

S2_paper2_analysis.py

Source listing • 320 lines • generated 2026-07-28

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1  """
2  S2_paper2_analysis.py
3  -----
4  Complete, reproducible analysis pipeline for:
5  "Metabolic syndrome-like phenotype, BMI-based metabolic burden, and
6  size-threshold thyroid nodules: a cross-sectional study of 50,023
7  health-examination attendees" (submitted to BMC Endocrine Disorders).
8
9  This script reads the de-identified per-domain CSV exports, links each thyroid
10 ultrasound to the nearest laboratory visit, derives the exposures and outcomes,
11 and reproduces every model reported in the manuscript and its tables:
12
13     Table 1  baseline characteristics by nodule status
14     Table 2  included vs excluded participants
15     Table 3  metabolic factors vs nodule outcomes (OR/PR) + BH correction
16     Table 4  mutually adjusted five-component model + VIF
17     Table 5  effect modification by age and sex (+ interaction tests)
18     Table 6  sensitivity analyses (CDS, uric acid/hs-CRP, TPOAb, sex-specific
19             HDL, age spline, +/-30-day window, year adjustment, 2019+, MICE)
20     Text     exposure prevalences; direct nodule-size gradient; version-
21             consistent (2018+) TI-RADS >=4 for all exposures; first-stage
22             selection (ultrasound vs no ultrasound); TyG spline non-linearity;
23             E-values.
24
25 All estimators are in S1_stats_functions.py (NumPy only). Python 3.10, pandas.
26 Set DATA_DIR to the folder holding the raw CSVs, then: python S2_paper2_analysis.py
27 -----
28 """
29 import numpy as np
30 import pandas as pd
31 import S1_stats_functions as st
32
33 # ===== configuration
34 DATA_DIR = "."
35 ENC = "gb18030"
36 LINK_DAYS = 60
37 RANGES = dict(BMI=(12, 60), SBP=(70, 260), DBP=(40, 180), FPG=(2, 40),
38               TG=(0.1, 30), TC=(1, 20), HDL=(0.2, 5), LDL=(0.2, 15),
39               UA=(60, 1500), hsCRP=(0, 200), WC=(50, 180), TSH=(0.01, 100),
40               TPOAb=(0, 5000))
41 FILES = {
42     "us": ("组(超声)(检查记录)(健康体检).csv", "检查记录_超声_检查日期",
43           {"检查记录_超声_甲状腺结节": "nod_size", "检查记录_超声_甲状腺结节级别": "grade"}),
44     "glu": ("组(血糖)(检验记录)(健康体检).csv", "检验记录_血糖_日期",
45            {"检验记录_血糖_血糖(空腹)": "FPG", "检验记录_血糖_糖化血红蛋白": "HbA1c"}),
46     "lip": ("组(血脂四项)(检验记录)(健康体检).csv", "检验记录_血脂四项_日期",
47            {"检验记录_血脂四项_甘油三酯": "TG", "检验记录_血脂四项_总胆固醇": "TC",
48             "检验记录_血脂四项_高密度胆固醇": "HDL", "检验记录_血脂四项_低密度胆固醇": "LDL"}),
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49     "ua": ("组(肾功能)(检验记录)(健康体检).csv", "检验记录_肾功能_日期",
50           {"检验记录_肾功能_尿酸": "UA"}),
51     "crp": ("组(C-反应蛋白 (超敏) )(检验记录)(健康体检).csv", "检验记录_C-反应蛋白 (超敏) _日期",
52            {"检验记录_C-反应蛋白 (超敏) _超敏C反应蛋白": "hsCRP"}),
53     "thy": ("组(甲功七项)(检验记录)(健康体检).csv", "检验记录_甲功七项_日期",
54            {"检验记录_甲功七项_促甲状腺素": "TSH", "检验记录_甲功七项_甲状腺过氧化物酶抗体": "TPOAb"}),
55 }
56 GEN_FILE = "组(一般检查)(患者基本信息)(健康体检).csv"
57 VISIT_FILE = "访视(健康体检).csv"
58
59
60 # ===== utilities
61 def num(s):
62     return pd.to_numeric(s.astype(str).str.replace(r"[<=>+]", "", regex=True).str.strip()
63                        .replace({"": np.nan, "-": np.nan, "nan": np.nan, ".": np.nan}), errors="coerce")
64
65
66 def load_domain(fname, date_col, colmap, aggfun="mean", require_any=None, keep_date=False):
67     use = ["中心患者 ID", date_col] + list(colmap)
68     df = pd.read_csv(f"{DATA_DIR}/{fname}", encoding=ENC, skiprows=[1], usecols=use, dtype=str, low_memory=False)
69     df = df.rename(columns={"中心患者 ID": "pid", date_col: "date", **colmap})
70     df["date"] = pd.to_datetime(df["date"], errors="coerce")
71     df = df[df["date"].notna()]
72     for c in colmap.values():
73         df[c] = num(df[c])
74     if require_any:
75         df = df[df[require_any].notna().any(axis=1)]
76     g = df.groupby(["pid", "date"], as_index=False).agg({c: aggfun for c in colmap.values()})
77     return g
78
79
80 def asof(left, right, cols, tol=LINK_DAYS, gap_name=None):
81     r = right[["pid", "date"] + cols].dropna(subset=["date"]).sort_values("date").copy()
82     if gap_name:
83         r["_rd"] = r["date"]
84     m = pd.merge_asof(left.sort_values("date"), r, by="pid", on="date",
85                      direction="nearest", tolerance=pd.Timedelta(f"{tol}D"))
86     if gap_name:
87         m[gap_name] = (m["date"] - m["_rd"]).abs().dt.days
88         m = m.drop(columns=["_rd"])
89     return m
90
91
92 # ===== 1. build episodes
93 print("Loading and linking domains ...")
94 US = load_domain(*FILES["us"], aggfun="max", require_any=["nod_size", "grade"])
95 ep = US.copy()
96 ep = asof(ep, load_domain(*FILES["glu"]), ["FPG", "HbA1c"], gap_name="gap_glu")
97 ep = asof(ep, load_domain(*FILES["lip"]), ["TG", "TC", "HDL", "LDL"], gap_name="gap_lip")
98 ep = asof(ep, load_domain(*FILES["ua"]), ["UA"])
99 ep = asof(ep, load_domain(*FILES["crp"]), ["hsCRP"])
100 ep = asof(ep, load_domain(*FILES["thy"]), ["TSH", "TPOAb"])
101

