

Electronic Supplementary Information
Tunable Intermediate-Logic Ternary Circuits based on MoSe₂-WSe₂
Heterojunction

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Table S1. Field effect mobility of the WSe₂, MoSe₂, and MoSe₂-WSe₂ vdW-H.

Channel layer	Linear regime		Saturation regime	
	(V _D = 1 V)		(V _D = 20 V)	
	μ_{electron} (cm ² V ⁻¹ s ⁻¹)	μ_{hole} (cm ² V ⁻¹ s ⁻¹)	μ_{electron} (cm ² V ⁻¹ s ⁻¹)	μ_{hole} (cm ² V ⁻¹ s ⁻¹)
MoSe ₂	46.79	0.04	20.62	0.23
WSe ₂	1.63	34.47	2.39	24.36

Field effect mobility (μ_{eff}) is one of the parameters for evaluating the performance of transistors. It can be extracted from $\mu_{\text{eff}} = \frac{\partial I_D}{\partial V_G} \frac{L}{W} \frac{1}{C_{\text{ox}} V_D}$, where L and W are the channel length and width, respectively, and C_{ox} is the capacitance of the gate insulator.^{S1} Regarding the drain voltage applied to the MoSe₂-WSe₂ vdW-H transistor in Figure 1e, μ_{eff} is extracted from the saturated drain current ($V_D = -20$ V). The calculated μ_{eff} of the baseline MoSe₂ and WSe₂ transistors as a function of V_G is shown In Table S1. As a result, the MoSe₂ and WSe₂ transistors exhibit n-type dominant and p-type dominant behaviors, respectively.

Table S2. Comparison of the proposed H-TR with previous studies on heterojunction transistors for ternary inverter operation.

P-type material (or ambipolar)	N-type materials (or ambipolar)	Dielectric	g_m [μ S/F]	Negative g_m region [V]	Year	Ref.
WSe ₂ (ambipolar)	MoS ₂	HfO ₂	No length	~0.1	2016	[22]
Graphene	Graphene	SiO ₂	No length	~20	2016	[38]
WSe ₂	Graphene	SiO ₂	$\sim 4.3 \times 10^{-4}$	~15	2017	[19]
Black phosphorus (ambipolar)	MoS ₂	HfSiO	$\sim 1.2 \times 10^{-5}$	~1.5	2017	[18]
Black phosphorus	SnSeS	HfO ₂	$\sim 1.4 \times 10^{-4}$	~2	2018	[29]
Graphene	R6G /graphene	ODTS/SiO ₂	$\sim 2.6 \times 10^{-3}$	~18	2018	[27]
MoTe ₂	MoS ₂	h-BN/SiO ₂	-	~20	2019	[28]
MoTe ₂	MoS ₂	SiO ₂	$\sim 6.4 \times 10^{-7}$	~8	2019	[26]
Graphene	Graphene	SiO ₂	$\sim 1.7 \times 10^{-2}$	~13	2019	[39]
Black phosphorus (ambipolar)	ReS ₂	HfO ₂	$\sim 1.7 \times 10^{-3}$	~2	2020	[23]
Black phosphorus	MoS ₂	SiO ₂	$\sim 1.8 \times 10^{-4}$	~10	2020	[42]
WSe ₂	ReS ₂	SiO ₂	$\sim 1.5 \times 10^{-4}$	~43	2020	[43]
WSe ₂ (ambipolar)	MoSe ₂ (ambipolar)	SiO ₂	$\sim 1.1 \times 10^{-2}$	~45	2020	This work

Table S3. Comparison of the T-inverter with previous studies on ternary inverters.

Pull-up transistor	Pull-down transistor	Output swing	Pulsed measurement	Middle logic state [V]	Tunability of intermediate-state	Ref.
WSe ₂	WSe ₂ /MoS ₂ C-Hetero	~75%	X	0.7	X	[22]
Graphene	Graphene	~40%	X	0.6	X	[38]
BP	BP/ ReS ₂ C-Hetero	~75%	X	4	X	[25]
BP	Graphene/ Wse ₂	~75%	X	15	X	[19]
BP	BP/MoS ₂ C-Hetero	~90%	X	0.4	X	[18]
BP	BP/SnSeS	~50%	X	1.2	X	[29]
Graphene/R6G/ graphene	R6G/ graphene	~10%	X	20	X	[27]
MoTe ₂	MoTe ₂ /MoS ₂	~70%	X	9	X	[28]
MoTe ₂	MoTe ₂ /MoS ₂	~60%	X	18	X	[26]
ReSe ₂	IGZO	~97%	O	1.5	X	[30]
BP	BP/ReS ₂	~90%	O	1.5	X	[23]
BP	BP/MoS ₂	~40%	X	5	X	[42]
MoSe ₂ /WSe ₂	MoS ₂	~100%	O	34	O	This work

