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Collision-Aware Coordination of Dual Drilling Manipulators Using RoboCompiler and Control Barrier Functions

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Abstract

Concurrent drilling with two hydraulic booms requires coordinated motion in a confined workspace under actuator limits and intentional tool–rock contact. This paper couples RoboCompiler mechanism models with a centralized control barrier function quadratic program. Independently compiled graphs provide closed-chain kinematics, actuator maps, and reduced dynamics. The program selects actuator commands and reference-progress rates under collision, nominal effort, and flow constraints, reserving clearance for delay, hydraulic response, uncertainty, and stopping travel; a supervisor sequences routing, guarded contact, drilling, and recovery. A twelve-hole MuJoCo mission completed 48.035 m of modeled drilling; in comparison missions, concurrent operation was 42.5% shorter than sequential operation. A 100-collar docking campaign completed 294 of 300 operations across three conditions with no monitored clearance violation and pre-contact feed-extension rates below 20 mm/s; five single-condition ablations assess routing, online filtering, and uncertainty allowances. Isaac Sim checks confirm exported geometry, tree dynamics, and closed-chain static equilibrium.

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28 1. Introduction

29 Automating the manipulators of construction and mining machines can
30 improve the repeatability of tool positioning and reduce the need for operators
31 to remain close to active work areas [1, 2, 3]. Underground drilling is a de-
32 manding case: several long-reach hydraulic booms on one carrier must reach
33 a prescribed hole pattern within a shared, confined workspace. Productive
34 operation requires the booms to move concurrently, position their tools accu-
35 rately, and establish supported contact with the rock before drilling. Earlier
36 work in construction-oriented drilling includes an automated machine concept
37 for tunnelling and underground mining [4] and a rocky-wall consolidation
38 system integrating a drilling rig, a rod-handling manipulator, and automatic
39 rod feeding and recovery [5].

40 Collision avoidance, task coordination, and hydraulic actuation are coupled
41 throughout such a sequence. A boom moving to its next target can obstruct
42 one that is aligning, drilling, or retracting, and its occupied volume depends
43 on the whole mechanism, including cylinders, closed linkages, and telescopic
44 feed stages. A changed command does not take effect immediately: hydraulic
45 response, command delay, and residual plant motion affect both tracking and
46 stopping, so the required clearance must cover the motion that continues
47 during braking [6, 7]. In addition, tool–rock contact is intentional, whereas
48 all other contact remains prohibited. Contact loads also affect drilling perfor-
49 mance. In experiments on robotic concrete drilling, Ortner and Kromoser [8]
50 found that higher feed rates reduced drilling time, although the reduction was
51 not proportional to the increase in drilling forces. This related application
52 motivates considering process loads alongside motion coordination.

53 Prior work on drilling-boom automation has addressed motion planning
54 and collision avoidance. Kivelä et al. [1] combined coordinate control with
55 online reference modification and potential-field-based avoidance, including
56 simultaneous operation of two drilling booms in simulation. Cui et al. [2]
57 addressed a three-arm tunnel drilling robot through hole sequencing, improved
58 potential-field planning, and trajectory smoothing, supported by physical-
59 machine experiments. Xu and Lin [9] combined kinematic error compensation
60 with a sampling-based planner; their planning study moved the middle boom
61 while representing the outer booms as obstacles. These methods select tool
62 targets and generate admissible geometric routes. Coordinated execution also
63 requires both moving booms to be adjusted online when actuator response,
64 available capacity, or contact conditions change along those routes.

For a single drilling boom, pose-parameterized motion planning and measured-state inverse kinematics were combined with self-collision filtering in [10], where control barrier functions (CBFs) constrain joint velocities through a quadratic program (QP) that modifies the nominal positioning command when a self-collision constraint becomes active. Extending this approach to concurrent drilling requires mutual constraints involving both mechanisms, environmental clearance, and coordinated decisions on how quickly each reference advances. For hydraulic booms, these decisions must also reflect the relation between commanded actuator motion, delivered motion, and the distance needed to stop.

Multi-manipulator safety control offers related formulations. Kaypak et al. [11] developed centralized and decentralized high-order CBF formulations for multiple robotic arms, using convex collision geometry together with joint, velocity, and torque bounds, and reported simulation and hardware studies. Wei et al. [12] used differentiable optimization to construct collision constraints for convex primitives and demonstrated torque-level control in manipulation and contact tasks. Palmieri et al. [13] combined hierarchical QP control, CBF constraints, inter-arm avoidance, and admittance in a semi-autonomous agricultural robot, with laboratory and vineyard experiments. Applying these formulations to drilling machinery additionally requires the transmission geometry and response of hydraulic closed-chain mechanisms to enter the coordination problem.

For hydraulic machines, Shen and Sloth [3] incorporated disturbance estimation and input-delay compensation into robust CBF control of an industrial wheel loader. Huang et al. [14] combined kinematic CBF constraints on excavator joint velocities with a disturbance-observer-based adaptive sliding-mode tracking controller, evaluated in simulation. Backup CBF methods provide constructions for preserving safety under bounded inputs by relating admissible states to a specified backup controller [15]. For mechanism modeling, URDF+ [16] and Extended URDF [17] represent closed-chain and coupled mechanisms, and RoboCompiler [18] compiles a mechanism graph into closure equations, motion maps, actuator-transmission maps, and reduced dynamics, so that geometry and effort are evaluated from one mechanical description.

The problem addressed here is the integration of these capabilities for concurrent drilling: geometric constraints evaluated through the closed-chain motion maps, hydraulic limits expressed in the coordinates of the commanded actuators, clearance that covers delayed response and stopping travel, and regulation of both tasks across free motion and pressure-mode drilling. Table 1

103 relates this integration to representative prior work.

Table 1 Scope of representative prior work and the capabilities integrated in the proposed framework.

Study or direction	Established capability	Integration in the proposed framework
Kivelä et al. [1]	Online collision-aware references and simultaneous two-boom drilling in simulation.	Centralized command and progress regulation with explicit hydraulic response, capacity, and stopping constraints.
Drilling planners [2, 9]	Multi-arm task and path planning, geometric collision avoidance, and positioning refinement.	Measured-state safety filtering during concurrent motion and transitions between positioning and drilling.
Single-boom CBF [10]	Pose-based planning and joint-velocity self-collision filtering.	Compiled actuator coordinates, mutual and environmental clearance, and coupled reference progress.
Kaypak et al. [11]	Multi-arm CBF coordination with joint, velocity, and torque bounds.	Hydraulic closed-chain mechanisms, pending commands, and reserves for bounded stopping travel.
Interaction control [12, 13]	Constrained manipulation, contact tasks, and supervisory mode switching.	Guarded drilling contact, support-force checks, pressure-mode flow caps, and feed-sweep clearance.
Hydraulic-machine safety [3, 14]	Disturbance- and delay-aware CBF control on a wheel loader; excavator kinematic CBF control with disturbance-observer-based tracking.	Coupled two-boom geometry and residual-motion allowances during backup stopping.
RoboCompiler [18]	Consistent closed-chain motion, actuation, and reduced-dynamics interfaces.	Connection of independently compiled mechanisms to hydraulic safety filtering and drilling supervision.

104 This paper presents a coordination framework for two mirrored hydraulic
105 drilling booms on a common carrier. RoboCompiler compiles the phys-
106 ical graph of each boom independently and supplies closed-configuration
107 reconstruction, tool and body Jacobians, actuator-effort maps, and reduced
108 dynamics in actuator coordinates, so that the collision model and the tool
109 controller share one mechanism description. A centralized QP selects the
110 commands of the eighteen actuator channels, which are rate references in rate-
111 controlled modes and admissible flow caps in pressure-control modes, together
112 with a reference-progress rate for each boom; either boom can therefore slow,
113 pause, or yield when clearance or hydraulic capacity becomes restrictive. The
114 constraints cover self-, inter-boom, and environmental clearance, actuator
115 limits, nominal hydraulic effort, and the flow budget of each boom. Each
116 clearance constraint reserves distance for estimation and geometry uncertainty,

117 command delay, hydraulic lag, slew-limited braking, and residual plant motion,
 118 and a backup-compatible barrier condition keeps a prescribed slew-limited
 119 stop admissible. A supervisor sequences routing, yielding, guarded approach,
 120 support engagement, pressure-mode drilling, and retreat or recovery, and sets
 121 the permitted contacts and actuator modes of each phase.

122 The main contributions are:

- 123 1. A centralized formulation that regulates the actuator commands and
 124 reference progress of two independently compiled closed-chain hydraulic
 125 booms. Tool tracking, the clearance constraints (mutual, self-, and
 126 environmental), and the nominal effort and flow limits are all expressed
 127 in common actuator coordinates.
- 128 2. A stopping-aware barrier construction that combines pending-command
 129 prediction, hydraulic response, slew-limited braking, residual-motion
 130 memory, and uncertainty allowances in affine QP constraints, and states
 131 the conditions under which a specified backup stop preserves clearance
 132 across controller updates.
- 133 3. Contact supervision that coordinates guarded approach, pressure-mode
 134 drilling, feed-sweep clearance, and recovery with motion, evaluated
 135 in simulation through a twelve-hole drilling mission with controller
 136 comparisons, a 100-collar docking campaign (three conditions for the
 137 full framework and five ablations under one condition), and Isaac Sim
 138 checks of the exported model.

139 2. Application of RoboCompiler to two drilling mechanisms

140 RoboCompiler [18] supplies the mechanical interfaces of each boom to a
 141 centralized, actuator-aware CBF filter (Fig. 1). The previous single-boom
 142 method combined measured-state inverse kinematics with joint-velocity self-
 143 collision filtering [10]; the present filter works in actuator coordinates and
 144 incorporates hydraulic response, command delay, stopping travel, nominal
 145 force/flow constraints, and mutual, self-, and environmental clearance.

146 Each boom has a graph $\mathcal{G}_b = (\mathcal{V}_b, \mathcal{E}_b, \mathcal{A}_b)$, $b \in \{L, R\}$, containing rigid
 147 bodies and inertias, joints and attachment frames, and actuator ports. Cylin-
 148 der bodies and rods close the shoulder and wrist linkages. Telescopic stages
 149 satisfy $d_{bj} = k_j d_{b1} + o_j$, with master stroke d_{b1} , gain k_j , and offset o_j .

150 The right boom reflects the left graph while retaining separate states,

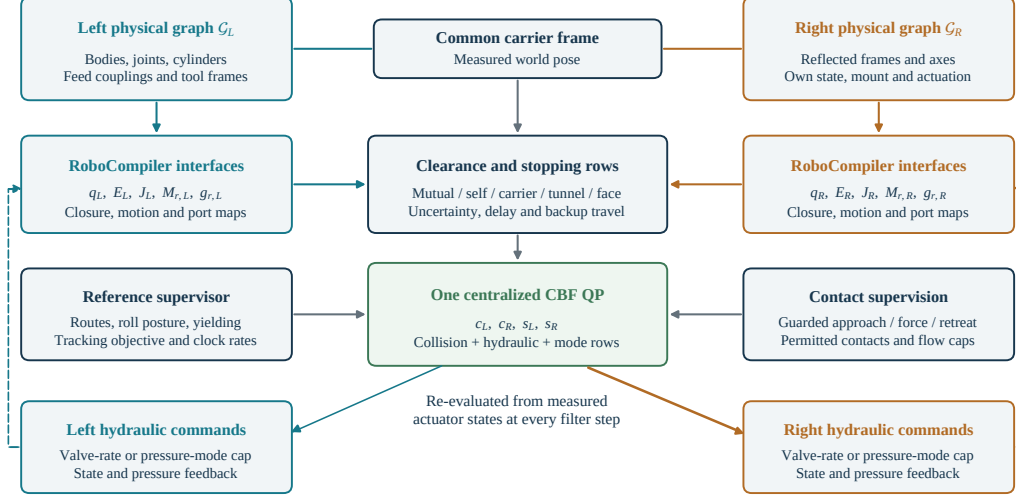


Fig. 1. Coordination architecture. Each physical graph supplies closure, geometry, and dynamics interfaces. A centralized filter selects both actuator commands and reference-progress rates using shared clearance constraints and contact-dependent supervision.

151 mounts, and commands. With $S = \text{diag}(1, -1, 1)$ and $\bar{S} = \text{diag}(S, 1)$,

$$\begin{aligned} T^R &= \bar{S}T^L\bar{S}, & r^R &= Sr^L, & \mathcal{I}^R &= S\mathcal{I}^LS^\top, \\ a_{\text{rev}}^R &= -Sa_{\text{rev}}^L, & a_{\text{pris}}^R &= Sa_{\text{pris}}^L, \end{aligned} \quad (1)$$

152 where T is a joint or named-frame transform, r the center of mass, $\mathcal{I}$ its
 153 inertia, and a a joint axis. Conjugation preserves right-handed frames, and
 154 the revolute-axis sign preserves axial-vector transformation. Reflection retains
 155 connectivity, closure, and actuator conventions. Each graph is compiled inde-
 156 pendently; centralized coordination adds a second nine-coordinate command
 157 block and inter-boom clearance rows. Figure 2 shows the five independent
 158 cycles and two feed-coordinate couplings of each instance.

159 2.1. Closed-chain configuration and motion interfaces

160 The actuator vector $x_b \in \mathbb{R}^9$ comprises swing, lift, zoom, tilt, feed-swing,
 161 roll, bolting, feed-extension, and master-feed coordinates; all are lengths
 162 except roll. Rod spin φ_b is a separate process coordinate with axisymmetric
 163 collision geometry. For augmented configuration q_b and $u_b = (x_b^\top, \varphi_b)^\top$,

$$\Phi_b(q_b) = 0, \quad q_b = \mathcal{Q}_b(u_b), \quad \dot{q}_b = N_b(q_b)\dot{u}_b, \quad (2)$$

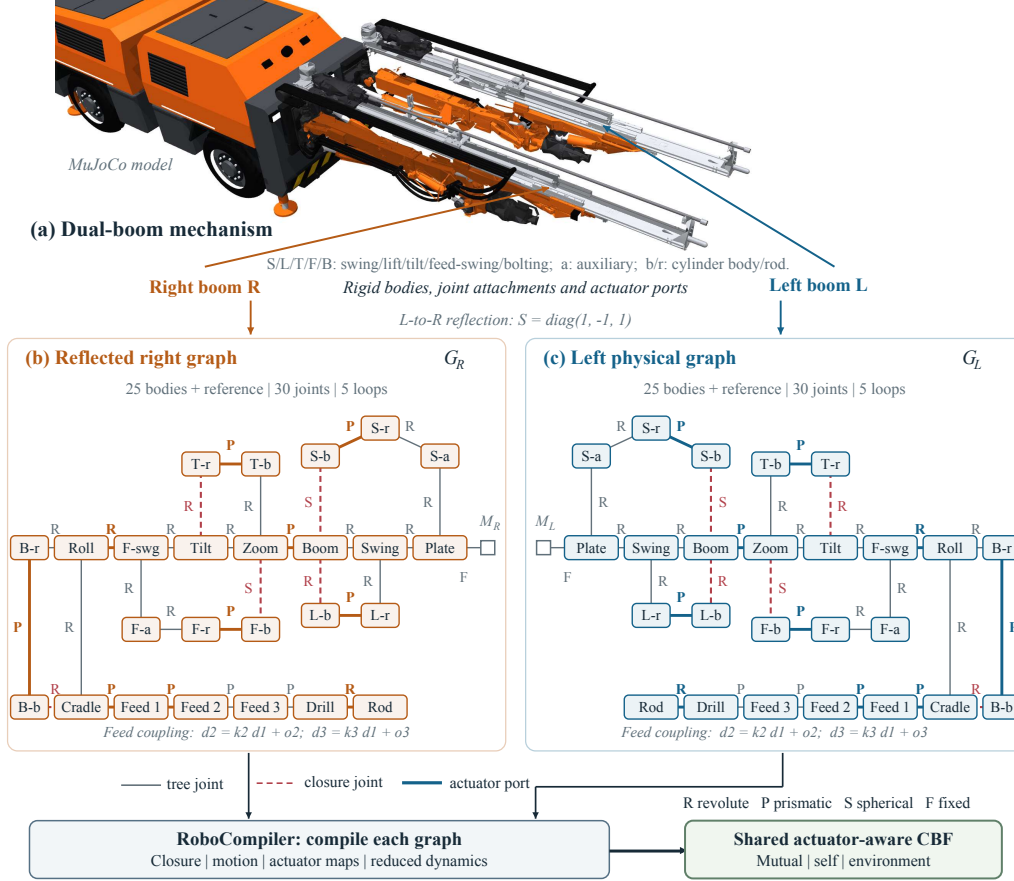


Fig. 2. Dual-boom mechanism and physical graphs. (a) Carrier-mounted mechanisms in MuJoCo. (b,c) Reflected right and left graphs: rounded vertices denote rigid bodies, squares mounting references M_b , solid/dashed edges tree/closure joints, and thick colored edges actuator ports. Each graph has 25 bodies, 30 joints, and five independent cycles; feed couplings are coordinate relations. Separately compiled interfaces enter the centralized CBF filter.

where Φ_b contains loop residuals and $N_b = DQ_b$ satisfies $D\Phi_b N_b = 0$. Its nine x_b columns form E_b . Continuation and closure correction reconstruct dependent coordinates from measured actuator coordinates, subject to the full residual tolerance, the selected assembly branch, and a regular dependent-coordinate Jacobian.

