

## Appendix

### Appendix I. Mathematical definition of demand and shift optimization.

#### Equation 1. Definition of the demand.

Suppose we want to model the demand  $D(d)$  on a particular day( $d$ ) according to the various critical tasks (CTs) that are expected of orthopaedic residents, where  $D \in R, D \geq 0$ . Then, the demand on a particular day( $d$ ) may be defined as:

$$D(d) = O(d) \cdot \bar{t}_O + T(d) \cdot \bar{t}_T + A(d) \cdot \bar{t}_A + C(d) \cdot \bar{t}_C + R$$

, where  $O(d)$  is the number of ORs complete per day,  $T(d)$  is the number of traumas seen per day,  $A(d)$  is the number of admissions per day,  $C(d)$  is the number of consults seen per day, and  $R$  is the baseline amount of time required to round per day. Similarly,  $\bar{t}_O$  is the average amount of time it takes to complete an OR,  $\bar{t}_T$  is the average amount of time it takes to complete a trauma,  $\bar{t}_A$  is the average amount of time it takes to complete an admission, and  $\bar{t}_C$  is the average amount of time it takes to complete a consult.

#### Equation 2. Definition of optimization potential possible.

Suppose  $N_{OS}$  is the total number of shifts of the optimized schedule on an annual basis, where  $n_{OS}(d)$  is the number of residents in the optimized schedule on a particular day  $d$ . Suppose  $C$  is the cut-off on the demand of the residents, where  $C \in R, C \geq 0$ . Then, the number of residents on a particular day can be modeled by:

$$n_{OS}(d) = \begin{cases} 2, & \text{if } D(d) > C \\ 1, & \text{if } D(d) \leq C \end{cases}$$

The total number of shifts of the optimized schedule may be defined by:

$$N_{OS} = \sum_{d=1}^D n_{OS}(d)$$

Accordingly, the annual reduction possible may be defined as:

$$Reduction\ Possible = \frac{N_{HS} - N_{OS}}{N_{HS}} \cdot 100\%$$

, where  $N_{HS}$  is the historic number of residents scheduled, and  $N_{OS}$  is the optimized number of residents scheduled.