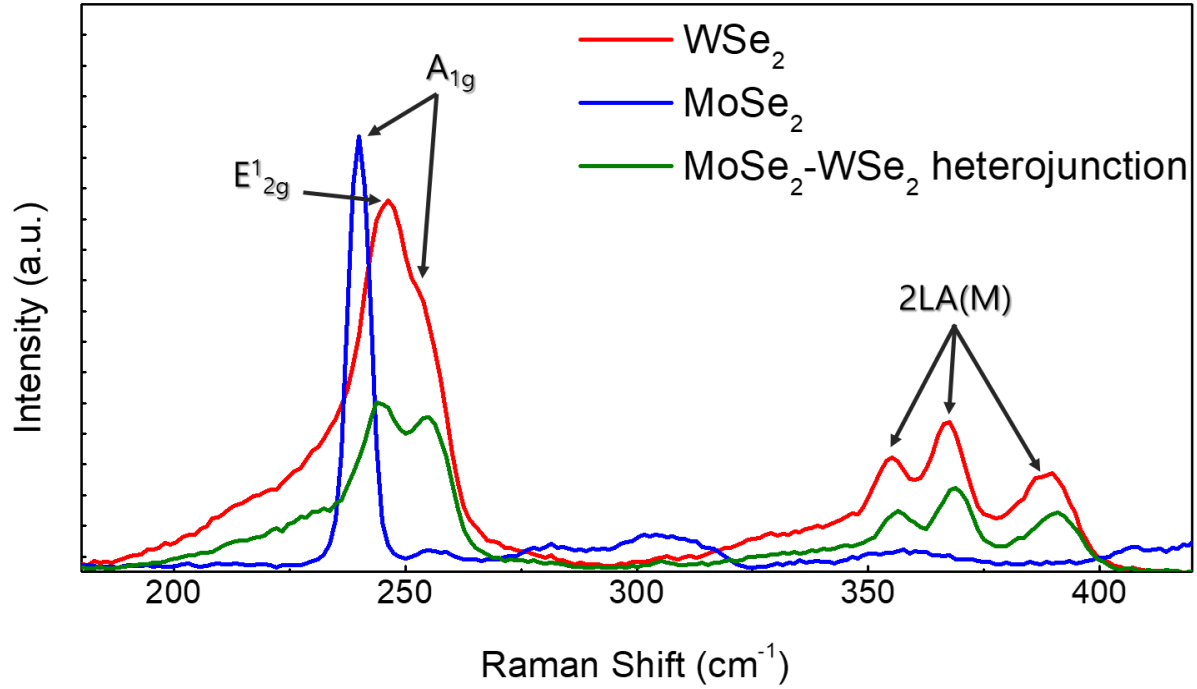


Figure S1. Raman spectra of WSe₂, MoSe₂, and MoSe₂-WSe₂ vdW-H. The Raman spectra were measured at three different positions of the WSe₂, MoSe₂, and MoSe₂-WSe₂ vdW-H regions as shown in Figure S1. The observed Raman peaks (red curve) of the WSe₂ at 246.3 and 253.8 cm⁻¹ correspond to the E¹_{2g} and A_{1g} vibrational modes, respectively. The E¹_{2g} mode arises from the vibrations involved in both W and Se atoms in the basal plane. These vibrations are in the opposite directions from each other.^{S2,3} The A_{1g} mode refers only to the vibrations of the Se atoms along the perpendicular to plan. The other peaks (2LA (M) modes) are the second-order Raman mode due to LA (longitudinal acoustic) phonons at the M point in the Brillouin zone and combinational Raman modes.^{S2,3} The Raman peak of MoSe₂ (blue curve) was observed at 239.9 cm⁻¹ corresponding to the A_{1g} modes due to the out-of-plane vibration. In-plane vibration was not observed.^{S4} In the MoSe₂-WSe₂ region, the Raman peaks corresponding to both WSe₂ and MoSe₂ appeared and there was no significant shift of these peaks. This supports that the MoSe₂-WSe₂ was having van der Waals interaction without the new bond between the WSe₂ and MoSe₂.

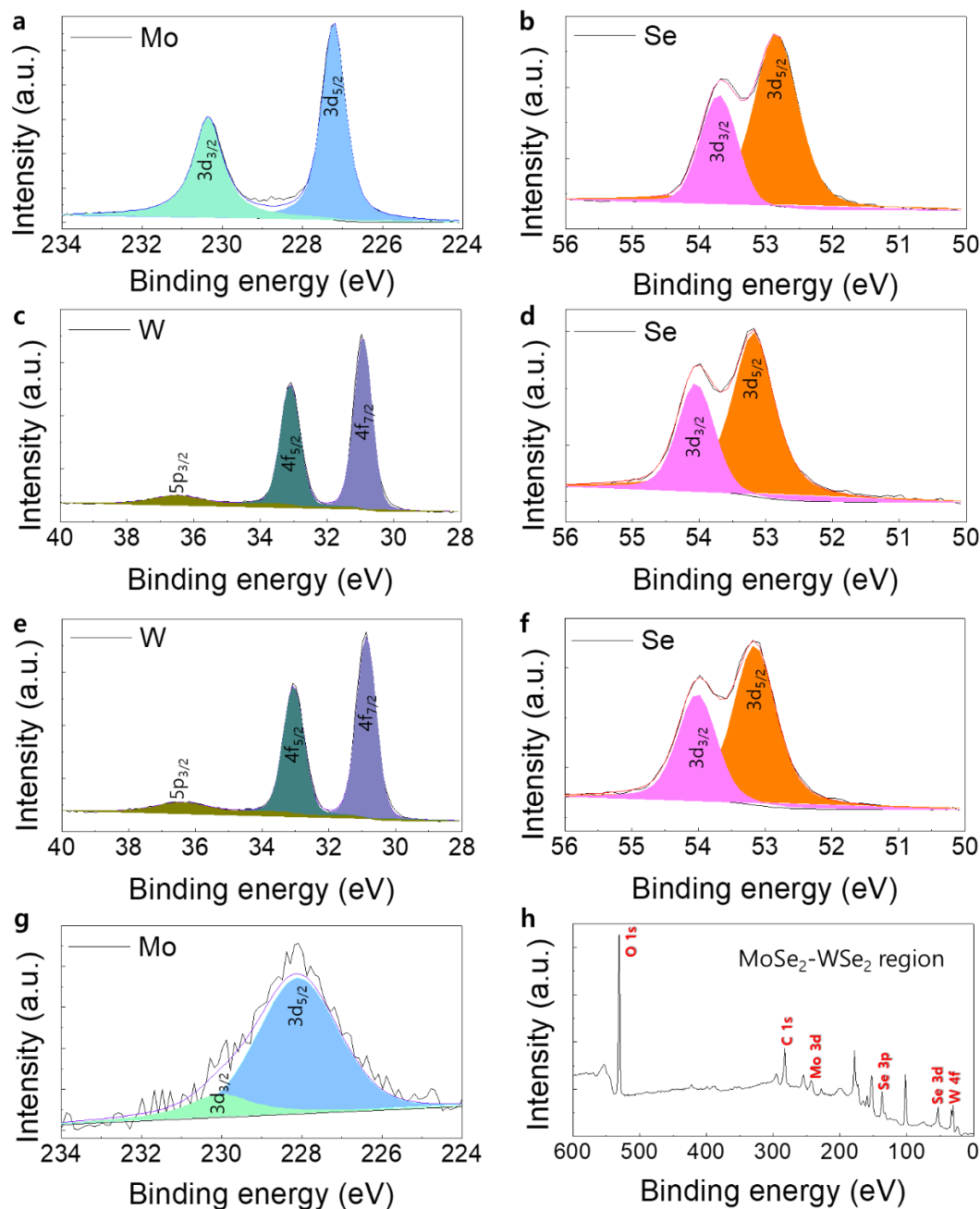


Figure S2. XPS spectra of WSe_2 , MoSe_2 , and $\text{MoSe}_2\text{-WSe}_2$ vdW-H. a) Mo 3d and b) Se 3d binding energies for MoSe_2 . c) W 4f, 5p and d) Se 3d binding energies for WSe_2 . e) W 4f, 5p, f) Se 3d, g) Mo 3d, and h) XPS survey scans for the $\text{MoSe}_2\text{-WSe}_2$ vdW-H region. X-ray photoelectron spectroscopy (XPS) was applied to examine the binding energies of MoSe_2 , WSe_2 , and the $\text{MoSe}_2\text{-WSe}_2$ vdW-H. For the WSe_2 , the observed peaks of W at 30.8 and 33.0 eV correspond to the $4f_{7/2}$ and $4f_{5/2}$ binding energies, respectively, and the observed peak at 36.4 eV corresponds to the $5p_{3/2}$ binding energy. Two peaks representing the $3d_{5/2}$ and $3d_{3/2}$ binding energies