Body j is located in world frame W through carrier frame K and mount M_b :

$${}^W T_{bj} = {}^W T_K {}^K T_{M_b} \tilde{T}_{bj}(Q_b(u_b), \hat{\theta}_b). \quad (3)$$

171 Here ${}^W T_K$ is the measured carrier pose and $\hat{\theta}_b \in \mathbb{R}^3$ an estimated three-axis
 172 orientation correction. The corrected pose $\tilde{T}_{bj}$ applies this rotation to distal
 173 bodies about a specified reference node while preserving proximal poses.
 174 Actuator Jacobians hold the carrier pose and orientation correction fixed
 175 within each control step; geometric error allowances and residual-response
 176 terms cover their unresolved motion.

177 For body-fixed point p , $\dot{p} = J_{p,b}\dot{x}_b$ and $\omega = J_{\omega,b}\dot{x}_b$; hence the drilling axis
 178 satisfies $\dot{a}_b = \omega \times a_b$. Tool regulation and the clearance constraints use these
 179 same Jacobians.

180 2.2. Reduced dynamics and contact-load interfaces

181 With rod spin fixed, $E_{T,b}$ restricts E_b to physical-tree velocities. The
 182 actuator map L_b and contact Jacobian $J_{c,b}$ preserve power:

$$\dot{\ell}_b = L_b \dot{x}_b, \quad \tau_{a,b} = L_b^\top f_b, \quad \tau_{c,b} = J_{c,b}^\top w_b. \quad (4)$$

183 Here ℓ_b is actuator displacement, f_b transmitted force or torque, w_b stacked
 184 external forces or wrenches, and $\tau_{a,b}, \tau_{c,b}$ their reduced efforts. The chosen
 185 coordinates give $L_b = I$. Eliminating internal loop reactions from tree inertia
 186 $M_{T,b}$ and bias $h_{T,b}$ [19] yields

$$\begin{aligned} M_{r,b} &= E_{T,b}^\top M_{T,b} E_{T,b}, & h_{r,b} &= E_{T,b}^\top (h_{T,b} + M_{T,b} \dot{E}_{T,b} \dot{x}_b), \\ M_{r,b} \ddot{x}_b + h_{r,b} &= L_b^\top f_b + J_{c,b}^\top w_b. \end{aligned} \quad (5)$$

187 The derivative $\dot{E}_{T,b}$ follows the closed configuration path; auxiliary closure-
 188 chart coordinates are massless.

189 For positioning, the filter uses inertia frozen at the latest model update
 190 and gravity bias $g_{r,b} = h_{r,b}(x_b, 0)$. The orientation correction used in Eq. (3)
 191 is supplied by a prescribed load-dependent geometry map:

$$\hat{\theta}_b = \Psi_b(x_b, w_b). \quad (6)$$

192 For the measured carrier pose, Ψ_b returns the three-axis correction from actu-
 193 ator configuration and external loading, including gravity. The coordination
 194 filter uses this correction and its stated error bounds as inputs. Residual body
 195 motion, cross-boom coupling, and carrier response enter the stopping-response
 196 budget.

197 3. Hydraulic actuation and command feasibility

198 Each boom has a separate hydraulic supply governed by chamber continu-
 199 ity, friction, and compensated metering [20] (Appendix A). The filter selects
 200 actuator-rate commands c_b using the identified response

$$v_b^{\text{next}} = (I - K_b)v_b + K_bc_b, \quad K_b = \text{diag}(1 - e^{-\Delta t/\tau_{bj}}), \quad (7)$$

201 where $v_b = \dot{x}_b$, τ_{bj} is effective response time, and Δt the control period. Before
 202 spool conversion, pressure feedback gives $\tilde{c}_j = c_j - F_{\text{hp},j}/B_{v,j}$, with high-pass
 203 chamber effort $F_{\text{hp},j}$ and $B_{v,j} = 2\zeta_j\sqrt{k_{h,j}M_{r,jj}}$. Here ζ_j is damping ratio and
 204 $k_{h,j} = \beta_e(D_{A,j}^2/V_{A,j} + D_{B,j}^2/V_{B,j})$ oil stiffness, defined by bulk modulus β_e ,
 205 effective areas $D_{A,j}, D_{B,j}$, and chamber volumes $V_{A,j}, V_{B,j}$. The identified
 206 response and its reserve include this inner feedback.

207 Phase restrictions, speed limits, and slew bounds $|c_{bj} - c_{bj}^-| \leq a_{bj}\Delta t$
 208 constrain commands, with pending command c_{bj}^- and rate-of-change bound
 209 a_{bj} . Extension capacity is

$$p_{A,\text{req}} = \frac{g_{r,j} + F_{C,j} + D_{B,j}(p_T + p_c)}{D_{A,j}}, \quad \tilde{c}_j^+ = \eta_v \frac{Q_{\text{nom},j}}{D_{A,j}} \phi(p_{\text{in,max},j} - p_{A,\text{req}}), \quad (8)$$

210 where $F_{C,j}$ is Coulomb friction, p_T tank pressure, p_c compensator drop,
 211 $Q_{\text{nom},j}$ full-opening flow, and ϕ the metering function in Eq. (A.2). The inlet
 212 limit $p_{\text{in,max},j}$ is the smaller pump/port limit, and η_v reserves valve capacity.
 213 Retraction exchanges chamber areas and reverses the load sign. The nominal
 214 supply budget is

$$\sum_j q_{bj} \leq Q_{\text{avail},b}, \quad q_{bj} \geq D_{A,j}c_{bj}, \quad -D_{B,j}c_{bj}, \quad 0, \quad (9)$$

215 where q_{bj} is a flow epigraph and $Q_{\text{avail},b} = \max(\eta_Q Q_{\text{max},b} - Q_{\text{perc},b} - Q_{\text{res},b}, 0)$.
 216 Pump capacity $Q_{\text{max},b}$ is reduced by reserve factor $\eta_Q \in (0, 1]$, percussion flow
 217 $Q_{\text{perc},b}$, and reserved branch flow $Q_{\text{res},b}$.

218 4. Collision geometry and stopping-aware barriers

219 4.1. Coverage of the two booms and the environment

220 The shared constraints cover mutual and self-collision, carrier obstacles,
 221 tunnel boundaries, the rock face, and actuator/joint limits (Fig. 3). Graph-
 222 frame convex pieces provide closest-point distances [21]; enclosing capsules

223 provide broad-phase lower bounds. Pruning requires these bounds to exceed
 224 the clearance allowance and reachable stopping envelope.

225 For witnesses p_A, p_B and normal n directed from A to B ,

$$d_i = g_i \dot{x}, \quad g_i = n^\top (J_B - J_A), \quad x = (x_L^\top, x_R^\top)^\top. \quad (10)$$

226 The Jacobians contain both booms' columns and zero columns for fixed ob-
 227 stacles. Mutual rows thus couple commands while retaining separate physical
 228 graphs. Witness gradients apply locally; point-speed bounds accommodate
 229 witness changes during braking. For capsule endpoints p_0, p_1 , radius r , and
 230 angular Jacobian column $J_{\omega,j}$,

$$\pi_j = \max(\|J_{p_0,j}\|, \|J_{p_1,j}\|) + r\|J_{\omega,j}\|. \quad (11)$$

231 Self-collision bounds remove common rigid-body motion through relative
 232 twists. Nonnegative P_{ij}, Q_{ij} bound clearance-loss rates for positive and
 233 negative actuator motion. Symmetric geometric bounds give $P_{ij} = Q_{ij}$; scalar
 234 limits use $P_{ij} = \max(-g_{ij}, 0)$ and $Q_{ij} = \max(g_{ij}, 0)$.

235 For rock-face height $X_f(Y, Z)$, smooth lower surface $X_c \leq X_f$, and slope
 236 bound L_f , free-side clearance satisfies

$$\underline{d}_f(p) = \frac{X_c(p_Y, p_Z) - p_X}{\sqrt{1 + L_f^2}}. \quad (12)$$

237 Subtracting probe radii and capsule-axis half-spacing covers the represented
 238 surface between samples. Tunnel rows use hull vertices and analytic bound-
 239 ary distances. Multiple samples use the conservative soft minimum $d_i =$
 240 $-\kappa_d^{-1} \log \sum_\ell e^{-\kappa_d d_{i\ell}}, \kappa_d > 0$.

241 Explicit exclusions cover joint neighbors, guided feed stages, and rigid at-
 242 tachments. Further exclusions use branch-and-bound mesh-clearance searches
 243 over joint limits, conditional on grid-estimated speed constants bounding the
 244 continuum. Policy clearances apply to actively constrained pairs.

245 4.2. Uncertainty reserve and stopping distance

246 Each geometric row requires $D_i = d_i^{\text{pol}} + m_i$, where d_i^{pol} is the policy
 247 clearance and

$$m_i = \sum_j |g_{ij}| \epsilon_{x,j} + (\ell_{iL} + \ell_{iR}) \epsilon_\theta + \chi_i^W (\epsilon_{Kt} + \ell_{iK} \epsilon_{Kr}) + \rho_i + h_{\text{fb}}. \quad (13)$$

248 Here $\epsilon_{x,j}$ bounds the actuator-coordinate error. The scalars ϵ_θ and $(\epsilon_{Kt}, \epsilon_{Kr})$
 249 bound the Euclidean norms of the orientation-correction error and of the

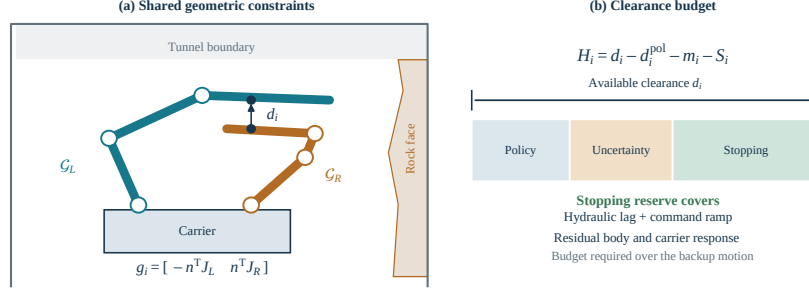


Fig. 3. Shared collision constraints. Mutual-clearance rows couple both booms; environment and self-collision rows enter the same optimization. Clearance covers policy separation, uncertainty, and backup motion, using local witness gradients and bounded point speeds.

250 carrier translation and rotation errors. Each equals the norm of the corre-
 251 sponding per-axis bounds, so an orientation error displaces a point at lever ℓ
 252 by at most $\ell\epsilon_\theta$, to first order. Levers ℓ_{ib}, ℓ_{iK} bound distances from the correc-
 253 tion reference nodes and the carrier rotation center; χ_i^W selects world-obstacle
 254 rows. Common carrier-pose errors cancel in mutual distances. The reserve
 255 ρ_i covers geometry, interpolation, and one-step linearization; $h_{fb} > 0$ sets
 256 the recovery band. Rate-response uncertainty enters the stopping reserve.
 257 Joint/stroke rows use pre-shrunk limits in their coordinate units.

258 The backup ramps each rate-controlled actuator toward zero and closes
 259 its valve at zero command:

$$c_j^{\text{br}} = c_j^- - \text{sgn}(c_j^-) \min(|c_j^-|, a_j \Delta t). \quad (14)$$

260 Define $c_j^+ = \max(c_j, 0)$, $c_j^\ominus = \max(-c_j, 0)$, $\nu_j^+ = \max(v_j, c_j, 0)$, and $\nu_j^- =$
 261 $\max(-v_j, -c_j, 0)$. A convex piecewise-linear ramp majorant satisfies $\mathcal{R}_j(z) \geq$
 262 $z^2/(2a_j)$ and $\mathcal{R}'_j(z) \geq z/a_j$ throughout the rate domain. The shared stopping
 263 reserve and barrier are

$$\begin{aligned} S_i = & \sum_j T_j (P_{ij} \nu_j^+ + Q_{ij} \nu_j^-) + \sum_j [P_{ij} \mathcal{R}_j(c_j^+) + Q_{ij} \mathcal{R}_j(c_j^\ominus)] \\ & + \sum_j A_{ij} (|c_j| + z_j^r) + \sum_j B_{ij} z_j^s, \quad H_i = d_i - D_i - S_i. \end{aligned} \quad (15)$$

264 Effective lag times T_j , ramp bounds, and residual-response gains A_{ij}, B_{ij}
 265 include response inflation $\iota \geq 1$. The additional terms bound residual body
 266 motion, cross-boom coupling, and carrier motion following command changes.

267 Nonnegative slew and step memories evolve as

$$\begin{aligned} z_j^{r,+} &= \lambda_j z_j^r + \min(|\Delta c_j|, a_j \Delta t), \\ z_j^{s,+} &= \lambda_j z_j^s + \max(|\Delta c_j| - a_j \Delta t, 0), \end{aligned} \quad (16)$$

268 where Δc_j is the applied command change and $\lambda_j = e^{-\Delta t / \tau_{\text{ring},j}}$ follows residual-
269 response decay time $\tau_{\text{ring},j}$. Slew-limited commands excite z^r ; excess steps
270 also excite z^s .

271 The condition $H_i \geq 0$ ensures separation throughout a backup continued
272 to rest, provided the estimation allowance and response, clearance-speed, and
273 residual-motion bounds hold throughout that physically realizable stop. This
274 interpretation uses the assumed contact modes, control period, and zero rates
275 for hydraulically locked actuators. Rate uncertainty is represented through
276 response inflation. Forced backup stops (Section 7.1, Appendix D) test these
277 assumptions against realized stopping travel, actuator motion, and clearance.