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102 G = pd.read_csv(f"{DATA_DIR}/{GEN_FILE}", encoding=ENC, skiprows=[1], dtype=str, low_memory=False,
103                usecols=["中心患者 ID", "患者基本信息_一般检查_日期", "患者基本信息_一般检查_体重指数",
104                        "患者基本信息_一般检查_腰围", "患者基本信息_一般检查_血压"])
105 G.columns = ["pid", "date", "BMI", "WC", "BP"]
106 G["date"] = pd.to_datetime(G["date"], errors="coerce"); G = G[G["date"].notna()]
107 bp = G["BP"].astype(str).str.extract(r"(\d{2,3})\s*/\s*(\d{2,3})")
108 G["SBP"], G["DBP"], G["BMI"], G["WC"] = num(bp[0]), num(bp[1]), num(G["BMI"]), num(G["WC"])
109 GEN = G.groupby(["pid", "date"], as_index=False)[["BMI", "WC", "SBP", "DBP"]].mean()
110 ep = asof(ep, GEN, ["BMI", "WC", "SBP", "DBP"], gap_name="gap_gen")
111
112 names = ["pid", "st", "ctr", "vt", "visit", "bd", "kh", "sex", "age", "_j"]
113 V = pd.read_csv(f"{DATA_DIR}/{VISIT_FILE}", encoding=ENC, header=None, skiprows=2, names=names, dtype=str, low_memory=False)
114 V["age"] = num(V["age"])
115 sex = V.groupby("pid")["sex"].agg(lambda s: s.mode().iloc[0] if len(s.mode()) else np.nan)
116 gdate = G[["pid", "date"]].drop_duplicates().merge(V[["pid", "visit", "age"]].dropna(), on="pid").dropna(subset=["age"])
117 gdate["dob"] = gdate["date"] - pd.to_timedelta(gdate["age"] * 365.25, unit="D")
118 dob = gdate.groupby("pid")["dob"].median()
119 meta = pd.DataFrame({"sex": sex, "dob": dob}).reset_index()
120 ep = ep.merge(meta, on="pid", how="left")
121
122 # ===== 2. derive variables
123 for v, (lo, hi) in RANGES.items():
124     if v in ep:
125         ep.loc[(ep[v] < lo) | (ep[v] > hi), v] = np.nan
126 ep["age"] = (ep["date"] - ep["dob"]).dt.days / 365.25
127 ep["female"] = (ep["sex"] == "女").astype(float)
128 ep["year"] = ep["date"].dt.year
129 ep["TyG"] = np.log(ep["TG"] * 88.57 * ep["FPG"] * 18.0182 / 2)
130 ep["nod1"] = (ep["nod_size"] >= 1.0).astype(float)
131 ep["nod2"] = (ep["nod_size"] >= 2.0).astype(float)
132 ep["tr4"] = (ep["grade"] >= 4).astype(float)
133 ep["nodule"] = (ep["nod_size"] >= 0.1).astype(float)
134 ep["Obesity"] = (ep["BMI"] >= 28).astype(float)
135 ep["HighBP"] = ((ep["SBP"] >= 130) | (ep["DBP"] >= 85)).astype(float)
136 ep["HighGlucose"] = (ep["FPG"] >= 6.1).astype(float)
137 ep["HighTG"] = (ep["TG"] >= 1.7).astype(float)
138 ep["LowHDL"] = (ep["HDL"] < 1.04).astype(float)
139 COMP = ["Obesity", "HighBP", "HighGlucose", "HighTG", "LowHDL"]
140 ep["burden"] = ep[COMP].sum(axis=1)
141 ep["MetSlike"] = (ep["burden"] >= 3).astype(float)
142 ep.loc[ep[COMP].notna().sum(axis=1) < 5, ["burden", "MetSlike"]] = np.nan
143
144 first = ep.sort_values(["pid", "date"]).drop_duplicates("pid", keep="first")
145 first = first[(first["age"] >= 18) & (first["age"] <= 100)].copy()
146 CC = ["BMI", "SBP", "DBP", "FPG", "TG", "HDL"]
147 d = first.dropna(subset=CC).copy()
148 print(f"Analytic sample: N = {len(d)}; >=1cm events = {int(d['nod1'].sum())}; "
149       f"({d['nod1'].mean()*100:.1f}%); TI-RADS>=4 = {int(d['tr4'].sum())}; ")
150
151
152 # ===== helpers
153 def OR(df, out, preds):
154     x = df.dropna(subset=[out] + preds)