of Se are observed at 53.1 and 54.8 eV, respectively (Figure S2a and S2b).^{S5,6} For the MoSe₂, the observed double peaks of Mo at 227.2 and 230.2 eV correspond to the 3d_{5/2} and 3d_{3/2} binding energies, respectively. The two peaks of Se corresponding to the 3d_{5/2} and 3d_{3/2} binding energies observed at 52.8 and 53.6 eV, respectively (Figure S2c and S2d).^{S5,6} In the MoSe₂-WSe₂ vdW-H region, all three elements (W, Se, and Mo) were observed. The two peaks representing the 4f_{7/2} and 4f_{5/2} binding energies of W are observed at 30.8 and 33.0 eV, respectively (Figure S2e). Two peaks corresponding to the 3d_{5/2} and 3d_{3/2} binding energies of Se are observed at 53.0 and 54.0 eV, respectively (Figure S2f). The 3d_{5/2} and 3d_{3/2} binding energies of Mo are weakly observed at 228.0 and 230.0 eV, respectively. The presence of W, Mo, and Se elements was clearly confirmed through the XPS survey scan (Figure S2g and S2h).

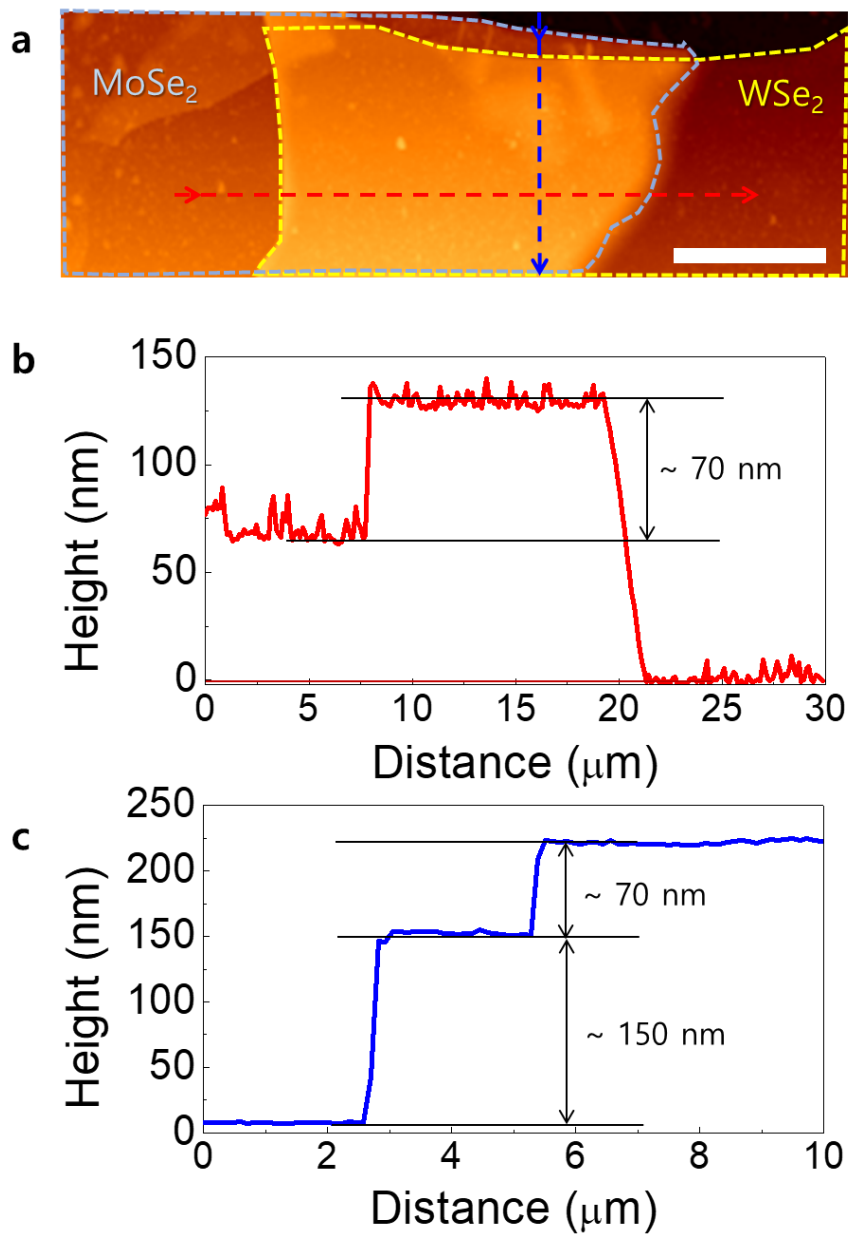


Figure S3. Thickness of MoSe₂ and WSe₂ vdW-H. a) AFM image of the MoSe₂ (grey dashed line)-WSe₂ (yellow dashed line) vdW-H. The length of the scale bar is 5 μm. Cross-section profile along b) red dashed line (x-axis scan) and c) blue dashed line (y-axis scan) in the AFM image of MoSe₂-WSe₂ vdW-H. The thicknesses of the WSe₂ and MoSe₂ were measured to be about 70 and 150 nm, respectively, using the profile (blue dashed line) of the AFM image.