278 5. Centralized online CBF coordination

279 5.1. Delayed prediction and barrier constraints

280 A centralized quadratic program separates tracking from admissibility [22,
281 23], accounting for actuator response and one-cycle command latency [24].
282 Stack $v = (v_L^\top, v_R^\top)^\top$, $c = (c_L^\top, c_R^\top)^\top$ and $K = \text{blkdiag}(K_L, K_R)$. Estimated
283 state (x, v) and pending command c^- give

$$\begin{aligned} v^{(1)} &= (I - K)v + Kc^-, & \Delta x^{(1)} &= \frac{\Delta t}{2}(v + v^{(1)}), \\ v^{(2)}(c) &= (I - K)v^{(1)} + Kc, & \Delta x^{(2)}(c) &= \frac{\Delta t}{2}(v^{(1)} + v^{(2)}(c)). \end{aligned} \quad (17)$$

284 The first interval is committed. Define $e_i^{(1)} = d_i - D_i + g_i \Delta x^{(1)}$ and $e_i^{(2)}(c) =$
285 $e_i^{(1)} + g_i \Delta x^{(2)}(c)$. A nonnegative pressure-mode flow cap uses $\min(g_{ij}, 0)$ for
286 command-dependent clearance and is treated as instantaneously closable.
287 Slew/ramp terms apply to rate-mode columns, which retain g_{ij} ; valves closed
288 beyond their stopping time use zero rate under hydraulic locking, with
289 clearances updated from measured positions. Equation (15) gives predicted
290 barriers $\widehat{H}_i^{(1)}$ and $\widehat{H}_i^{(2)}(c)$. The hard collision row is

$$\widehat{H}_i^{(2)}(c) \geq t_i, \quad t_i = \min\{(1 - \gamma \Delta t) \widehat{H}_i^{(1)}, \widehat{H}_i^{(2)}(c^{\text{br}})\}, \quad (18)$$

291 where $\gamma > 0$ and $0 < \gamma \Delta t \leq 1$. The minimum admits the backup. For frozen
292 prediction data, $T_j \geq \Delta t(1/K_{jj} - 1/2)$ and the ramp-slope condition yield

293 $\widehat{H}_i^{(2)}(c^{\text{br}}) \geq \widehat{H}_i^{(1)}$. Appendix C relates this property to measured inter-cycle
 294 prediction defects and mode transitions.

295 Linear epigraphs represent maxima, absolute values, and ramp majorants:
 296 $w_j^+ \geq v_j^{(2)}, c_j, 0$, $w_j^- \geq -v_j^{(2)}, -c_j, 0$, and $y_j^\pm \geq m_{j\ell}(\pm c_j) + b_{j\ell}$ for ramp-
 297 segment slopes $m_{j\ell}$ and intercepts $b_{j\ell}$. Collision rows are affine and hard in
 298 the expanded decision vector.

299 Within the geometric recovery band $-h_{\text{fb}} \leq e_i^{(1)} < 0$, the target becomes

$$t_i \leftarrow \min\{t_i, e_i^{(1)} - \eta_b(h_{\text{fb}} + e_i^{(1)})\}, \quad (19)$$

300 where $\eta_b \in (0, 1)$. The additional condition $g_i \Delta x^{(2)}(c) \geq \min\{0, g_i \Delta x^{(2)}(c^{\text{br}})\}$
 301 limits predicted clearance loss to the backup's. The stopping guard is

$$\widehat{H}_i^{\text{guard}} = e_i^{(1)} - S_i^{(1)}/\iota, \quad (20)$$

302 with inflated committed-state reserve $S_i^{(1)}$. A geometric guard below $-h_{\text{fb}}$ or
 303 solver failure applies Eq. (14) to both booms and freezes reference progress.

304 5.2. Tracking objective and hydraulic effort rows

305 Each boom's reference clock advances at $\dot{v}_b = s_b \in [0, 1]$. Transit and
 306 terminal-alignment maps define J_b , feedforward $w_{\text{ff},b}$, and feedback $w_{\text{fb},b}$
 307 (Appendix C). Commands (c_L, c_R) , progress rates (s_L, s_R) , and epigraph
 308 variables minimize

$$\sum_b \left(\|J_b c_b - s_b w_{\text{ff},b} - w_{\text{fb},b}\|_{Q_b}^2 + \rho_b (1 - s_b)^2 + \|c_b - c_b^{\text{pref}}\|_{\Lambda_b}^2 \right), \quad (21)$$

309 subject to Eqs. (9), (18), and (22), command/limit bounds, and contact-
 310 mode rows. Here c_b^{pref} is a secondary rate preference and $\|z\|_Q^2 = z^\top Q z$, with
 311 $Q_b, \Lambda_b \succeq 0$ and $\rho_b \geq 0$. The positioning block of Λ_b uses reduced inertia
 312 normalized by a nominal-speed energy scale, providing a physical metric
 313 across linear/angular coordinates. Small regularization makes the expanded
 314 Hessian positive definite.

315 Let diagonal R_b have entry one in rate mode and zero in pressure-cap
 316 mode, $K_{v,b} = K_b R_b$, and $\bar{v}_b^{(2)} = (I - K_{v,b})v_b^{(1)} + K_{v,b}c_b$. Nominal acceleration
 317 and braking-effort constraints are

$$\begin{aligned} F_b^- &\leq M_{r,b} \frac{K_{v,b}(c_b - v_b^{(1)})}{\Delta t} + g_{r,b} + f_{\text{fr},b}(v_b^{(1)}) \leq F_b^+, \\ F_b^- &\leq -M_{r,b} \frac{K_b \bar{v}_b^{(2)}}{\Delta t} + g_{r,b} \leq F_b^+, \end{aligned} \quad (22)$$

318 where $F_j^+ = D_{A,j}p_{\text{rel},j} - D_{B,j}p_T$ and $F_j^- = -(D_{B,j}p_{\text{rel},j} - D_{A,j}p_T)$ bound
 319 hydraulic effort f_j^h at port-relief pressure $p_{\text{rel},j}$. The first row includes friction
 320 and prescribes acceleration only in rate mode. The second estimates gravity-
 321 loaded abrupt decay; the applied backup remains slew-limited.

322 These rigid-model estimates are compared with chamber efforts in free mo-
 323 tion, valve closure, and loaded operation in Appendix D; Appendix C specifies
 324 the discrepancy bound required for robust tightening, and the reported nomi-
 325 nal missions use the untightened limits. When the nominal force/flow limits
 326 would exclude c^{br} , they are widened to admit it and the excess is recorded; this
 327 preserves feasibility of the optimization, whereas physical feasibility depends
 328 on the actual actuator and pump capacity. Because the mutual rows contain
 329 the commands of both booms and each boom has its own progress rate, either
 330 boom can yield temporarily during concurrent operation.

331 6. Permitted contact and supervisory coordination

332 Docking and loaded operation use guarded approach and force supervision
 333 for designated stinger, bit and rod contacts. Outside these phases, the same
 334 bodies obey rock-face avoidance. Other feed bodies retain front-face clearance,
 335 and mutual-boom, carrier, self-collision and tunnel constraints remain active
 336 throughout.

337 For estimated axial face gap g_c , gap-error allowance δ_c and approach-speed
 338 limit $\bar{v}_c$, the guarded contact row is

$$H_c = \max(g_c - \delta_c, 0) + T_c \bar{v}_c - S_c \geq 0. \quad (23)$$

339 Here S_c is one-sided stopping travel and T_c the minimum effective lag among
 340 closing actuators. Equation (18) enforces the next-state row until force
 341 establishes support. The positive part is evaluated at the measured state before
 342 the program is assembled: the row enters with the constant $\max(g_c - \delta_c, 0)$
 343 and with the gap Jacobian multiplied by σ_c , where $\sigma_c = 1$ if $g_c > \delta_c$ and $\sigma_c = 0$
 344 otherwise, so it is affine in the decision variables. Since $\max(z, 0) \geq z$ and
 345 $\max(z, 0) \geq 0$, this expression never exceeds the clipped first-order prediction,
 346 and the affine row is a restriction of the clipped one. The stopping travel
 347 S_c always uses the unclipped gap Jacobian; for $g_c \leq \delta_c$ the row therefore
 348 limits only the closing rate. The gap Jacobian follows from $F(p + g_c a) =$
 349 0 , with $F(p) = X_f(p_Y, p_Z) - p_X$. Sensing, carrier-pose, face-interpolation
 350 and orientation-correction errors are amplified by $\|\nabla F\|/|\nabla F^T a|$; admissible

351 approaches require a finite gap-error bound. Search-distance and time limits
 352 terminate unsuccessful attempts.

353 After the feed extension establishes support at F_{ext}^* , the bit advances under
 354 a second guarded row and enters pressure mode with thrust

$$F_{\text{bit}}^* \leq \min(F_{\text{nom}}, F_{\text{bit,max}}, F_{\text{ext}}^* - F_{\text{st,min}}), \quad (24)$$

355 where F_{nom} , $F_{\text{bit,max}}$ and $F_{\text{st,min}}$ are requested thrust, maximum bit force and
 356 minimum support force. Thrust is ramped and reduced when support falls
 357 below its minimum. For telescopic gain $\kappa_f = \partial z_{\text{bit}} / \partial d_{b1}$, relating axial bit
 358 travel to master stroke, pressure targets satisfy

$$\begin{aligned} D_{A,\text{feed}} p_{A,\text{feed}}^* &= \kappa_f F_{\text{bit}}^* + F_{C,\text{feed}} + D_{B,\text{feed}} p_{B,\text{feed}}, \\ D_{A,\text{ext}} p_{A,\text{ext}}^* &= F_{\text{ext}}^* + F_{C,\text{ext}} + D_{B,\text{ext}} p_{B,\text{ext}}. \end{aligned} \quad (25)$$

359 The QP constrains branch flow caps, with separate force-window supervi-
 360 sion. Established support replaces the corresponding valve-travel term by
 361 $d_c \max(P_{ij}, Q_{ij})$, where d_c bounds residual, uncommanded settling travel of
 362 the supported actuator after support establishment.

363 Before forward feeding, each convex body $\mathcal{B}$ is enlarged to its continuous
 364 swept set

$$\mathcal{W} = \mathcal{B} \oplus [0, \ell]a = \text{conv}(\mathcal{B} \cup (\mathcal{B} + \ell a)), \quad (26)$$

365 where ℓ is remaining translation, including feed-stage gains, and $\oplus$ denotes
 366 the Minkowski sum. The two envelopes are checked against each other, the
 367 carrier, tunnel and own mechanisms for a drilling axis fixed within its error
 368 reserve. Online constraints use measured feed positions.

369 Each boom follows the phase sequence in Fig. 4. Front-load limits, per-
 370 sistent support loss and excessive feed-extension change terminate loaded
 371 operation. Extension stroke monitors axial slip; transverse stinger motion is
 372 evaluated separately. The supervisor selects actuator-space routes and roll
 373 postures, checks joint look-ahead through the same filter, and introduces
 374 yielding or retreat when progress stalls. The scaled task-map minimum singu-
 375 lar value screens goals and attenuates terminal feedback. Replanning starts
 376 from measured states; unsuccessful recovery holds the booms and reports the
 377 command as unreachable.

378 For the 100-collar campaign in Section 7.2, the look-ahead additionally
 379 uses the load-dependent geometry correction and a planning allowance, with
 380 route endpoints evaluated at the current non-positioning actuator strokes.
 381 The supervisor explores alternative routes after predicted stalls and records

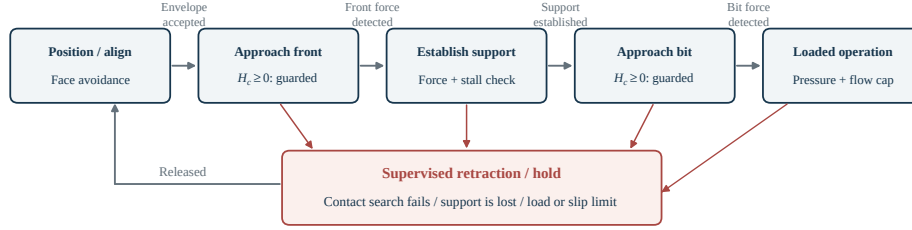


Fig. 4. Per-boom contact supervision within centralized coordination. Approach, force establishment, loaded operation, and retraction select face-contact and actuator modes. Contact failure, excessive load, persistent support loss, or axial slip triggers retreat.

382 unsuccessful route prefixes to avoid repeating them from nearby states. Re-
 383 covery returns home and retries the round once, or retraces the recorded
 384 motion under the active constraints and proceeds to the next round; persistent
 385 planning or recovery failure produces a hold (Appendix F).

386 The plant couples hydraulic actuation to spatially varying rock strength,
 387 percussion-dependent penetration, unilateral bit contact, bore-wall guidance
 388 and rotational resistance. Appendix B defines this phenomenological drilling-
 389 load model and the separate bore-path drift model.

390 7. Numerical verification and validation

391 Timing was measured on two platforms. The demonstration mission and
 392 the 100-collar campaign ran on two virtual cores of a cloud server (Intel Xeon,
 393 2.10 GHz) shared by two concurrent missions; the accelerated evaluations
 394 ran on a Dell XPS 15 9530 laptop (Intel Core i7-13700H, 32 GB RAM).
 395 Appendix D gives the threading and resource conditions.

396 7.1. Coordinated twelve-hole drilling in a confined tunnel using MuJoCo

397 Two hydraulic drilling booms on a common carrier completed six paired
 398 drilling rounds in MuJoCo [25], referred to below as the demonstration mission:
 399 ten face holes and two upward holes, each with a 4.0 m target depth. The
 400 mission started and ended at home (Fig. 5). The plant included closed-chain
 401 linkages, configuration-dependent body-pose response, four carrier stabilizers
 402 with load-dependent support response, hydraulic dynamics, rock interaction,
 403 and bounded sensing errors. The plant step was 1 ms; control ran every 10 ms
 404 during positioning and contact transitions and every 50 ms in slower phases
 405 with closed positioning valves, with a one-period command delay. The plant
 406 was stepped synchronously with the controller, so the reported durations are

407 simulated time and exclude computation. The controller core took 35.7 ms per
 408 cycle on average in this mission; in separate accelerated evaluations (twelve-
 409 hole missions with 0.3 m holes and round 3 at 4 m), it averaged 5.8–6.1 ms,
 410 with about 1% of the 10 ms cycles overrunning. Appendix D gives the target
 411 pattern, parameters, and detailed diagnostics.

