torque. Thus, explanation of the sign of torque using only the spatial distribution as in Fig. 4 of the main text has no issue. Furthermore, we calculated  $\tau_z$  by multiplying  $\sin\theta_M$  with  $dE_{\text{tot}}/d\theta_M$  to examine only the  $z$  component, as shown in Fig. S2c. Consequently, the calculated  $\tau_z$  follows the sign trend determined by  $dE_{\text{tot}}/dy$  also. Here, we selected the  $\tau_z$  with the most abrupt change for the analysis in Fig. 5 of the main text.

### III. Evaluation of perpendicular magnetic anisotropy field varied from helium ion irradiation.

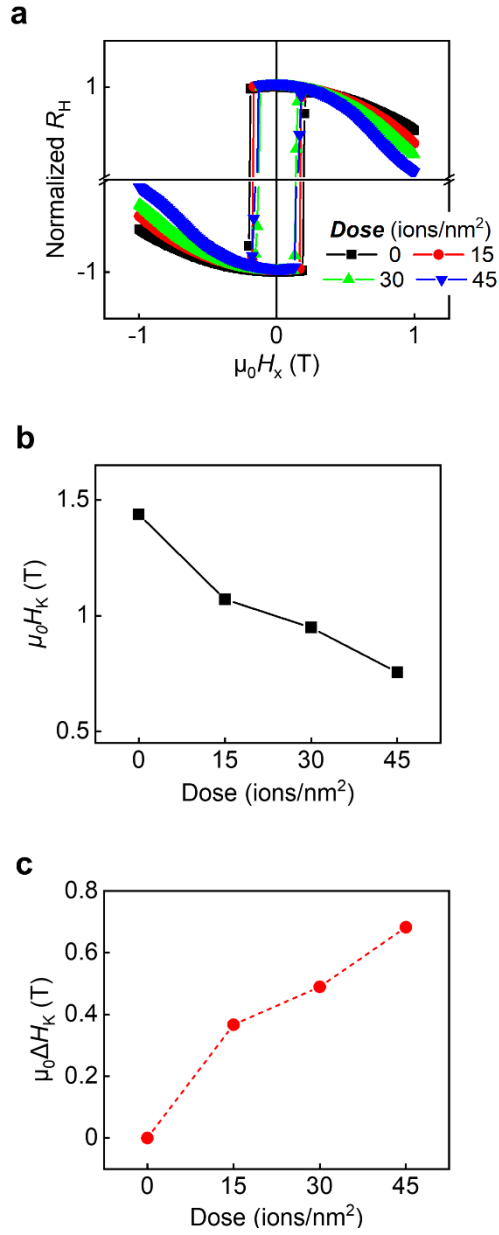


Fig. S3. Analysis of anisotropy characteristics by HII process. **a** AHE hysteresis loop under in-plane directional magnetic field according to dose. **b** Extracted  $H_K$  using GST method and **c** calculated  $\Delta H_K$ .

Here  $\Delta H_K$  can be calculated by  $\Delta H_K \equiv H_K^{NI} - H_K^I$  and  $H_K^{NI}$  is fixed to  $H_K$  at dose = 0 ions/nm<sup>2</sup>.

The helium ion irradiation (HII) process can change magnetic properties such as the anisotropy properties,[S2-S4] exchange bias between FM/antiferromagnet interface,[S5-S7] DMI,[S8,S9] motion of domain wall (DW),[S10,S17] SOT properties,[S12-S15] and skyrmion manipulation.[S16,S17]. Among various changes observed in the experiment, we focus on PMA and DMI variations. But there was some reports that DMI is less sensitive to changes within an appropriate dose range compared to changes in [S8,S14,S16]. Therefore, the study ignored variations in DMI and instead focused on changes in PMA energy due to HII using the general Sucksmith-Thompson (GST) method for anisotropy analysis.[S18] For GST measurements, the anomalous Hall effect (AHE) hysteresis loop is requisite as shown in Fig. S3a with respect to the in-plane directional magnetic field. Measured hysteresis loop is able to fit with GST equation and Fig. S3b presents the results of extracting the effective anisotropy field ( $H_K$ ). In here, we should mention that the measured  $H_K$  is effective anisotropy field considering the demagnetization contribution also. As observed, with increasing the degree of ion irradiation, denoted as dose, the anisotropy decreases significantly, with values of  $\mu_0 H_K = 1.44, 1.07, 0.95$ , and  $0.76$  T for doses of 0, 15, 30, and 45 ions/nm<sup>2</sup>, respectively. Importantly, the difference in  $H_K$  between the irradiated (I) region and the non-irradiated (NI) region, defined as  $\Delta H_K \equiv H_K^{NI} - H_K^I$ , is noteworthy. The calculated  $\Delta H_K$  is shown in Fig. S3c, and it exhibits an increasing trend with dose. Specifically, at doses of 15, 30, and 45 ions/nm<sup>2</sup>,  $\mu_0 \Delta H_K = 0.4, 0.5$ , and  $0.7$  T, respectively.

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