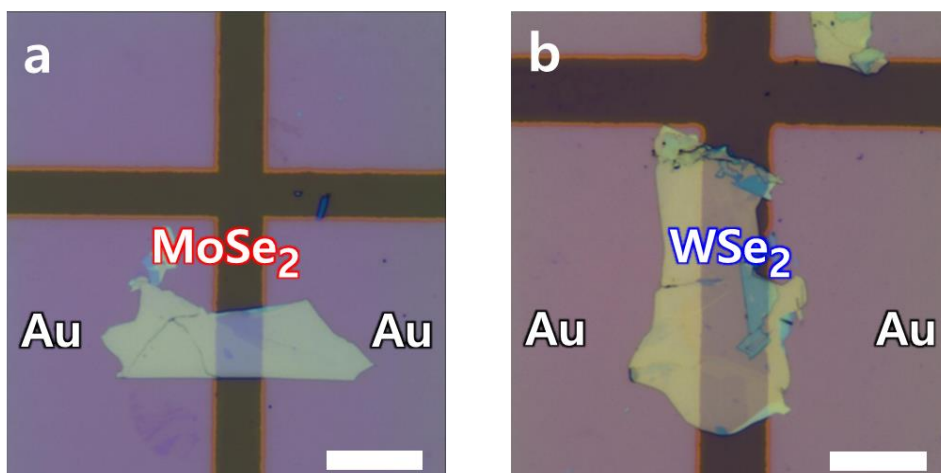


Figure S4. Optical microscope images of a) baseline MoSe_2 transistor and b) baseline WSe_2 transistor. The length of the scale bar is 30 μm .

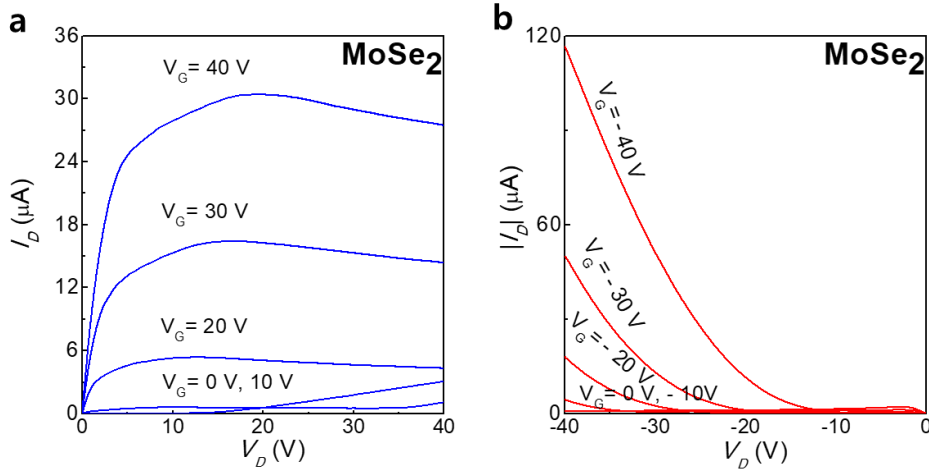


Figure S5. Output characteristics of the baseline MoSe₂ transistor a) for $V_D = 0$ to 40 V and $V_G = 0, 10, 20, 30, \text{ and } 40 \text{ V}$ and b) for $V_D = 0$ to -40 V and $V_G = 0, -10, -20, -30, \text{ and } -40 \text{ V}$.

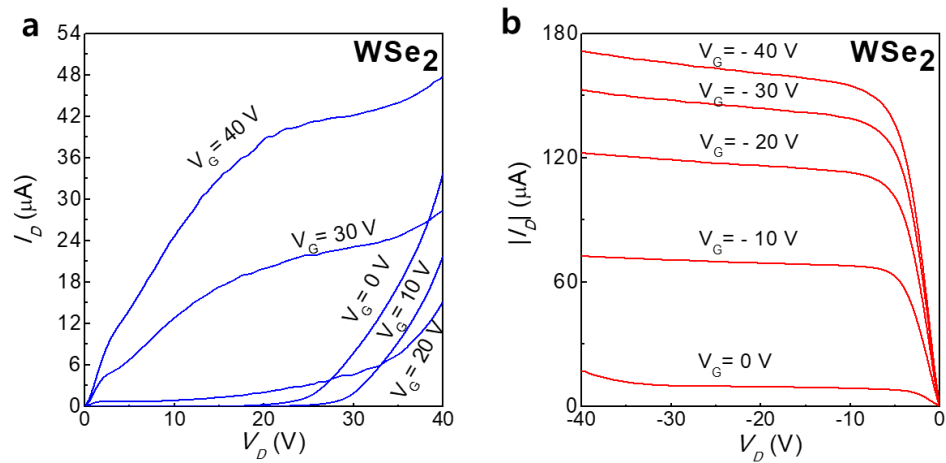


Figure S6. Output characteristics of the baseline WSe₂ transistor a) for $V_D = 0$ to 40 V and $V_G = 0, 10, 20, 30, \text{ and } 40 \text{ V}$ and b) for $V_D = 0$ to -40 V and $V_G = 0, -10, -20, -30, \text{ and } -40 \text{ V}$.