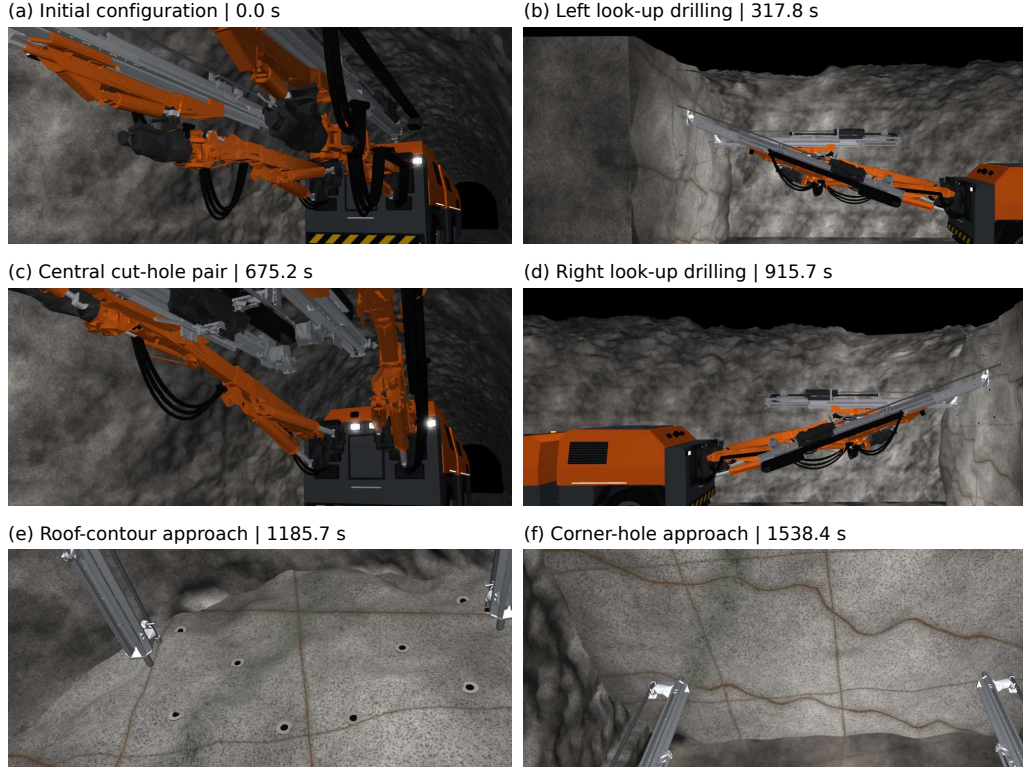


Fig. 5. Representative configurations: (a) home; (b) left upward/right face drilling; (c) central cut holes; (d) right upward/left face drilling; (e) roof-contour approach; and (f) lower-corner approach. Times are elapsed simulation time.

412 The demonstration mission completed all twelve holes and returned home
 413 in 1713.34 s (28.56 min), with 48.035 m of modeled drilling and hole depths
 414 of 4.0025–4.0056 m. Both booms drilled concurrently in every round, for
 415 848.99 s in total including anti-jamming intervals (Fig. 6). In round 5, the left
 416 boom yielded through home; after a segment timeout at 1168.47 s, replanning
 417 completed the repositioning at 1177.27 s. Figure 7 shows the bit-tip paths.

418 Mean and maximum collar errors were 1.77 and 3.98 mm, and the maxi-
 419 mum initial-axis error was 0.0688°. Over 69 668 control cycles, every active

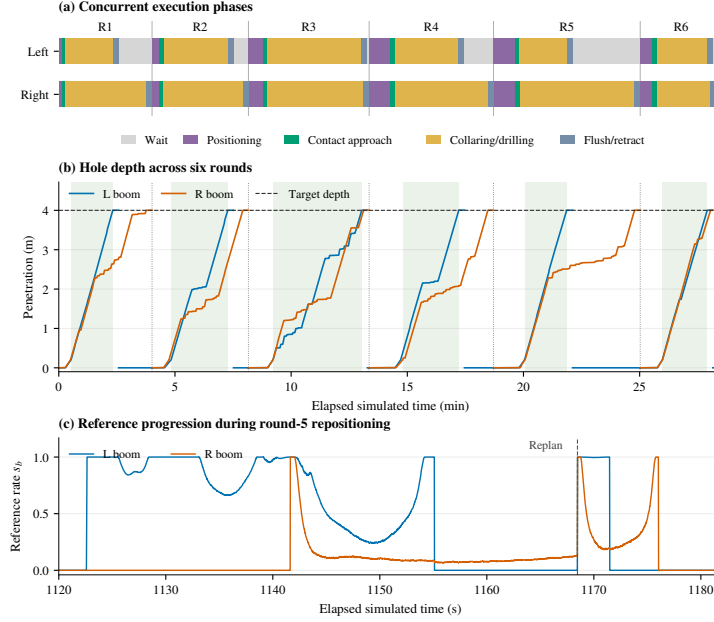


Fig. 6. Six paired rounds: (a) independent phases; (b) hole depths, with concurrent drilling shaded and the 4 m target dashed; and (c) reference-progress rates during round 5, marking the replan at 1168.47 s. Breaks indicate depth-register resets; concurrent drilling includes anti-jamming recovery.

clearance class stayed above its policy; the minimum inter-boom separation was 214.8 mm against a 50 mm policy. No solver failure, guard-triggered fallback, or prohibited contact occurred, and a separate CAD audit found no intersection in 23 730 590 pair checks over 17 134 configurations sampled every 0.1 s. All holes were completed despite 165 anti-jamming activations. The maximum pre-contact feed and axial bit speeds were 11.6 and 9.3 mm s⁻¹, below the 20 mm s⁻¹ approach limit.

Controller comparisons. Four further missions shared plant parameters, initial conditions, targets, and seeds: the proposed filter in concurrent and in sequential operation; independent actuator-aware filters, each treating the other boom at its measured pose; and a geometric velocity-level CBF with $\gamma = 20$ s⁻¹ that keeps the clearance functions, uncertainty allowances, and tracking objectives. Each configuration supplied its own supervisory look-ahead, and independent control planned the booms separately, so the comparison covers complete configurations, including their routes.

All four completed twelve 4 m holes and returned home without prohibited

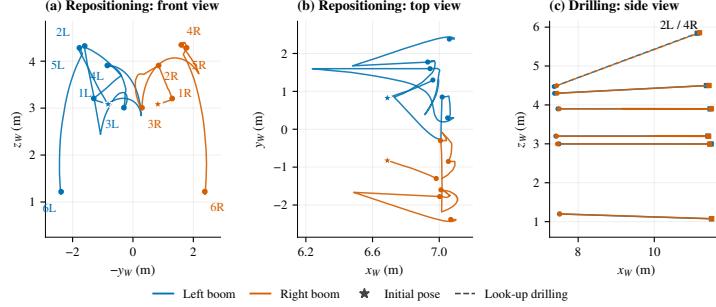


Fig. 7. Plant bit-tip paths sampled at 10 Hz: (a,b) front/top projections of positioning, with round/boom labels at completion and stars at initial poses; (c) collaring/drilling in side view, with upward holes dashed and first/last samples marked by circles/squares. World axes point toward the face (x_W), left (y_W), and upward (z_W).

436 contact or sampled policy violation (Table 2). Concurrent operation took
 437 1666.57 s, which is 42.5% less than sequential operation (speed-up 1.74); the
 438 drilled-length rates were 103.8 and 59.7 m h⁻¹. To remove differences in
 439 drilling time, a post hoc schedule replaced the drilling duration of each hole
 440 with its value in the proposed concurrent run while keeping the measured
 441 non-drilling durations and each scheduling rule (T_{norm}). In this schedule the
 442 speed-up over sequential operation was 1.72, the independent filters were
 443 4.97 s faster than the proposed filter, and the geometric CBF was 147.01 s
 444 (8.8%) faster. The booms stayed more than 210 mm apart in all four missions,
 445 so this target pattern separates the configurations by duration rather than
 446 by inter-boom clearance; they differ in clearance when references conflict, as
 447 shown next. Each entry is a single execution, and the proposed concurrent
 448 run differs from the demonstration mission by 46.77 s.

Table 2 One complete twelve-hole, 4 m mission per controller, each with return home and no sampled policy-clearance violation. T is simulated duration; T_{norm} uses common per-hole drilling durations in a post hoc schedule calculation. Rate is achieved length divided by T ; $e_{p,\text{max}}$ and $e_{a,\text{max}}$ are maximum collar/axis errors; $d_{\text{LR},\text{min}}$ is minimum inter-boom clearance.

Controller	T (s)	T_{norm} (s)	Rate (m h ⁻¹)	$e_{p,\text{max}}$ (mm)	$e_{a,\text{max}}$ (°)	$d_{\text{LR},\text{min}}$ (mm)
Proposed, concurrent	1666.57	1666.57	103.8	3.98	0.0588	211.7
Proposed, sequential	2896.14	2870.76	59.7	4.99	0.0874	227.6
Independent	1723.95	1661.60	100.3	4.09	0.0862	214.7
Geometric CBF ($\gamma = 20$)	1551.57	1519.56	111.5	2.69	0.0489	217.1

449 *Conflicting references and forced stops.* With route supervision bypassed,
450 conflicting references drove both booms across the tunnel center. The proposed
451 filter kept 94.47/94.50 mm inter-boom clearance at half/full reference speed
452 and the independent filters 88.85/88.23 mm, against the 50 mm policy. At
453 the same reference speeds, the result of the geometric CBF depended on
454 its gain: $\gamma = 20 \text{ s}^{-1}$ gave minimum separations of 0.88/−0.62 mm, with
455 contact at full speed, whereas $\gamma = 5 \text{ s}^{-1}$ kept 75.22/77.15 mm. Unlike the
456 geometric CBF, the proposed barrier reserves stopping travel computed from
457 the identified response and braking limits. The proposed filter approached at
458 about 180 mm s^{-1} , compared with $867\text{--}1056 \text{ mm s}^{-1}$ for the geometric CBF
459 at these two gains. In forced backup stops during positioning, the clearance
460 loss stayed within 42% of the stopping reserve plus uncertainty allowance
461 for the nominal plant, for pump capacity reduced to 15%, and for combined
462 perturbations at 80% relief pressure. The reserve was exceeded at 50% relief
463 pressure and, under combined perturbations, at 60%, in both cases without
464 adapting the braking ramp; in the reported cases with the ramp scaled to the
465 known capacity, no exceedance occurred. Appendix D details these tests, the
466 parameter perturbations, computation times, and effort accuracy.

467 7.2. Reaching and docking at 100 collars

468 A separate MuJoCo campaign on the same plant tested positioning and
469 contact establishment, without drilling, at 100 collars in 50 paired rounds,
470 with 50 targets per boom and 15 assignments across the tunnel center line
471 (Fig. 8). Each operation comprised a move to a 0.45 m stand-off, guarded
472 approach, load establishment, a 2 s docked hold, and retraction. An operation
473 counted as completed only if the total front contact load (stinger plus bit)
474 was at least 4 kN at every controller-cycle sample of the hold. The docking
475 guard still checked the envelope of the intended 4 m hole. The target pattern
476 and route heuristics were refined on the nominal model and in pilot trials;
477 one start-clearance rule was amended during the campaign, and all reported
478 runs use the same final target sequence (Appendix F). Figure 9 shows one
479 recorded round.

480 The full framework (A) was run under three conditions, S1–S3, which
481 differ in the seeds of the sensing noise, of the directional-valve gains (scattered
482 within $\pm 5\%$ and fixed per run), and of the face relief. Five ablations were run
483 on S1: B removes the online collision rows; C substitutes a kinematic CBF;
484 D uses direct joint-space moves with the full filter; E sets the estimated-error
485 allowances to zero; and F combines direct moves with removed collision rows.

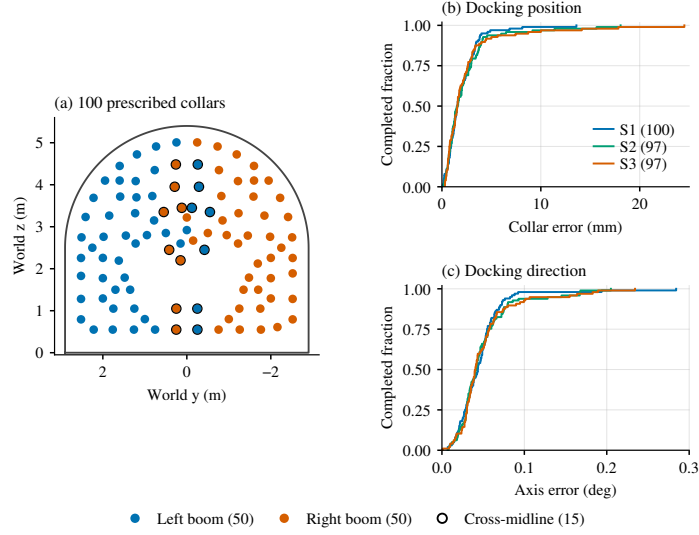


Fig. 8. Target pattern and docking accuracy. (a) Collar locations by assigned boom; rings mark cross-center assignments. (b,c) Empirical cumulative distributions of collar and axis errors at completed docked holds: 100 for S1 and 97 each for S2 and S3. The target sequence is shared across conditions.

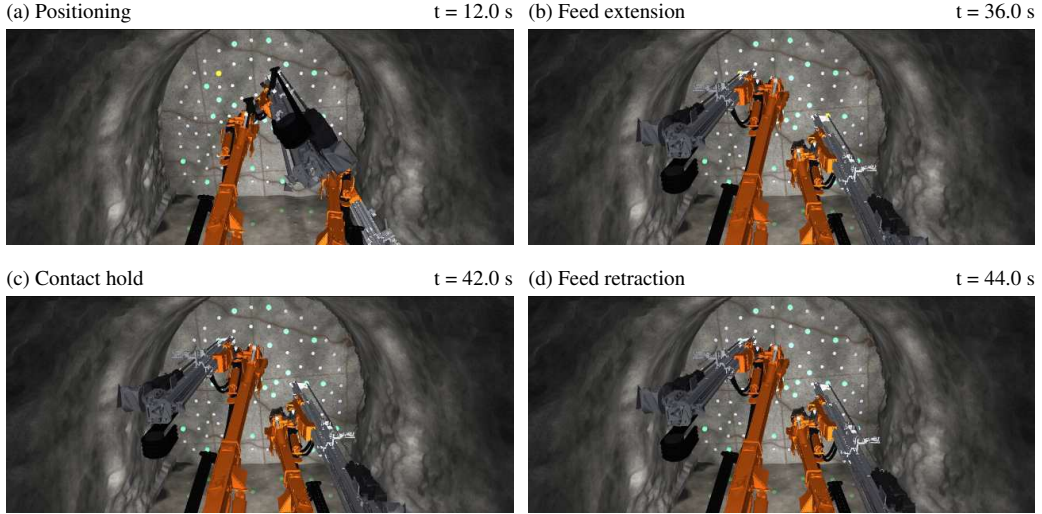


Fig. 9. Recorded MuJoCo execution of round 12 (A/S1, targets L28/R36): positioning, feed extension, supported hold and retraction. Times are relative to the start of the round. All snapshots use the same camera view.

486 A, B, C, and E share a supervisory look-ahead that uses the full actuator-
 487 aware filter, and limit and permitted-contact handling stays active in every
 488 variant (Appendix F).

489 The full framework completed 100, 97, and 97 operations under S1–S3
 490 (294 of 300; 98%) without prohibited contact or sampled policy-clearance
 491 violation; the smallest margin over policy was 29.4 mm. Of the six incomplete
 492 operations, four belonged to two rounds that were skipped after planning or
 493 replanning failed, and two reached the docked hold but fell below the load
 494 criterion. Pooled collar errors had a median of 1.57 mm, a 95th percentile of
 495 5.75 mm, and a maximum of 24.51 mm; axis errors had a median of 0.042° and
 496 a maximum of 0.284°. For the 94 targets completed in all three conditions,
 497 the across-condition range of the collar error had a median of 1.69 mm and a
 498 maximum of 23.81 mm. All 296 pre-contact feed-extension rates stayed below
 499 20 mm s⁻¹ (maximum 16.5 mm s⁻¹).