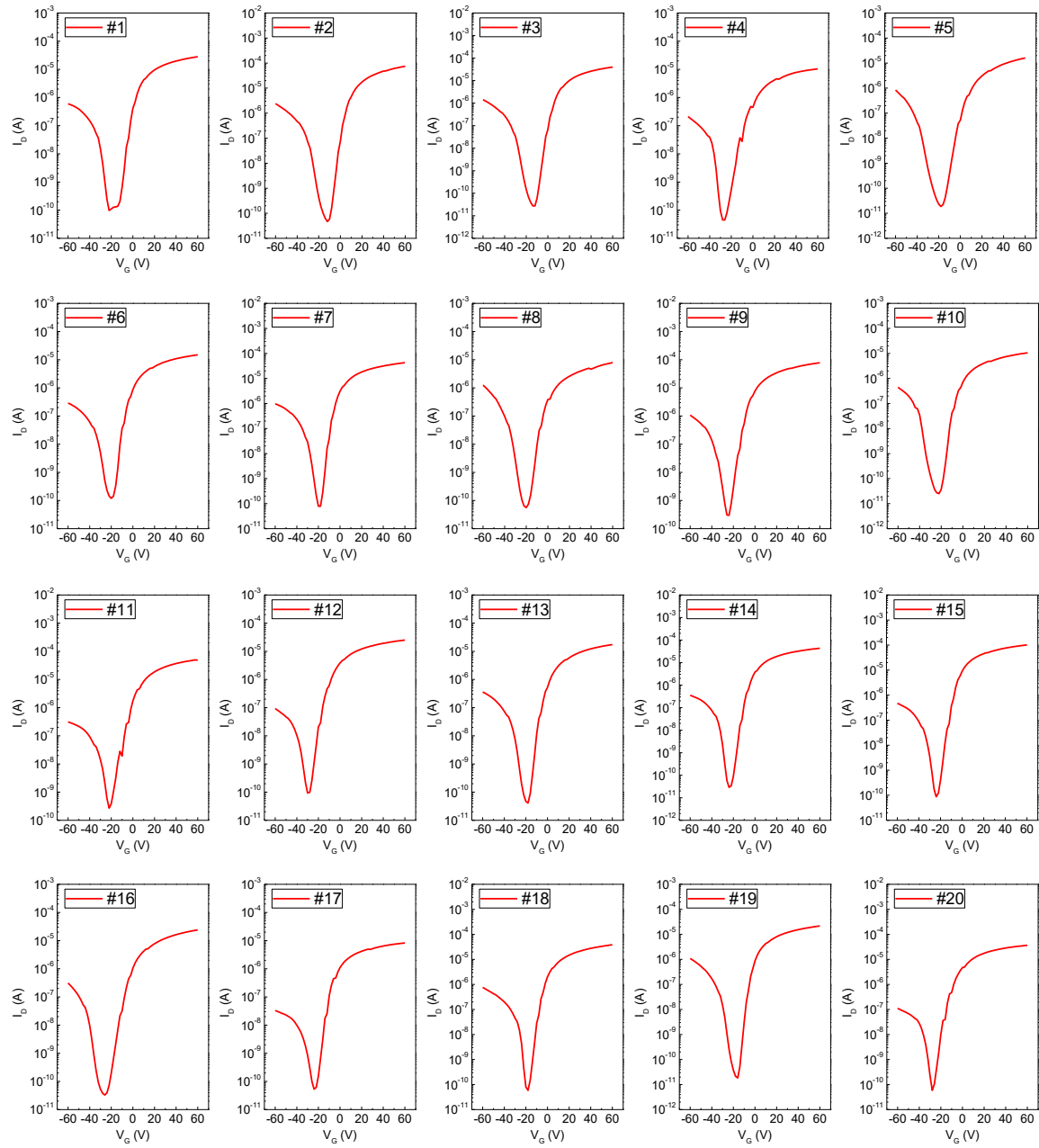


Figure S7. Transfer characteristics of 20 baseline MoSe₂ transistors.

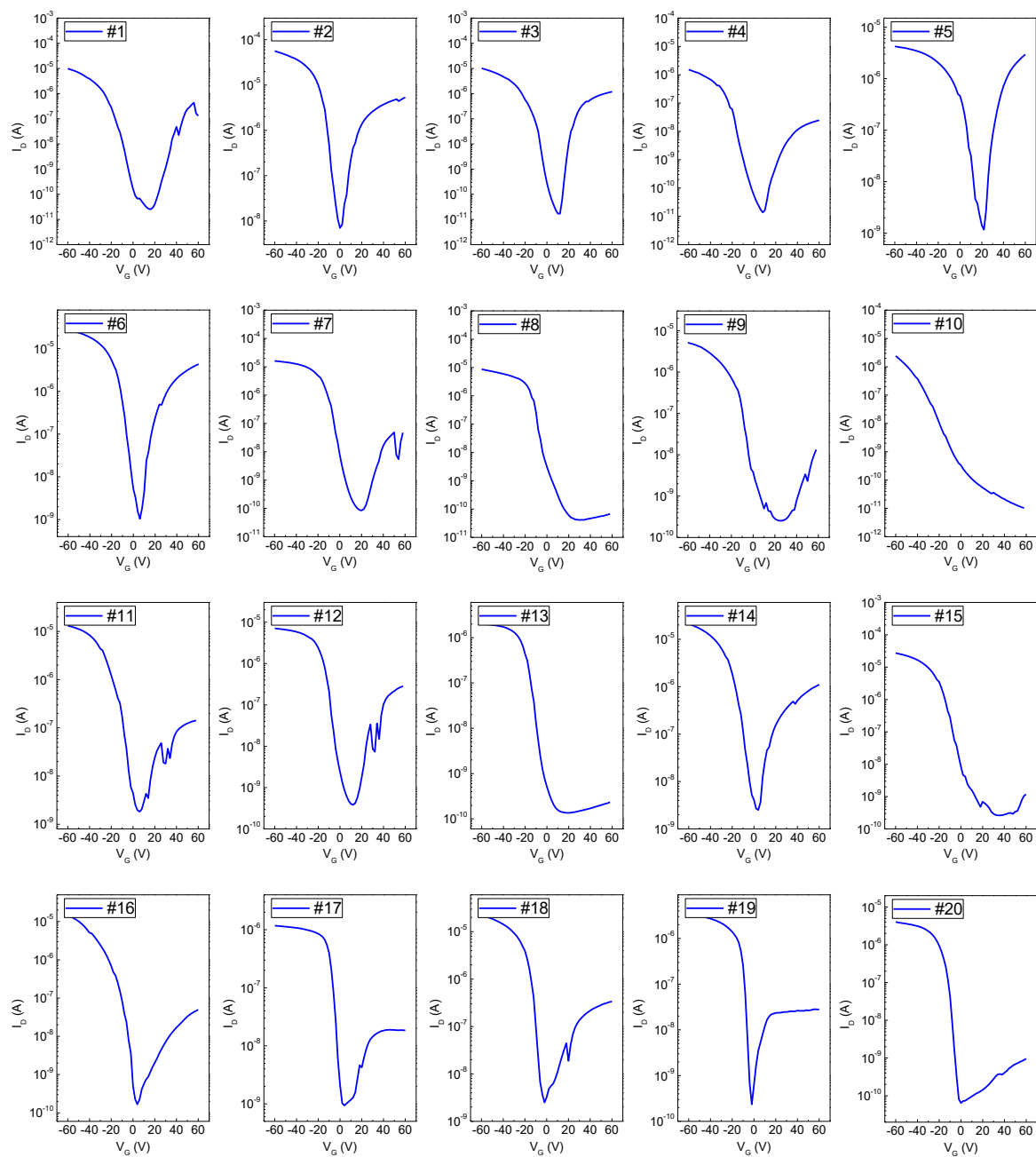


Figure S8. Transfer characteristics of 20 baseline WSe₂ transistors.

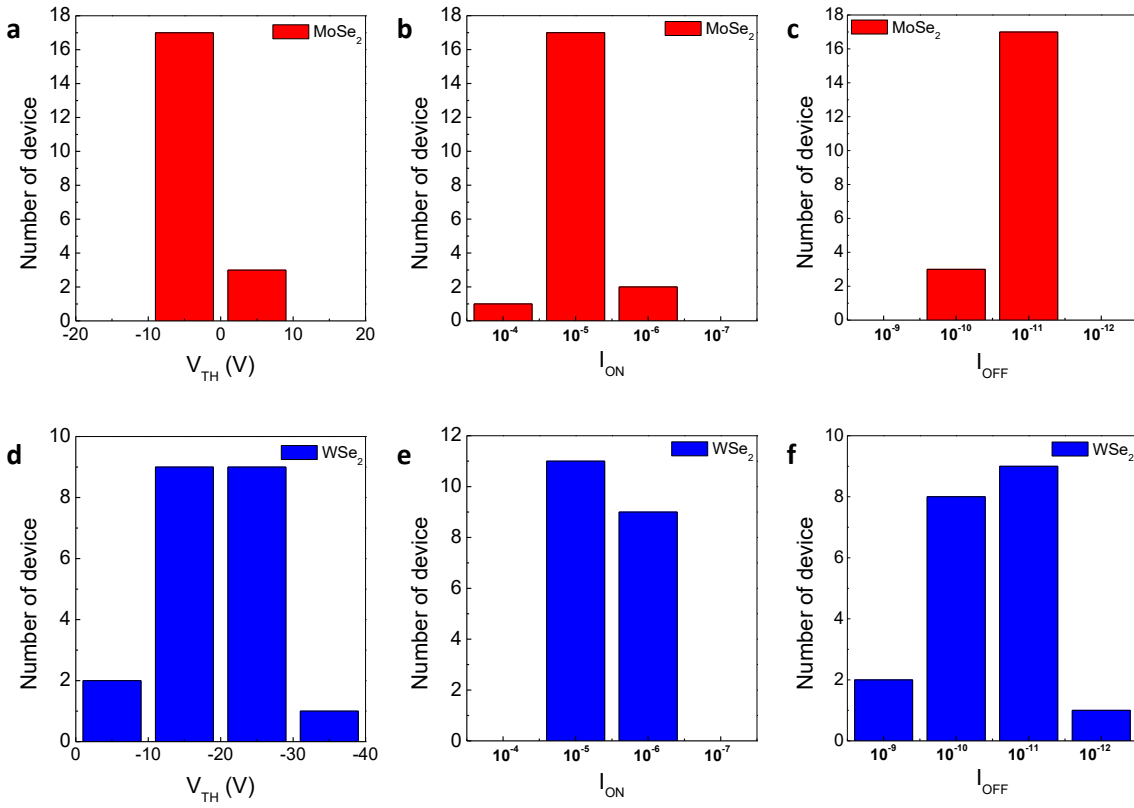


Figure S9. Statistical analysis of 20 baseline MoSe₂ and 20 baseline WSe₂ transistors. Histogram distribution of (a) V_{TH} , (b) I_{ON} , and (c) I_{OFF} of the 20 baseline MoSe₂ transistors. (d) V_{TH} , (e) I_{ON} , and (f) I_{OFF} of the 20 baseline WSe₂ transistors.

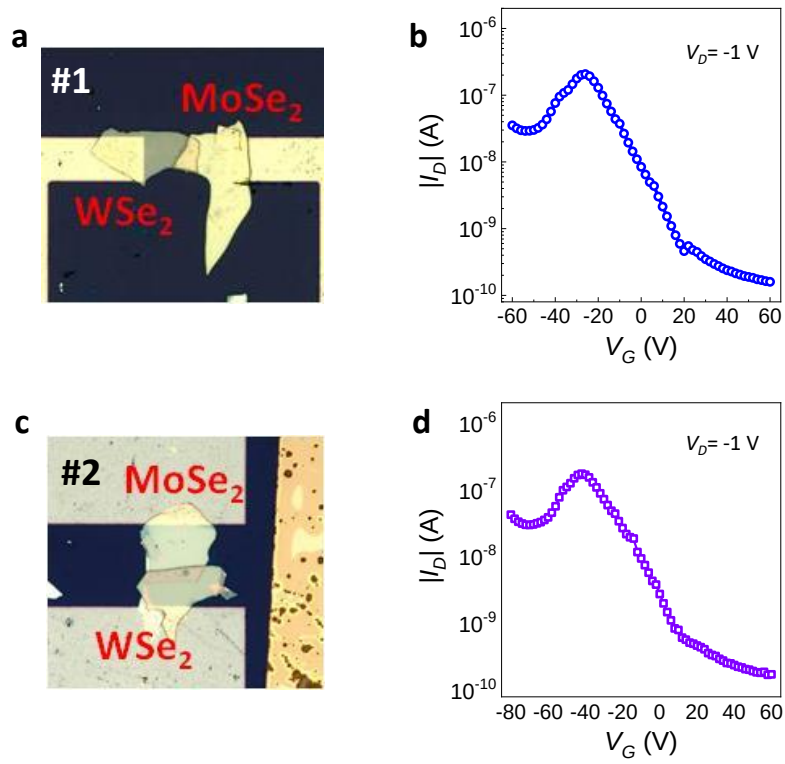


Figure S10. Investigations of multiple MoSe₂-WSe₂ vdW-H-TRs. a) Optical microscopy image and b) Transfer characteristics of the MoSe₂-WSe₂ vdW-H-TR (device #1) for $V_D = -1$ V. c) Optical microscopy image and d) Transfer characteristics of the MoSe₂-WSe₂ vdW-H-TR (device #2) for $V_D = -1$ V.

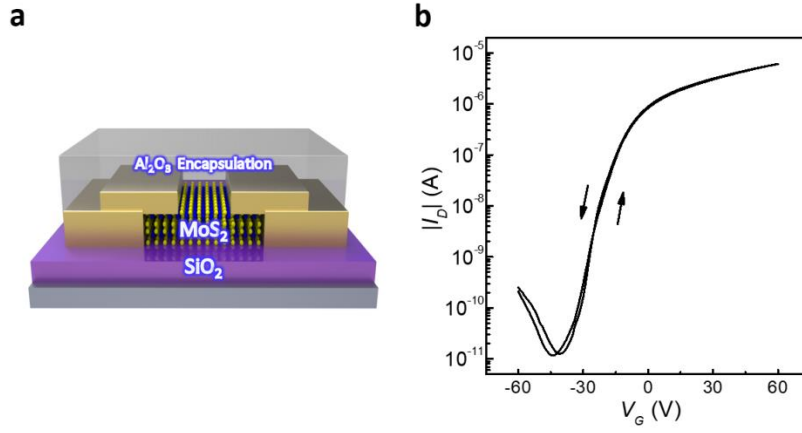


Figure S11. Forward and reverse sweeps plot of MoS₂ transistor without floating-gate. a) 3D Schematic structure of the MoS₂ H-TR. b) Transfer characteristics of the MoS₂ transistor.