Table 3 Outcomes of the 100-collar campaign. N_c counts completed load-qualified docking cycles; N_p counts those completed within paired rounds that retained every monitored policy clearance. $\Delta_{\min}$ is the minimum clearance minus its class policy. $v_{\text{td},\max}$ is maximum feed-extension rate in the 50 ms preceding detected contact; $N_{>20}/N_{\text{td}}$ counts rates above 20 mm s⁻¹ among all touch-downs. T is simulated execution time excluding planning computation. D/S1 completed four targets before subsequent direct moves were held by the filter.

Run	N_c	N_p	$\Delta_{\min}$ (mm)	$v_{\text{td},\max}$ (mm/s)	$N_{>20}/N_{\text{td}}$	T (s)
A/S1	100/100	100	+30.8	15.0	0/100	3074.13
A/S2	97/100	97	+30.0	16.5	0/98	3130.51
A/S3	97/100	97	+29.4	15.7	0/98	3060.32
B/S1	100/100	100	+29.4	18.6	0/100	2242.89
C/S1	100/100	100	+26.3	25.9	16/100	2088.09
D/S1	4/100	4	+31.1	10.3	0/4	425.40
E/S1	100/100	100	+30.8	20.3	1/100	2624.52
F/S1	97/100	36	-328.0	14.2	0/98	1570.01

500 The S1 ablations separate the roles of routing and online filtering (Fig. 10,
 501 Table 3). With direct joint-space moves, the full filter (D) preserved every
 502 monitored clearance but stalled after four targets, whereas variant F, without
 503 the collision rows, completed 97 docking cycles, only 36 of them in policy-
 504 compliant rounds, with collision or geometric penetration in 29 rounds and
 505 73.365 s of recorded contact. With supervised routes, A, B, C, and E all

506 completed 100 targets within the monitored clearances, and B, C, and E
 507 needed 15–32% less simulated time than A. Under S1, the look-ahead with
 508 the full filter, which these four variants share, thus kept the executed routes
 509 within policy even without the online collision rows (B). The online rows
 510 preserved clearance when the route was not pre-screened (D versus F), and
 511 execution with them took longer (A versus B).

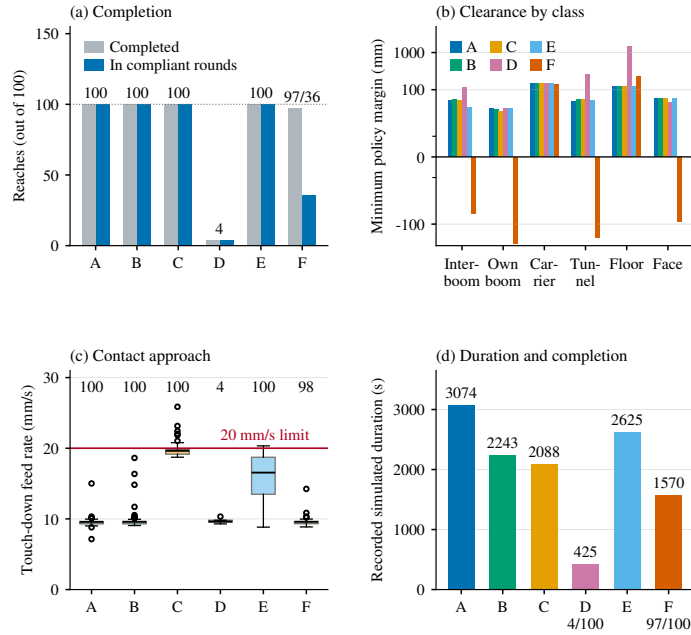


Fig. 10. S1 controller comparisons (A–F: Table F.12): (a) docking completion and completion within policy-compliant rounds; (b) minimum excess over each clearance policy, on a symmetric logarithmic axis; (c) pre-contact feed-extension rates (quartiles, median, 1.5-IQR whiskers and outliers; sample counts above); (d) simulated execution duration, with incomplete task counts marked. Planning computation is excluded.

512 The online formulations differed in contact approach. The pre-contact
 513 feed-extension rate exceeded 20 mm s^{-1} at 16 of 100 touch-downs with the
 514 kinematic CBF (C, maximum 25.9 mm s^{-1}) and at one of 100 without error
 515 allowances (E, 20.3 mm s^{-1}), and at none with A or B. Durations in Table 3
 516 are simulated execution time: the plant was paused during route planning,
 517 which required a median of 139–167 s of computation per round (Appendix F).

518 *7.3. Cross-engine verification of the exported dual-boom model in Isaac Sim*

519 Cross-engine model verification in Isaac Sim comprised prescribed-state
 520 replay, rigid-body tree queries, and a dynamically integrated closed-chain
 521 static hold. These checks assessed the transfer of configuration maps, col-
 522 lision geometry, inertia, and equilibrium loads. The replay uses all 17 134
 523 configurations stored at approximately 0.1 s intervals from the demonstration
 524 mission. All fifteen checks passed (Table 4).

Table 4 Cross-engine model verification: prescribed-state replay, open-tree dynamics and a closed-chain static hold. Maxima and numerical acceptance criteria refer to the stated samples and channels.

Quantity and coverage	Full-run result	Comparison criterion
Link frames; 17 134 configurations	8.24 μm ; 1.34 μrad	1 mm; 1 mrad
Left/right bit position; same configurations	9.10/9.88 μm	1 mm
Loop gap; prescribed-state replay	1.97 μm	1 mm; loops not enforced
Closest-distance discrepancy; 13 classes	1.498 mm	5 mm in $\geq 99\%$ of comparable states per class, and for each class minimum
Known-collision controls	6/6 detected	Negative reported separation in every specified collision class
Tree mass matrix; 24 states	$\epsilon_M = 1.75 \times 10^{-5}$	$\epsilon_M < 5 \times 10^{-3}$
Gravity; same 24 states	$\epsilon_g = 8.88 \times 10^{-6}$	$\epsilon_g < 5 \times 10^{-3}$
Coriolis/centrifugal term; same 24 states	$\epsilon_c = 1.20 \times 10^{-5}$	$\epsilon_c < 2 \times 10^{-2}$
Static hold; final second of 10 s	Maximum interval-averaged coordinate speed 2.73 $\times 10^{-4}$ rad/s, 2.42 $\times 10^{-5}$ m/s; loop gap 4.89 μm	Speed over intervals ≥ 0.1 s below 10^{-3} rad/s or m/s; gap below 1 mm
Mean body/carrier-coordinate displacement; 12 coordinates	12/12 within tolerance	Larger of 2% of reference magnitude and 20 μrad or 20 μm
Mean actuator effort; 16 force and 4 torque channels	Largest errors 21.4 N and 0.772 N m	Larger of 2% of reference magnitude and 500 N or 500 N m

525 Figure 11 compares the reference bit paths with positions reconstructed
 526 from PhysX link poses. Position and loop-gap discrepancies stayed at the
 527 micrometer scale, which confirms the transferred joint frames at the prescribed
 528 configurations. Geometric queries covered thirteen distance classes: eleven
 529 prohibited contacts and two permitted stinger–face contacts. Every prohibited-
 530 contact class kept its policy clearance on the replay grid; the minimum inter-
 531 boom separation was 215.13 mm, close to the finer-grid MuJoCo minimum

of 214.76 mm. Six configurations with known self-, inter-boom, roof, floor, carrier, or face collisions produced the expected reports.

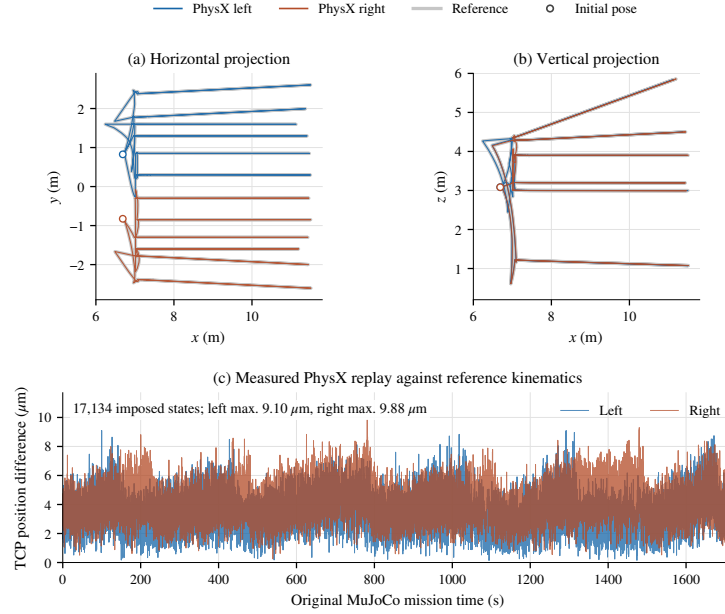


Fig. 11. Prescribed-state verification of bit-tip trajectories. (a,b) Reference kinematics and PhysX link poses at retained MuJoCo configurations. (c) Position discrepancies. Time follows the demonstration mission; gravity and loop enforcement are disabled during replay.

Tree dynamics agreed at twenty-four states after accounting for the armature convention of the two engines. In a separate 10 s closed-chain hold at home with implicit position drives, the final-second mean displacements of all twelve body/carrier response coordinates and the measured efforts of all twenty channels met their tolerances (Appendix E).

8. Conclusion

This paper connected independently compiled closed-chain mechanism models to a centralized CBF-QP that coordinates two hydraulic drilling booms. The program regulates actuator commands and reference progress under mutual, self-, and environmental clearance constraints, nominal effort limits, and per-boom flow budgets; its clearance reserves cover command delay, hydraulic response, braking, residual plant motion, and uncertainty, and a supervisor sequences routing, intentional contact, drilling, and recovery.

547 In MuJoCo, a twelve-hole mission completed 48.035 m of modeled drilling
548 with mean/maximum collar errors of 1.77/3.98 mm; in separate comparison
549 missions, concurrent operation took 42.5% less simulated time than sequential
550 operation. The 100-collar docking campaign completed 294 of 300 operations
551 across three conditions without sampled policy-clearance violation, with pre-
552 contact feed-extension rates below 20 mm s⁻¹ and a pooled median collar error
553 of 1.57 mm. The comparisons indicate a division of roles: supervised routing
554 provided task progress, and the stopping-aware filter preserved clearance
555 when routes were not pre-screened or references conflicted. The comparisons
556 quantify execution duration and contact-approach regulation for the proposed
557 filter and the geometric CBF baseline. Isaac Sim checks confirmed the
558 exported geometry, tree dynamics, and closed-chain static equilibrium.

559 The capacity-perturbation tests characterize the dependence of stopping
560 reserves on available actuator capacity and braking ramps. The timing
561 results quantify controller and route-planning workloads under the reported
562 computational conditions.

563 **CRediT authorship contribution statement**

564 **Mehdi Heydari Shahna:** Writing - original draft, Validation, Method-
565 ology, Investigation, Formal analysis, Software, Data curation, Conceptualiza-
566 tion.

567 **Tuomo Kivelä:** Writing - review & editing, Resources, Supervision,
568 Funding acquisition.

569 **Jouni Mattila:** Writing - review & editing, Resources, Supervision,
570 Funding acquisition.

571 **Declaration of competing interest**

572 The authors declare that they have no known competing financial interests
573 or personal relationships that could have appeared to influence the work
574 reported in this paper.

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579 Code and model availability

580 The source code implementing the proposed coordination algorithm can
 581 be provided by the corresponding author on reasonable request. Machine-
 582 specific model parameters are confidential and are excluded from the shared
 583 implementation. Executing the implementation requires separately supplied
 584 mechanism, collision-geometry, and actuator-response data.

585 Appendix A. Hydraulic constitutive model

586 Chamber continuity and actuator effort satisfy

$$\begin{aligned} \dot{p}_A &= \frac{\beta_e}{V_A(x)}(Q_A - D_A v - Q_\ell), & \dot{p}_B &= \frac{\beta_e}{V_B(x)}(Q_B + D_B v + Q_\ell), \\ f^h &= D_A p_A - D_B p_B, & f &= f^h - f_{\text{fr}}(v), & f_{\text{fr}}(v) &= F_C \tanh(v/v_s) + b_v v, \end{aligned} \quad (\text{A.1})$$

587 where $v = \dot{x}$, Q_A, Q_B are signed flows into the chambers, D_A, D_B effective
 588 piston/annulus areas, and p_A, p_B chamber pressures. Leakage is $Q_\ell = C_\ell(p_A -$
 589 $p_B)$ with conductance C_ℓ . The effective bulk modulus is β_e ; F_C, b_v are Coulomb
 590 and viscous friction coefficients, and $v_s > 0$ regularizes the online friction
 591 approximation. The plant uses joint friction loss for dry friction. Chamber
 592 volumes are $V_A = V_{A0} + D_A(x - x^-)$ and $V_B = V_{B0} + D_B(x^+ - x)$, with
 593 dead volumes V_{A0}, V_{B0} and coordinate bounds x^-, x^+ . Rotary actuators use
 594 displacements per radian for D_A, D_B and torques for f^h, f ; rod spin has a
 595 separate process-drive branch.

596 The normalized spool opening $v \in [-1, 1]$ follows $\tau_s \dot{v} = v_{\text{cmd}} - v$, with
 597 time constant τ_s and target v_{cmd} . Compensated metering is

$$\begin{aligned} Q_{\text{in}} &= Q_{\text{nom}} |v| \phi(p_S - p_{\text{in}}), & Q_{\text{out}} &= Q_{\text{nom}} \frac{D_{\text{out}}}{D_{\text{in}}} |v| \phi(p_{\text{out}} - p_T), \\ \phi(\Delta p) &= \frac{d}{\sqrt{p_c(d + p_\epsilon)}} \sqrt{\frac{p_c + p_\epsilon}{p_c}}, & d &= \text{clip}(\Delta p, 0, p_c), \end{aligned} \quad (\text{A.2})$$

598 where Q_{nom} is full-opening flow, p_S, p_T supply/tank pressures, p_c the compen-
 599 sator drop, and $p_\epsilon > 0$ the metering regularization. Spool direction selects
 600 inlet/outlet pressures $p_{\text{in}}, p_{\text{out}}$, areas $D_{\text{in}}, D_{\text{out}}$, and chamber-flow signs in
 601 Eq. (A.1). Load-sensing supply is pump-limited; port relief and make-up
 602 functions restrict chamber pressures.

603 Appendix B. Rock geometry and drilling-load model

604 The face and local unconfined compressive strength are

$$\begin{aligned} X_f(Y, Z) &= x_f + A_f \text{clip}(\mathcal{F}_2(Y, Z), -1, 1), \\ \sigma(p) &= \sigma_0 \chi_\sigma(p) [1 + a_\sigma \text{clip}(\mathcal{F}_3(p), -1.5, 1.5)], \\ \mathcal{F}_d(p) &= \frac{1}{2} \sum_k a_k \cos(\mathbf{k}_k^\top p + \psi_k). \end{aligned} \quad (\text{B.1})$$

605 Here $x_f, A_f, \sigma_0, a_\sigma$ are nominal face location, relief amplitude, intact strength
606 and relative strength variation. Fourier amplitudes a_k , wavevectors $\mathbf{k}_k$ and
607 phases ψ_k are seeded. Joint/shear bands use strength factor $\chi_\sigma \leq 1$ and
608 torque multiplier $\chi_T \geq 1$; overlaps take the minimum strength and maximum
609 torque factors. The tunnel has vertical walls, floor $Z = 0$, and a semicircular
610 roof of radius $W/2$ and spring height $H - W/2$, for width W and height H .
611 Piecewise longitudinal expansion represents previous excavation. A discretized
612 face supports frictional stinger contact.

613 Hammer pressure follows $\tau_h \dot{p}_h = p_h^{\text{cmd}} - p_h$, with time constant τ_h and
614 bounded target p_h^{cmd} . Active percussion gives

$$\begin{aligned} E &= E_0 p_h / p_0, & f_h &= f_0 \sqrt{p_h / p_0}, \\ F_* &= F_{*,0} p_h / p_0, & \eta_F &= \xi e^{1-\xi}, \\ \xi &= F_{\text{ax}} / F_*, & \theta_I &= 180 |\omega| / (\pi f_h), \\ \eta_I &= \exp[-(\theta_I - \theta_*)^2 / (2s_I^2)], \\ v_p &= \frac{f_h E \eta_F \eta_I}{k_{\text{SE}} \sigma(p_{\text{bot}}) A_{\text{bit}}}. \end{aligned} \quad (\text{B.2})$$

615 Reference pressure, impact energy, blow frequency and optimal thrust are
616 $p_0, E_0, f_0, F_{*,0}$. Bit thrust and spin are F_{ax}, ω ; θ_I, θ_*, s_I are actual/optimal
617 indexing angles and spread in degrees. Bit area is $A_{\text{bit}} = \pi R_{\text{bit}}^2$ for radius
618 R_{bit} ; k_{SE} converts strength to specific energy, and p_{bot} is the modeled bottom.
619 Penetration is zero at thrust $F_{\text{ax}} \leq F_{\text{min}}$ or with inactive percussion. Operating
620 hammer flow is $Q_{\text{perc}} = E f_h / (\eta_h p_h)$ for hydraulic efficiency η_h .

621 For collared unit axis a_0 , collar p_{col} , accumulated depth ℓ_h and bit position
622 p_{tip} , compression and axial velocity are $\delta = a_0^\top (p_{\text{tip}} - p_{\text{col}}) - \ell_h$ and $v_a = a_0^\top \dot{p}_{\text{tip}}$.
623 Unilateral contact gives

$$\begin{aligned} F_{\text{ax}} &= \mathcal{C}(\delta, v_a - v_p), \\ \mathcal{C}(\delta, w) &= \begin{cases} [k_a \delta + c_a w \min(1, \delta / \delta_0)]_+, & \delta > 0, \\ 0, & \delta \leq 0, \end{cases} \end{aligned} \quad (\text{B.3})$$

624 where $[z]_+ = \max(z, 0)$, k_a, c_a are axial stiffness/damping, and δ_0 is the
 625 damping-activation range. Scalar bisection couples Eqs. (B.2) and (B.3),
 626 advancing the bottom according to contact-dependent penetration. With
 627 $r = (I - a_0 a_0^T)(p_{\text{tip}} - p_{\text{col}})$, $\rho = \|r\|$ and $e_r = r/\rho$, wall guidance and initial
 628 face friction are

$$\mathbf{F}_w = -[k_w(\rho - r_c) + c_w e_r^T \dot{p}_{\text{tip}}]e_r, \quad \rho > r_c, \quad \mathbf{F}_t = \Pi_{\mu_f F_{\text{ax}}}(-k_t s_t - c_t v_t). \quad (\text{B.4})$$

629 Wall force is zero within clearance r_c ; k_w, c_w are wall stiffness/damping. Before
 630 wall engagement, s_t, v_t are transverse stick-anchor displacement and velocity,
 631 with stiffness/damping k_t, c_t . For friction coefficient μ_f , Π_R projects onto a
 632 force ball of radius R . Anchor updates enforce $\|k_t s_t\| \leq \mu_f F_{\text{ax}}$ before damping
 633 and projection.

634 Rotational resistance and the rod wrench are

$$\begin{aligned} T_{\text{res}} &= [T_0 \min(1, \ell_h/\ell_0 + b_0) + c_\omega |\omega| \\ &\quad + \mathbf{1}_{F_{\text{ax}} > F_{\text{min}}} \mu_b F_{\text{ax}} r_e \chi_T + T_s] \tanh(\omega/\omega_s), \\ \mathbf{F}_{\text{rock}} &= -F_{\text{ax}} a_0 + \mathbf{F}_\perp, \\ \mathbf{m}_{\text{rock}} &= (p_{\text{tip}} - p_G) \times \mathbf{F}_{\text{rock}} - T_{\text{res}} a_{\text{spin}}. \end{aligned} \quad (\text{B.5})$$

635 Here T_0, ℓ_0, b_0 set initial resistance; $c_\omega, \mu_b, r_e, \omega_s$ define viscous/frictional resis-
 636 tance and stall regularization. The indicator selects loaded friction; T_s adds
 637 seeded half-sine jamming pulses in loaded weak rock. The active transverse
 638 force is $\mathbf{F}_\perp \in \{\mathbf{F}_t, \mathbf{F}_w\}$, p_G is rod center of mass, and a_{spin} its signed joint
 639 axis, including reflection. A separate bore-path model adds joint-induced
 640 drift, random wobble and gravity bias while the mechanical rod follows its
 641 collared axis.

642 Appendix C. Tracking maps and sampled barrier diagnostics

643 Appendix C.1. Transit and terminal tracking maps

644 For actuator-space reference $x_b^{\text{ref}}(\vartheta_b)$ and clock rate $\dot{\vartheta}_b = s_b$, transit
 645 tracking uses

$$\begin{aligned} J_b &= P_{\text{pos}}, \quad w_{\text{fb},b} = P_{\text{pos}} dx_b^{\text{ref}}/d\vartheta_b, \\ w_{\text{fb},b} &= \text{clip}\left(K_x P_{\text{pos}}(x_b^{\text{ref}} - x_b), -\bar{w}_b, \bar{w}_b\right). \end{aligned} \quad (\text{C.1})$$

646 The selector $P_{\text{pos}} = [I_6 \ 0_{6 \times 3}]$ retains six positioning coordinates, K_x contains
 647 proportional gains, and $\bar{w}_b$ bounds feedback componentwise. With $\Pi_{\text{pos}} =$

648 $P_{\text{pos}}^\top P_{\text{pos}}$, terminal alignment uses

$$J_b = \begin{bmatrix} J_{p,b} \\ \beta_{b1}^\top J_{\omega,b} \\ \beta_{b2}^\top J_{\omega,b} \end{bmatrix} \Pi_{\text{pos}}, \quad w_{\text{fb},b} = \begin{bmatrix} K_p(p_b^d - p_b) \\ K_o \beta_{b1}^\top (a_b \times a_b^d) \\ K_o \beta_{b2}^\top (a_b \times a_b^d) \end{bmatrix}. \quad (\text{C.2})$$

649 Here p_b, a_b denote estimated tool position and unit axis; p_b^d, a_b^d are their
 650 targets. Orthonormal β_{b1}, β_{b2} span the plane perpendicular to a_b^d , with gains
 651 $K_p, K_o > 0$. Translation/orientation feedback is bounded and attenuated near
 652 poor task-map conditioning. Terminal feedforward is zero; tool roll enters the
 653 secondary preference. Positioning-actuator columns alone determine terminal
 654 alignment.

655 *Appendix C.2. Sampled barrier recursion and effort discrepancy*

656 For a row with the same definition in consecutive cycles, the inter-cycle
 657 prediction defect is

$$\delta_{i,k} = \hat{H}_i^{(2)}(c_k) \Big|_k - \hat{H}_i^{(1)} \Big|_{k+1}. \quad (\text{C.3})$$

658 When the optimized command is applied and Eq. (19) is inactive, Eq. (18)
 659 implies

$$\hat{H}_i^{(1)}(k+1) \geq \min \{ (1 - \gamma \Delta t_k) \hat{H}_i^{(1)}(k), \hat{H}_i^{(2)}(c_k^{\text{br}}) \Big|_k \} - \delta_{i,k}. \quad (\text{C.4})$$

660 The measured defect combines response and integration errors, changes in
 661 witnesses and estimates, and local-reserve variation. The values reported
 662 in Appendix D characterize the sampled barrier recursion. Extension to a
 663 plant-level invariance result additionally requires a uniform bound on $\delta_{i,k}$. A
 664 mode change restarts the recursion with the new barrier, including stopping
 665 terms for released actuators, and a change of control period requires valid
 666 prediction and stopping bounds for the new period; the barrier jumps observed
 667 at such transitions are also reported there.

668 For Eq. (22), robust effort limits take the form $F_{b,j}^+ - \varepsilon_{b,j}$ and $F_{b,j}^- + \varepsilon_{b,j}$
 669 when $\varepsilon_{b,j}$ bounds the complete-period discrepancy between predicted and
 670 actual effort, including pressure transients and external loading. The effort
 671 errors measured in the tested conditions are given in Appendix D; capacity-
 672 aware stopping additionally uses the available pressure, flow, and realizable
 673 ramp.

674 Appendix D. Detailed drilling outcomes and controller diagnostics

675 Appendix D.1. Task, plant and individual outcomes

676 The tunnel width and height were 5.8 and 5.4 m. The face was centered
677 at $X = 7.45$ m with 0.12 m relief amplitude; world axes point toward the face
678 (X), left (Y), and upward (Z). Target collars were ray–surface intersections.
679 Table D.5 spans central cut holes separated by 0.6 m, asymmetric 20° upward
680 drilling, and outward contour/corner configurations.

Table D.5 Six-round target pattern. (Y_0, Z_0) are ray-anchor coordinates in meters at $X_0 = 7.45$ m; collars are intersections with the nonplanar face. Yaw is positive from $+X$ toward $+Y$, elevation upward. Each target depth is 4.0 m.

Round	Left hole: type; (Y_0, Z_0)	Right hole: type; (Y_0, Z_0)	Yaw L/R ($^\circ$)	Elevation L/R ($^\circ$)
1	Production; (1.30, 3.20)	Production; (−1.30, 3.20)	0/0	0/0
2	Upward; (1.60, 4.50)	Production; (−0.85, 3.90)	0/0	20/0
3	Central cut; (0.30, 3.00)	Central cut; (−0.30, 3.00)	0/0	0/0
4	Production; (0.85, 3.90)	Upward; (−1.60, 4.50)	0/0	0/20
5	Roof contour; (1.80, 4.30)	Roof contour; (−1.80, 4.30)	+2.86/ − 2.86	+2.86/ + 2.86
6	Lower corner; (2.40, 1.20)	Lower corner; (−2.40, 1.20)	+2.86/ − 2.86	−1.72/ − 1.72

681 The hydraulic model in Section 3 was coupled to the rock/contact model
682 in Appendix B. Rock parameters were prescribed at 200 MPa intact strength
683 and 6% field scaling, with three joint families, one shear band and a 64 mm
684 bit. Control used actuator/carrier measurements and estimated orientation
685 corrections; evaluation used plant states. Rock, sensing, and left/right torque-
686 event seeds were 2026, 11 and 77/78; bore-path seeds for zero-based round r
687 were $1000 + 10r$ and $1001 + 10r$.

688 The missions were run with MuJoCo 3.3.7 (implicit-fast integrator, Newton
689 solver with at most 100 iterations and tolerance 10^{-10} , elliptic friction cones)
690 under Python 3.11 with NumPy 2.4.4; distance queries used Coal 3.0.3. The
691 QP was solved in dense form by the dual active-set method of Goldfarb and
692 Idnani [26] (quadprog 0.1.12), cold-started in every cycle. Decision variables
693 were scaled by nominal actuator speed, flow, and ramp travel, constraint
694 rows by their largest coefficient, and the Hessian was regularized by 10^{-6}
695 times its mean diagonal. A solution was accepted when the largest scaled
696 constraint violation was below 10^{-6} ; otherwise the cycle counted as a solver
697 failure. Rows satisfied by every admissible command were removed before
698 the solve. Table D.6 lists the controller and response parameters.

699 Collar and axis errors at hole definition were

$$e_{p,h} = \|p_h - p_h^*\|_2, \quad e_{a,h} = \cos^{-1}(a_h^\top a_h^*), \quad (\text{D.1})$$

Table D.6 Controller and response parameters of the reported missions. Actuator order: swing, lift, zoom, tilt, feed-swing, roll, bolting, feed extension, feed. The bolting cylinder is not actuated in the missions and uses the tilt-cylinder values.

Quantity	Value
Response times τ_{bj} (ms)	78, 66, 44, 69, 62, 116, 69, 44, 45
Identified lag T_j/ι (ms)	126, 107, 66, 125, 138, 128, 125, 68, 61
Response inflation ι	1.25 (twelve-hole missions); 1.30 (100-collar campaign)
Slew bounds a_{bj}	0.15 m s^{-2} ; roll 1.0 rad s^{-2} ; feed extension and feed 0.6 m s^{-2}
Rate limit; ramp majorant	0.6 of nominal valve speed; four linear segments
Capacity reserves η_v, η_Q	0.8, 0.9
residual-response decay time $\tau_{\text{ring},j}$	3 s
$\gamma; \eta_b; h_{\text{fb}}; \kappa_d$	20 s^{-1} ; 0.5; 10 mm; 200 m^{-1}
Model updates	reduced dynamics and geometry correction every five control cycles
$\epsilon_{x,j}$	0.2 mm (strokes); 0.5 mrad (roll)
Per-axis error bounds	orientation correction 2.5 mrad; carrier 0.5 mm and 0.1 mrad
ρ_i	face interpolation 4 mm; linearization 1 mm; row-specific geometry terms
Contact	$\bar{v}_c = 20 \text{ mm s}^{-1}$; $d_c = 5 \text{ mm}$; $F_{\text{st},\min} = 4 \text{ kN}$; $F_{\text{bit},\max} = 20 \text{ kN}$
Tracking	$K_p = K_o = 2.5 \text{ s}^{-1}$ (bounds 0.1 m s^{-1} , 0.1 rad s^{-1}); $K_x = 3 \text{ s}^{-1}$; $\rho_b = 100$
Supervisor	look-ahead step 20 ms; stall after 3 s below 1% of nominal rate and 5% clock rate; at most two replans

700 where p_h and a_h are actual collar position and unit axis, and starred quantities
701 are targets. Table D.7 separately reports the rock model’s transverse bottom
702 drift from the collared axis.

Table D.7 Individual outcomes of the demonstration mission. Collar and axis errors follow Eq. (D.1); bottom drift is the rock-model offset from the collared straight axis. Duration spans hole definition after support loading through flushing, including rapid feed, collaring, drilling and recovery. All holes reached their targets.