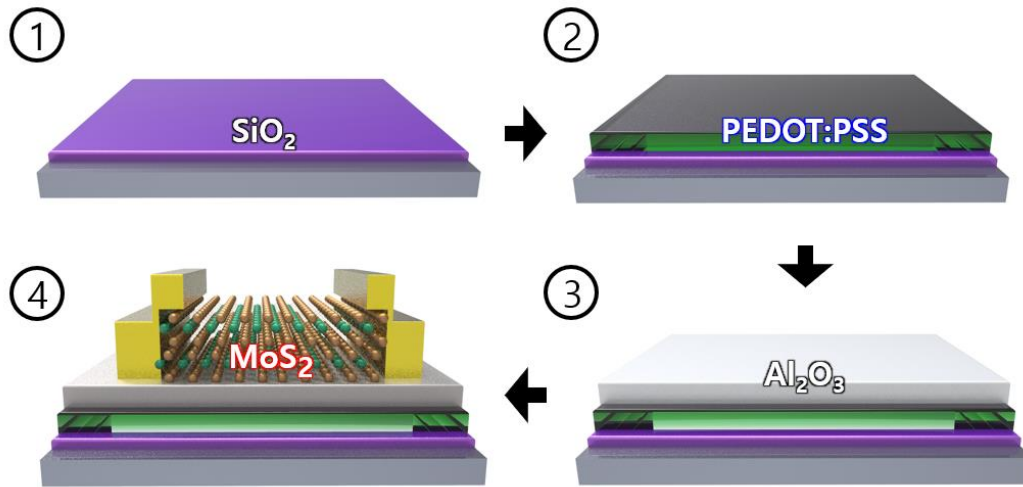


Figure S12. N-type MoS_2 floating-gate transistor fabrication process flow. We deposited PEDOT: PSS solution on top of SiO_2 substrate and sequentially deposited 80 nm thick Al_2O_3 by atomic layer deposition (ALD). And then, Au/Ti (100 nm/20 nm) as contact electrode was deposited on top of mechanically exfoliated MoS_2 layer.

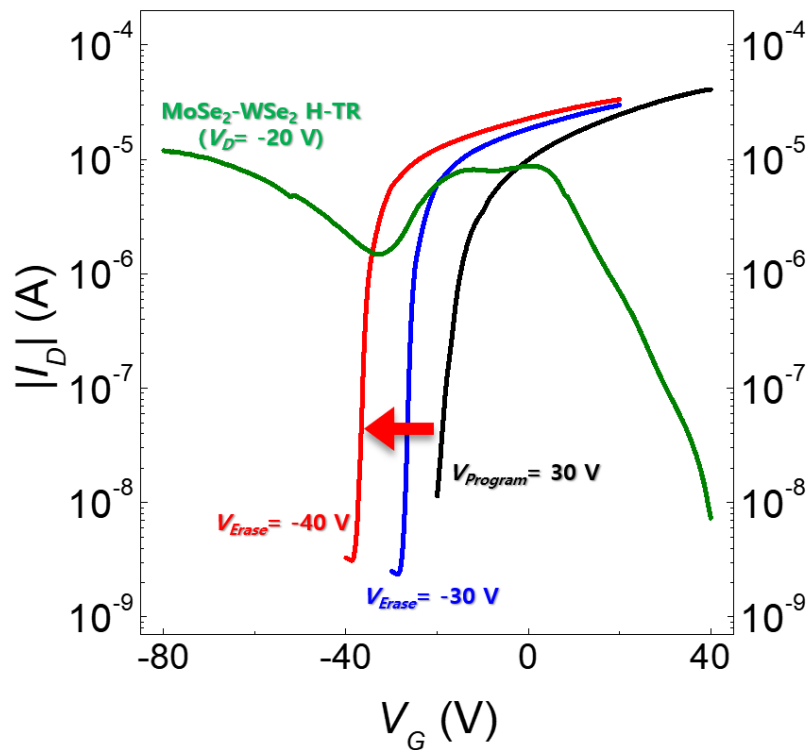


Figure S13. Comparison of transfer curves of the MoSe₂-WSe₂ vdW-H transistor (green curve for $V_D = -20$ V) and MoS₂ floating-gate transistor (black curve for $V_{Program} = 30$ V, blue curve for $V_{Program} = -30$ V and red curve for $V_{Erase} = -40$ V).