Hole	Depth (m)	e_p (mm)	e_a ($^\circ$)	Bottom drift (mm)	Duration (s)	Anti-jamming activations
1L	4.0028	1.51	0.014	73.1	123.7	0
1R	4.0027	3.98	0.034	65.4	210.8	19
2L	4.0025	3.89	0.034	16.9	172.1	7
2R	4.0026	0.62	0.015	79.6	211.0	17
3L	4.0028	1.71	0.028	123.9	249.7	26
3R	4.0027	1.74	0.049	77.3	254.9	26
4L	4.0056	1.17	0.015	53.6	169.8	8
4R	4.0027	0.90	0.069	31.3	246.4	22
5L	4.0028	2.15	0.024	29.2	126.2	0
5R	4.0029	0.90	0.005	70.0	302.1	36
6L	4.0027	1.46	0.025	37.5	135.8	1
6R	4.0025	1.14	0.004	56.2	144.1	3

703 *Appendix D.2. Clearance, hydraulic demand and contact*

704 Table D.8 and Fig. D.12 detail the demonstration mission. Minimum
705 inflated barrier and stopping guard were -5.75 and $+4.72$ mm, with a 10 mm
706 recovery band. The largest clearance-estimation error divided by its allowance,
707 excluding this band, was 0.408. The per-axis orientation-correction error
708 bound was 2.5 mrad, which gives $\epsilon_\theta = \sqrt{3} \times 2.5 = 4.33$ mrad in Eq. (13).
709 The largest residual component was 2.18 mrad and the largest residual norm
710 2.26 mrad. Peak flow utilization was 0.486, with no force-limit relaxation; at
711 most 389 barrier rows were constructed and 132 retained per QP.

Table D.8 Minimum monitored clearances, taking the smaller value across booms. Policies apply to active collision pairs; designated tool-rock contacts and structural exclusions follow their respective contact rules.

Class	Policy (mm)	Minimum (mm)	Margin (mm)
Inter-boom	50	214.8	164.8
Active self-pairs	30	79.1	49.1
Carrier	50	198.5	148.5
Tunnel walls/roof	100	259.8	159.8
Floor	100	513.4	413.4
Nonpermitted face	30	86.5	56.5

712 Pre-contact speeds were evaluated over 0.3 s before front-contact/collaring
713 transitions. At contact detection, the largest absolute estimated gap divided by
714 its error allowance was 0.14. Left/right bit-force peaks reached 20.95/23.01 kN,
715 while maximum transverse stinger-tip displacement was 3.45 mm.

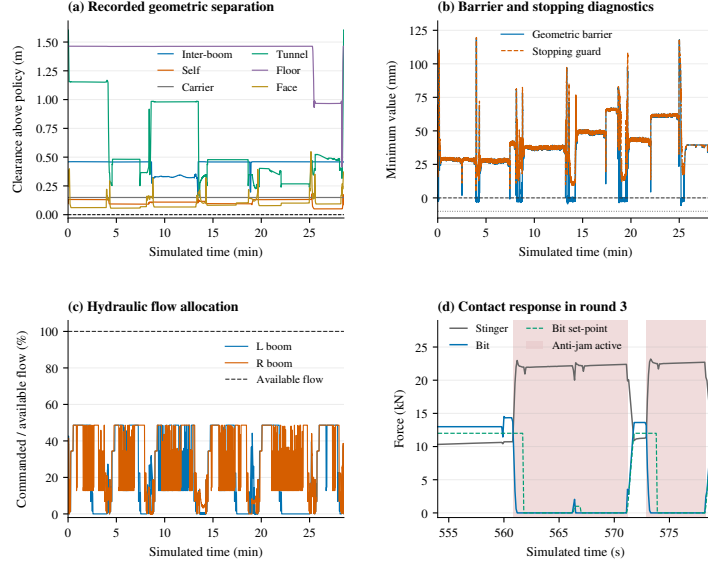


Fig. D.12. Demonstration mission: (a) clearance above each active class policy; (b) minimum inflated barrier and stopping guard, with the -10 mm recovery boundary; (c) flow normalized by available supply; and (d) left-boom contact forces, bit-force target and shaded anti-jamming intervals in round 3. Contact traces are sampled at 10 Hz; peak forces in the text use full-rate measurements.

716 Appendix D.3. Conflicting references and parameter perturbations

717 The geometric CBF used velocity-level geometric constraints in place of
 718 the proposed stopping reserve, actuator-response prediction, slew and braking
 719 treatment and hydraulic rows. An additional twelve-hole mission at 0.3 m
 720 depth also completed without inter-boom contact when inter-boom filtering
 721 and planning checks were removed.

722 Conflicting references drove both booms across the tunnel center with
 723 supervision bypassed. Closing speed used a centered 0.1 s distance secant
 724 at the first 200 mm separation (Fig. D.13). Proposed half/full-speed tests
 725 approached at approximately 180 mm s^{-1} . The geometric CBF at $\gamma = 20 \text{ s}^{-1}$
 726 approached at $889/1056 \text{ mm s}^{-1}$, reaching $0.88/-0.62 \text{ mm}$ minimum separation;
 727 the full-speed case recorded contact over twelve 1 ms steps. Removing
 728 inter-boom information also produced contact. At $\gamma = 5 \text{ s}^{-1}$, the geometric
 729 CBF kept $75.22/77.15 \text{ mm}$ at $867/983 \text{ mm s}^{-1}$. Slowing the reference with
 730 $\gamma = 20 \text{ s}^{-1}$ kept 55.29 mm at 321 mm s^{-1} . These cases show gain sensitivity
 731 and conservative speed regulation, including the effect of constraints from the
 732 nearby face.

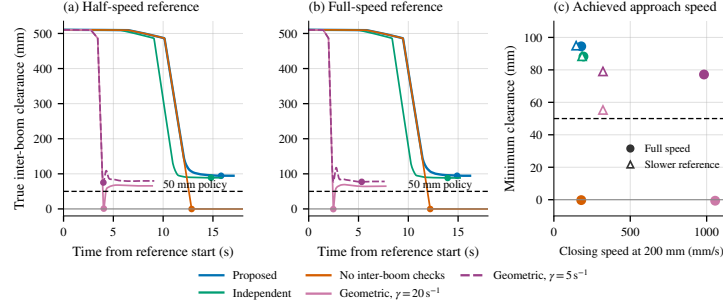


Fig. D.13. Conflicting references with route supervision bypassed: (a,b) inter-boom clearance during the first 18 s at half/full reference speed, with the 50 mm policy dashed; (c) achieved approach speeds for full and slower schedules, the latter lasting 5.5 times longer. Closing speed uses a centered 0.1 s interval at the first 200 mm crossing.

Increasing one valve gain by 15% and reducing the other pump capacity to 35% left 94.80 mm clearance with the proposed filter at 204 mm s^{-1} . In separate two-round, 0.3 m missions with both valve gains increased by 15%, its maximum support-approach speed was 9.5 mm s^{-1} . The geometric CBF reached 21.9 mm s^{-1} at support approach and 21.1 mm s^{-1} at collaring, against the 20 mm s^{-1} limit. Both drilled four holes; the geometric CBF returned home, while the return-home route of the proposed controller was rejected.

Appendix D.4. Computation and overrun-conditioned commands

The controller-core time is the wall-clock duration of one complete controller update, from the sampled measurements to the returned commands and progress rates. It comprises closure reconstruction and motion maps, orientation correction estimation, distance queries and constraint rows, the tracking and reduced-dynamics terms, and both assembly and solution of the QP, including the guard evaluation. The demonstration mission had mean/99th-percentile core times of 35.7/56.4 ms. Table D.9 reports separate reference and accelerated evaluations. Full accelerated 0.3 m missions used one numerical-library thread with dedicated computational resources; the accelerated 4 m round used default threading, and reference timing shared resources with another mission. The reported timings characterize controller-core workload under the stated hardware, threading, and resource-sharing conditions.

Overrun-conditioned substitution completed twelve 0.3 m holes in 489.08 s with three replans and no prohibited contact, compared with 452.57 s and one replan without substitution. All 2154 post-startup 50 ms cycles were

Table D.9 Measured 10 ms controller-core cycles. Full accelerated missions use 0.3 m holes; the accelerated 4 m test covers round 3. Substitution follows a detected overrun before the next synchronous plant step. The first two startup cycles are excluded; reference statistics also exclude one recorded cycle exceeding 1 s.

Run	Cycles	Mean (ms)	P99 (ms)	Max. (ms)	Over 10 ms
Reference, full 4 m mission	45 249	34.49	83.50	271.26	45 249 (100%)
Accelerated, full 0.3 m, no substitution	34 497	5.79	9.80	22.79	275 (0.797%)
Accelerated, full 0.3 m, substitution	38 141	5.83	9.98	35.77	375 (0.983%)
Accelerated, round 3 at 4 m	8 482	6.09	10.09	25.70	90 (1.061%)

757 within period, with a 10.41 ms maximum. The 377 substitutions included two
758 startup cycles of 59.07 and 62.74 ms.

759 Because the plant is stepped synchronously, the braking command was
760 substituted after computation and reference-clock advancement and before
761 the next plant step; deployment with a continuously evolving plant requires an
762 independently scheduled fallback and coordinated clock updates. Numerical
763 comparison of reference and accelerated evaluations satisfied 86 of 88 checks.
764 Two command differences exceeded the 10^{-5} normalized tolerance, with
765 maximum discrepancy 5.64×10^{-5} of nominal valve speed.

766 *Appendix D.5. Actuator-effort accuracy*

767 Predictions from Eq. (22) were compared with $f_j^h = D_{A,j}p_{A,j} - D_{B,j}p_{B,j}$,
768 sampled every 1 ms and averaged over a command period. The error, in
769 percent of port-relief effort, was $100|\langle f_j^h \rangle - \hat{f}_j^h| / \max(|F_j^-|, |F_j^+|)$. Alignment
770 included the one-period delay and retained complete, unchanged-mode periods
771 (Table D.10).

Table D.10 Maximum effort discrepancy normalized by port-relief effort. The first six rows compare nominal acceleration-effort predictions with period-mean chamber effort. Loaded closed-boom rows report chamber effort beyond rigid-model gravity; boom and feed groups are separate.

Condition	Error (%)
Nominal mission, free motion: boom actuators	3.10
Nominal mission, free motion: feed actuators	5.76
Dedicated nominal test: imposed ramp braking	4.78
Dedicated nominal test: abrupt valve closure	7.88
Unknown 300 kg payload per drill: ramp braking	18.64
Unknown 300 kg payload per drill: valve closure	20.12
Loaded drilling: closed boom actuators	39.0
Loaded drilling: rate-commanded feed	44.6

Nominal boom inertial correction peaked at 2.90% of relief effort, placing most free-motion demand in the gravity/friction contribution. Braking-row discrepancies relative to the first post-closure chamber-effort mean reached 9.8% nominally and 12.3% with known 300 kg payloads. Loaded-operation discrepancies quantify additional effort beyond the rigid positioning approximation. Nominal missions used the untightened effort rows and standard braking ramp.

Appendix D.6. Backup stops and capacity dependence

During positioning toward round 3, 3 s backups were imposed every 5 s. Inter-boom, self and carrier distances were monitored by active row; tunnel, floor and face distances used class minima. Utilization is the loss from committed-state estimated distance to minimum monitored stop distance, divided by the uninflated stopping reserve plus uncertainty allowance excluding the recovery band. Values above one identify reserve exceedance (Table D.11).

Table D.11 Forced-backup tests. Each row–stop check follows one collision row during one stop. Known/unknown denotes whether reduced relief settings are supplied to the controller. Combined conditions add 300 kg per drill, set pump capacity to 35%, increase valve gain by 15%, and apply sensor bias at its assumed bounds. Relief percentages are relative to nominal settings.

Condition	Stops	Row–stop checks	Exceedances	Max. utilization	Requested move
Nominal plant	19	795	0	0.36	Completed
Pump capacity 15%, unknown	19	703	0	0.42	Completed
Combined; relief 80%, unknown	16	507	0	0.40	Completed
Relief 50%, unknown	51	8950	15	2.84	Failed
Relief 50%, known; widening only	21	1476	17	3.27	Failed
Combined; relief 60%, unknown	9	259	22	6.92	Failed
Relief 50%, known; scaled ramp	13	228	0	0.35	Declined [†]

[†]The requested round was rejected; reported stops occurred during the subsequent return home. Additional configurations assessed known payload and combined known capacity.

Nominal stops reached standstill within 0.69 s. Successful tests with adequate pressure headroom began at estimated rates up to 0.44 of nominal valve speed, within the filter’s 0.6 limit. Capacity reductions identify the operating boundary: at 50% relief, reserve exceedances occurred with both unknown limits and known limits using force-row widening. Under combined perturbations at 60% relief, roll holding capacity was lost before braking and monitored self-clearance reached approximately -185 mm. This geometric monitor captures within-boom overlap independently of the plant’s inter-body contact counter.

795 With known capacity, an optional slower ramp increased reserved travel.
796 At 60% relief without combined perturbations, the requested move com-
797 pleted with a ramp factor up to 4.11 and no reserve exceedance. More
798 severe known-capacity cases were rejected in planning, with subsequent re-
799 turn/hold outcomes reported separately. These tests used capacity adaptation
800 in addition to the nominal controller.

801 *Appendix D.7. Barrier and recovery diagnostics*

802 The proposed concurrent run in Table 2 completed 69 537 successful QP
803 cycles, with minimum inflated barrier -5.16 mm, minimum stopping guard
804 $+3.95$ mm, and maximum clearance-error/allowance ratio 0.474. In unchanged-
805 mode 10 ms cycles, next-cycle shortfall from the previous target had 1.43 mm
806 99th percentile and 4.60 mm maximum. At hold-mode transitions, minimum
807 barrier decreased by up to 28.6 mm, remaining positive immediately afterward.
808 These sampled values show how closely the recursion in Eq. (C.4) held,
809 including the effect of contact-induced motion of nominally closed actuators.

810 Policy-clearance steps of 6/9 mm created approximately 3/6 mm barrier
811 deficits; first nonnegative returns occurred after 0.15/0.23 s. A 40 mm step
812 activated the guard for two cycles. Inter-boom separation remained above
813 97 mm.

814 **Appendix E. Cross-engine verification protocol**

815 The exported representation contains 63 rigid bodies, 60 tree coordinates
816 (37 revolute and 23 prismatic), two fixed tree joints and ten loop joints, includ-
817 ing ten auxiliary links of total mass 0.10 kg. Collision geometry comprises 256
818 convex pieces, four capsules, forty boxes and one face mesh, with 305 filtered
819 link pairs. Body and joint names, quaternion conventions and coordinate
820 signs were matched before comparison. Tests used Isaac Sim 5.1.0 with CPU
821 physics.

822 *Prescribed-state geometry.* Each retained configuration was assigned with
823 gravity and loop enforcement disabled. Link poses and contacts were sampled
824 after a 1 ms step and one manifold-refresh step. GJK closest-distance queries
825 used PhysX poses and cooked hulls; Coal reference queries used the exported
826 shapes. Conversion of 156 controller convex pieces to 256 exported pieces
827 introduced at most 3.20 mm reduction deviation; cooking added at most
828 4.23 mm inward deviation. All cooked hulls were available, and the remaining
829 shapes retained their authored geometry.

Closest-distance agreement and contact reporting were evaluated separately. Initial left-face manifold separation lay up to 108.2 mm below the reference distance. After refresh, all thirteen classes were reported at every comparable state, with separation-minus-reference differences from -0.184 to $+57.86$ mm. Figure E.14 compares these quantities.

Tree dynamics. Queries at 24 stored states used disabled loops and collisions. For MuJoCo and PhysX mass matrices M^{MJ} and M^{PX} , and diagonal MuJoCo armature A ,

$$\epsilon_M = \max_{k,i,j} \frac{\left| M_{ij}^{\text{PX}}(k) - \left(M^{\text{MJ}}(k) - A \right)_{ij} \right|}{\sqrt{M_{ii}^{\text{MJ}}(k) M_{jj}^{\text{MJ}}(k)}}. \quad (\text{E.1})$$

The target excludes armature, while normalization retains the recorded MuJoCo diagonal; retaining armature in the target gives approximately 0.908. Gravity and Coriolis errors use $\epsilon_f = \max_k \|f^{\text{PX}}(k) - f^{\text{MJ}}(k)\|_\infty / \|f^{\text{MJ}}(k)\|_\infty$ with matched signs and fixed SI coordinates.

Closed-chain equilibrium. The home hold enabled gravity and all ten loops, using the prescribed load-dependent support model, implicit position drives, a 1 ms step, 64 position iterations and one velocity iteration. External forces were applied at every solver iteration. Friction and limits were disabled; drives held actuator and coupled feed coordinates at home, with equality holders in MuJoCo.

Final-second excursions were bounded by $36.1 \mu\text{rad}$ and $3.58 \mu\text{m}$. Table 4 uses position-derived speeds over ≥ 0.1 s; angular maxima over 0.02 s and instantaneously were 1.27×10^{-3} and 8.97×10^{-3} rad/s. Equilibrium efforts average every final-second step. The 16 force and four torque channels include lift/tilt cylinders at approximately 132.3/15.1 kN each. The 2% tolerance governed the lifts; absolute tolerances governed the other eighteen channels, including sixteen lightly loaded channels. Force standard deviation reached 10.2 kN. Measured joint efforts passed all twenty mean-load comparisons; the drive spring component passed eight.

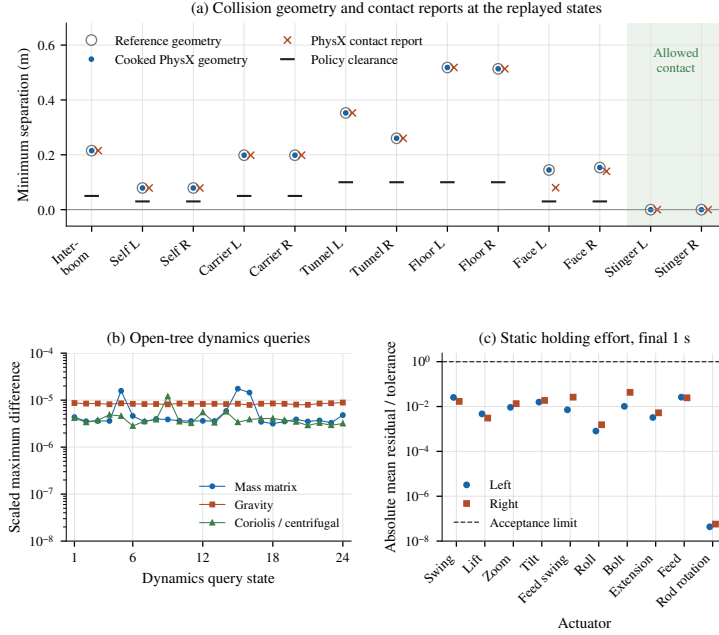


Fig. E.14. Cross-engine diagnostics: (a) closest distances and contact reports for eleven prohibited classes and two permitted stinger contacts; (b) open-tree dynamics with armature excluded from the reference matrix; (c) final-second mean effort residuals divided by channel tolerance (threshold: unity).

Appendix F. Protocol and diagnostics of the 100-collar campaign

Appendix F.1. Target selection, conditions and completion

The 100-collar pattern was adapted to the modeled rig through nominal-model reachability, entry/exit and docking checks: 23 collars were relocated, and 15 were assigned across the center line. Target and access checks covered all three face reliefs; dynamic look-ahead screening used S1. The paired order exercised conflicting transitions and varied postures. The 4 m depth parameter defined the remaining-drilling envelope checked before feed extension; each executed operation comprised positioning, docking, holding and retraction.

Conditions S1, S2 and S3 used seed tuples for sensing, valves and face relief of (11, 101, 2026), (12, 102, 2027) and (13, 103, 2028). Directional-valve gains were independently drawn from $[0.95, 1.05]$ and held fixed per run, while the controller used nominal gains. The pressure-controlled feed-extension branch retained its nominal mapping. The campaign used a 1.30 stopping-reserve multiplier, compared with 1.25 in the twelve-hole mission. The former is a prescribed design reserve motivated by $1.229 \times 1.05 \simeq 1.290$.

873 Load establishment required front force above 70% of the 10 kN loading
874 target after at least 1 s in the loading phase, with feed extension below
875 2 mm s^{-1} for 0.05 s. Completion required the full 2 s hold, total stinger-plus-
876 bit load of at least 4 kN at every controller-cycle hold sample, and retraction.
877 This process criterion was evaluated separately from placement accuracy and
878 clearance compliance. S2 round 39 and S3 round 20 each contributed two
879 skipped targets after planning/replanning failed. S2 round 31 and S3 round 25
880 each contributed one right-boom hold with a recorded zero-load sample. The
881 resulting counts are 100/97/97 for A. F likewise had one below-threshold
882 hold, plus two rejected docking geometries. The criterion is evaluated at every
883 controller cycle and therefore detects brief load drops that fall between stored
884 trajectory samples.

885 *Appendix F.2. Controller variants and supervisory refinement*

Table F.12 Controller configurations in the 100-collar campaign. Supervised variants A, B, C and E all evaluate candidate routes with the full actuator-aware filter. All variants retain phase supervision, actuator command bounds, stroke/joint limits and pre-extension docking guards.

Variant	Route selection	Online control
A	Supervised	Full actuator-aware collision, effort and permitted-contact constraints.
B	Supervised	Collision classes removed; limit, effort, valve/flow, slew and permitted-contact constraints retained.
C	Supervised	Kinematic CBF with $\gamma = 20 \text{ s}^{-1}$, valve/flow bounds and kinematic permitted-contact constraints.
D	Direct	Full actuator-aware filter; direct joint-space references.
E	Supervised	Full filter with estimated-error/geometry allowances set to zero, including the contact-gap allowance; recovery band and stopping inflation retained.
F	Direct	Same retained online constraints as B; direct joint-space references.

886 For C, the geometric/limit rows use $Gc \geq -\gamma \max(d - D, 0)$, with policy
887 distance D for collision rows and zero for limits. G stacks the actuator-
888 coordinate constraint gradients, and the inequality acts componentwise. This
889 formulation regulates geometric velocity and contact approach; the full for-
890 mulation additionally represents delayed actuator response, slew/braking,
891 nominal effort and uncertainty allowances. E keeps the 10 mm recovery band
892 and the 1.30 stopping inflation, and its phase supervision still uses the full
893 gap-uncertainty calculation. The geometric CBF of the twelve-hole mission
894 kept its stated uncertainty allowances. A, B, D, and F form a two-factor com-
895 parison of supervision and online collision rows, with their other constraints
896 in common.

Pilot trials refined the target rolls and supervisory rules before the reported comparisons. The study-specific supervisor in Section 6 added a 4.33 mrad planning reserve to ϵ_θ in its look-ahead, for all rows except the inter-boom rows. Its look-ahead screened persistent slow progress at 3% of nominal actuator speed and 15% reference-clock rate for 3 s, then evaluated alternative routes. Pilot outcomes were excluded from the campaign statistics.

One start-clearance rule was amended during the reported campaign. The final precheck uses its nominal 100 mm inter-boom threshold when the starting separation meets that threshold; otherwise the threshold is $\max(50 \text{ mm}, d_0 - 5 \text{ mm})$, where d_0 is the initial separation. C was restarted, A/S2 continued from its saved state at 1640 s, and A/S3 and E used the amended rule. The completed A/S1 and B runs were kept because none of their recorded planning calls started in the amended condition, and D and F use direct references. All eight reported runs share the final target sequence.

Appendix F.3. Placement and geometric monitoring

Table F.13 Accuracy and contact statistics. Collar and axis entries are median/95th percentile/maximum over completed holds. Peak stinger/bit forces are separated; minimum front load uses recorded samples from completed holds, and slip is maximum transverse stinger motion.

Run	Collar error (mm)	Axis error ($^\circ$)	Peak forces (kN)	Min. load (kN)	Max. slip (mm)
A/S1	1.56/4.01/13.60	0.044/0.083/0.284	19.2/18.2	8.71	0.23
A/S2	1.58/6.08/18.06	0.041/0.132/0.205	23.3/18.9	8.76	0.26
A/S3	1.56/7.70/24.51	0.041/0.116/0.234	19.8/15.1	8.45	1.78

Table F.13 lists the accuracy and contact statistics of the full framework, and Fig. F.15 compares the three conditions. The 294 completed holds form a pooled descriptive sample, with 94 targets common to all three missions.

Clearances were evaluated at controller cycles using plant body poses. Stored 0.1 s windows retain each class minimum; collision contacts were recorded at the 1 ms plant step. Table F.14 and Fig. F.16 show the resulting sampled geometric envelope. For A, 908 886 filter cycles had no guard or solver fallback; maximum measured clearance-error/allowance ratios were 0.91, 0.49 and 0.85 across S1–S3.

A separate triangle-mesh audit evaluated inter-boom, same-boom and carrier pairs at 9223, 3131 and 3061 configurations in A/S1–S3, respectively, and found no intersecting pair. B, C, D, and E likewise had no intersection over 1122, 1045, 426 and 1313 audited states. Audited minimum inter-boom

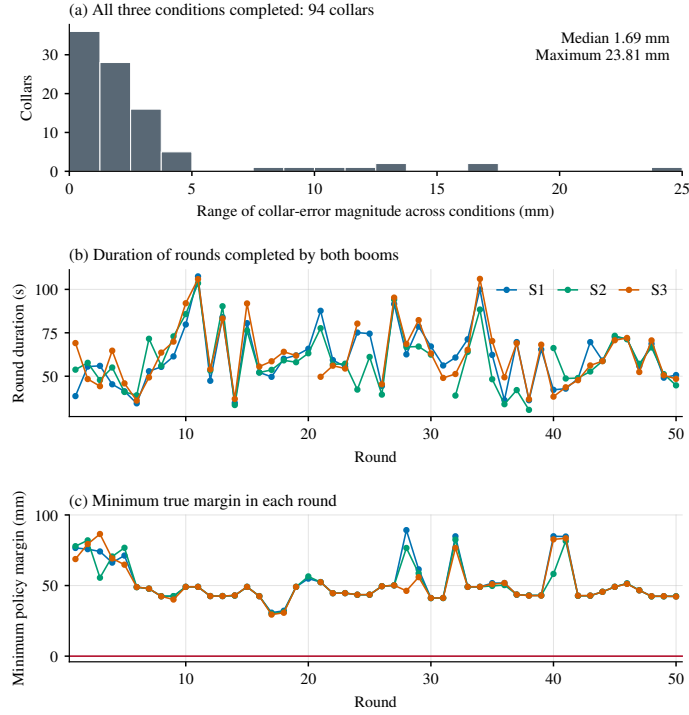


Fig. F.15. Full-framework condition sensitivity: (a) range of collar-error magnitude across S1–S3 for the 94 targets completed in all conditions; (b) durations of rounds completed by both booms; (c) minimum clearance excess over policy in each round. Conditions jointly vary sensing noise, valve gains and face relief.

Table F.14 Minimum monitored clearance in millimeters, with class policy in parentheses. Distances use plant configurations and active convex collision geometry; designated contact pairs follow their permitted-contact rules.

Run	Inter-boom (50)	Self (30)	Carrier (50)	Tunnel (100)	Floor (100)	Face (30)
A/S1	101.2	60.8	195.4	148.7	224.6	89.3
A/S2	94.9	60.0	189.6	173.1	160.8	88.9
A/S3	100.9	59.4	197.5	171.0	306.4	70.1
B/S1	103.3	59.4	194.9	155.8	226.0	89.2
C/S1	101.1	56.3	195.3	155.7	225.3	89.2
D/S1	162.7	61.1	198.5	362.8	1527.6	74.3
E/S1	82.4	60.8	195.3	151.2	225.3	89.2
F/S1	-0.6	-298.0	191.5	-131.4	321.4	-57.6

925 mesh distances for A were 126, 122 and 122 mm; the controller’s enclosing

926 convex geometry produced the smaller sampled distances in Table F.14.
927 Environmental clearance used the plant-geometry monitor. Within-boom
928 overlap was evaluated geometrically.

929 F recorded 73.365 s of plant contact, 122.12 s of monitored penetration
930 and 158.05 s below at least one policy distance. Its policy-violation durations
931 by class were 27.54/49.71/72.67/18.45 s for inter-boom/self/tunnel/face; these
932 intervals can overlap. The final return home contributed 1.91 s of penetration
933 outside the paired rounds. A focused triangle audit over 3105 event-window
934 states found 29 intersecting body pairs: one inter-boom and 28 within-boom
935 pairs. This count and the 29 affected rounds are different groupings of the
936 same events and coincide only in number.

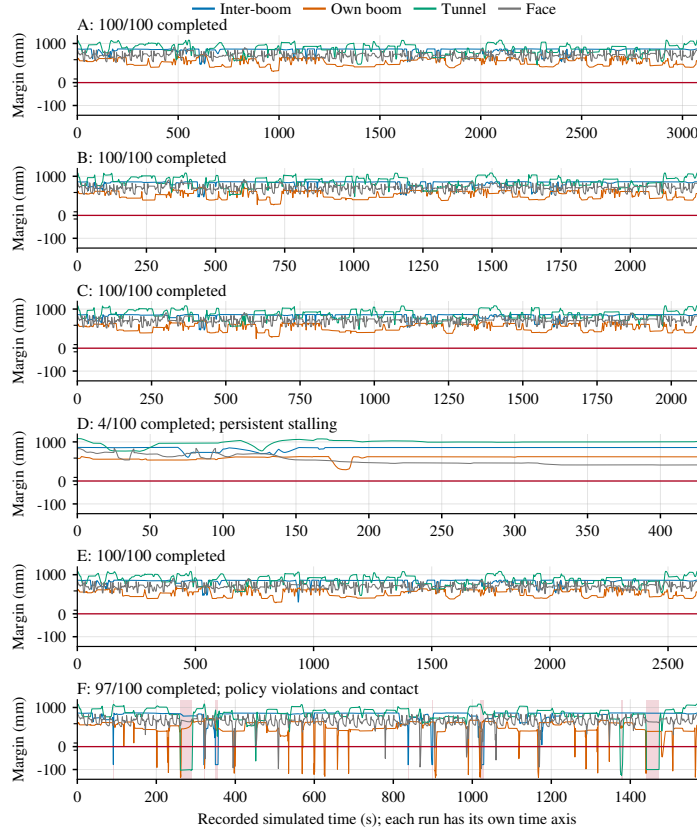


Fig. F.16. S1 clearance histories: each point retains the minimum excess over policy within a 0.1 s window, plotted at its endpoint. The symmetric logarithmic axis is linear within ± 50 mm; shading marks plant-contact intervals. Time axes follow each execution. Carrier and floor minima are included in Table F.14.

937 *Appendix F.4. Planning and computation*

938 The plant was paused during planning, so mission durations measure
939 synchronous simulated execution. Supervised planning required 139–167 s
940 median computation per round on shared resources, with maximum 1497 s.
941 Core mean/99th-percentile times for A/S1–S3 were 38.3/65.8, 41.8/71.4 and
942 38.1/65.2 ms. Full-framework motion/reference-duration ratios were 1.66, 1.56
943 and 1.66; S1 values for B/C/D/E/F were 1.06/1.05/2.54/1.43/1.16.

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