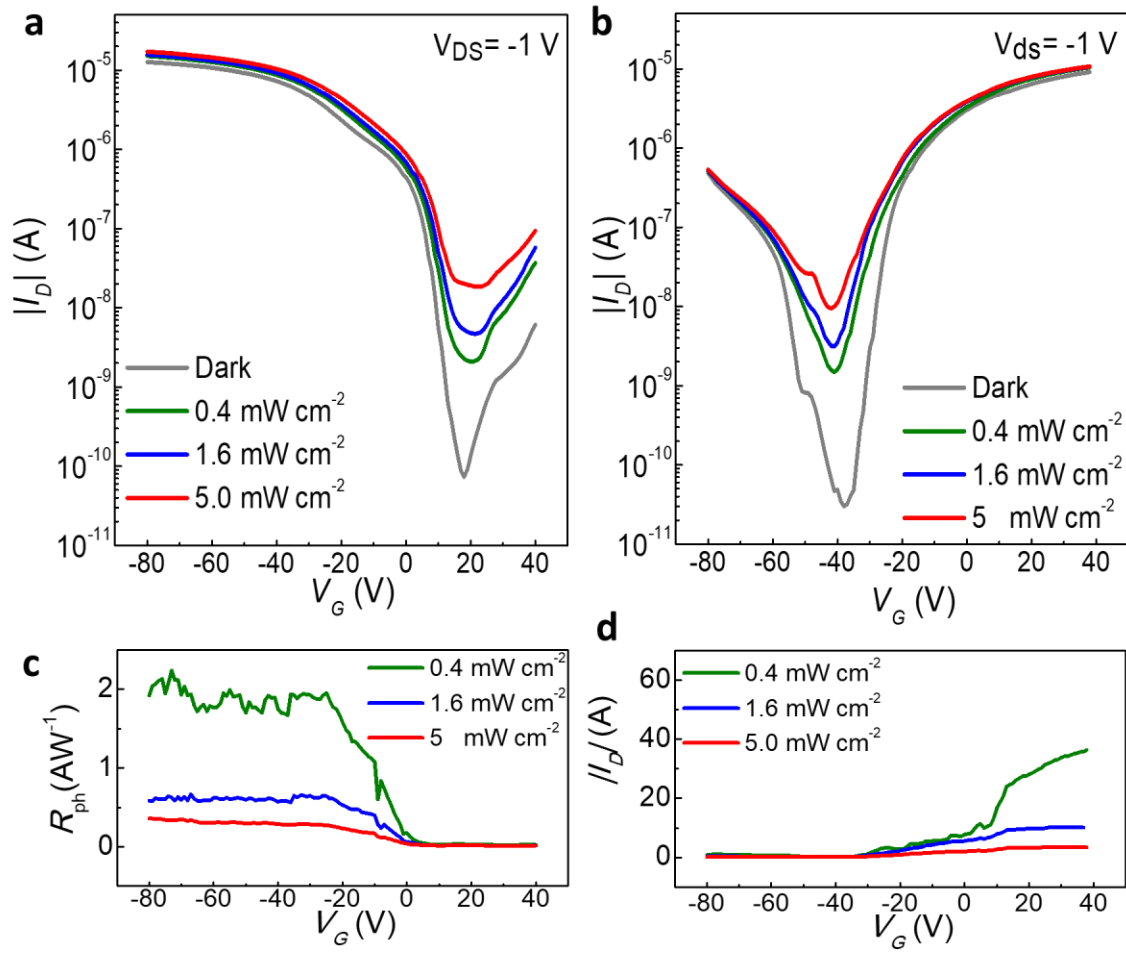


Figure S14. Photoresponsive characteristics of the baseline MoSe₂ and baseline WSe₂ transistors for $V_D = -1$ V. Transfer characteristics of a) MoSe₂ transistor and b) WSe₂ transistor under illumination for $V_D = -1$ V ($P_{inc} = 0.4, 1.6$, and 5.0 mW cm⁻², and $\lambda_{ex} = 638$ nm). Calculated photoresponsivity of c) MoSe₂ transistor, and b) WSe₂ transistor.

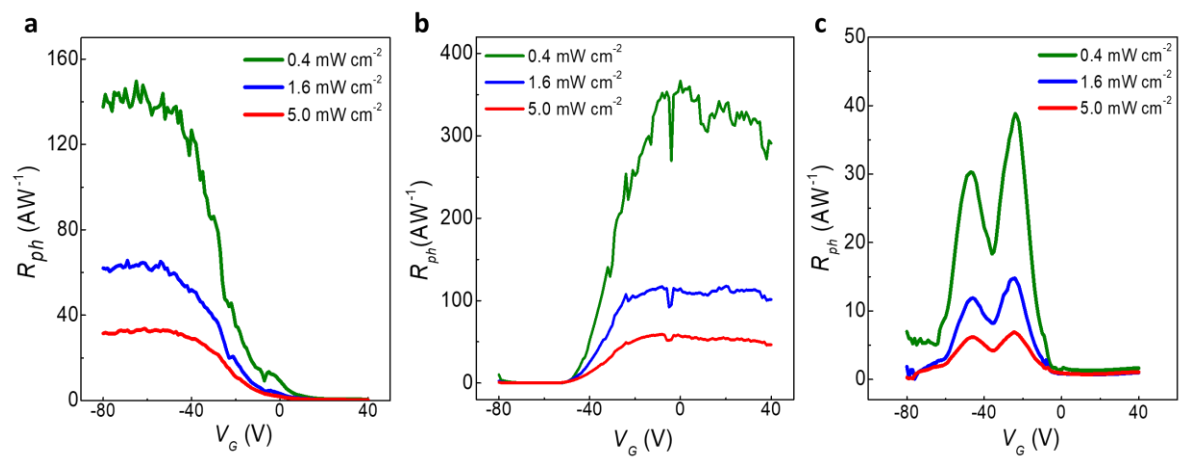


Figure S15. Photoreponsivity (R_{ph}) of a) baseline WSe_2 transistor b) baseline MoSe_2 transistor c) MoSe_2 - WSe_2 vdW-H-TR as a function of V_G .

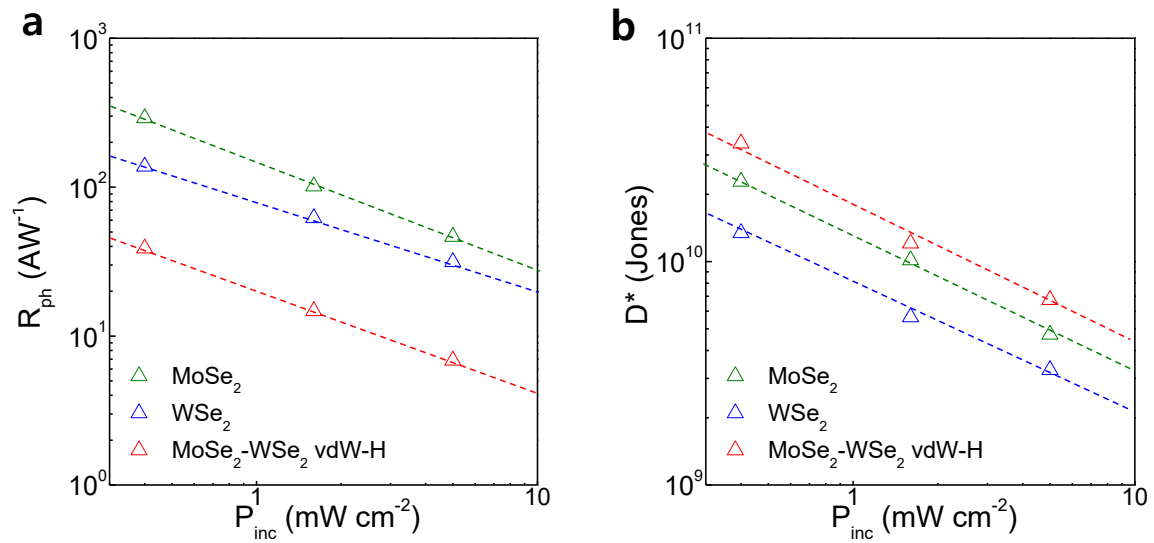


Figure S16. a) Photoresponsivity (R_{ph}) and b) specific detectivity (D^*) of the baseline WSe₂, baseline MoSe₂, and MoSe₂-WSe₂ vdW-H-TR.

References

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