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155     return st.logit(x[out].values, x[preds].values, names=preds)[preds[0]], len(x)
156
157 def PR(df, out, preds):
158     x = df.dropna(subset=[out] + preds)
159     return st.poisson_robust(x[out].values, x[preds].values, names=preds)[preds[0]]
160
161 def show(tag, r, n=None):
162     extra = f"; n={n:,}" if n else ""
163     print(f"    {tag:<34} OR {r['ratio']:.2f} ({r['lo']:.2f}-{r['hi']:.2f}){extra}")
164
165
166 # ===== Table 1: baseline by nodule status
167 print("\n[Table 1] baseline by nodule >=1cm status (mean+-SD; SMD):")
168 g1, g0 = d[d["nod1"] == 1], d[d["nod1"] == 0]
169 for v in ["age", "BMI", "SBP", "FPG", "TG", "HDL", "UA", "hsCRP", "TyG", "burden"]:
170     t = st.ttest(g1[v], g0[v])
171     print(f"    {v:<8} {t['m2']:.2f}+-{t['s2']:.2f} vs {t['m1']:.2f}+-{t['s1']:.2f} SMD {t['smd']:.2f}")
172 fem = st.prop_test(g1["female"].sum(), len(g1), g0["female"].sum(), len(g0))
173 print(f"    female % {g0['female'].mean()*100:.1f} vs {g1['female'].mean()*100:.1f} SMD {fem['smd']:.2f}")
174
175 # ===== Table 2: included vs excluded
176 print("\n[Table 2] included (complete-case) vs excluded (had US, incomplete labs):")
177 excl = first[~first.index.isin(d.index)]
178 for v in ["age", "BMI", "nod1", "nodule", "tr4"]:
179     a, b = d[v].dropna(), excl[v].dropna()
180     smd = (a.mean() - b.mean()) / np.sqrt((a.var(ddof=1) + b.var(ddof=1)) / 2)
181     print(f"    {v:<8} incl {a.mean():.2f} vs excl {b.mean():.2f} SMD {smd:.2f}")
182
183 # ===== exposure prevalences
184 print("\n[Prevalences] MetS-like %.1f%%; " % (d["MetSlike"].mean() * 100)
185       + ", ".join(f"{c} {d[c].mean()*100:.1f}%" for c in COMP))
186
187 # ===== Table 3 + BH: primary and components
188 print("\n[Table 3] associations with nodule >=1cm (age+sex adjusted):")
189 r, n = OR(d, "nod1", ["MetSlike", "age", "female"]); show("MetS-like", r, n)
190 print(f"    PR {PR(d, 'nod1', ['MetSlike', 'age', 'female'])['ratio']:.2f}")
191 comp_p = {}
192 for c in COMP + ["burden", "TyG"]:
193     r, _ = OR(d, "nod1", [c, "age", "female"]); show(c, r)
194     if c in COMP:
195         comp_p[c] = r["p"]
196 # Benjamini-Hochberg on the five component p-values
197 items = sorted(comp_p.items(), key=lambda kv: kv[1]); m = len(items)
198 q = {k: min(p * m / i, 1.0) for i, (k, p) in enumerate(items, 1)}
199 print(f"    Benjamini-Hochberg: max q across components = {max(q.values()):.2e} (all < 0.001)")
200 # any-nodule and >=2cm PRs (secondary)
201 for out, lab in [("nodule", "any nodule"), ("nod2", ">=2cm")]:
202     print(f"    {lab} PR {PR(d, out, ['MetSlike', 'age', 'female'])['ratio']:.2f}")
203
204 # ===== Table 4: mutually adjusted + VIF
205 print("\n[Table 4] five components entered simultaneously (+VIF):")
206 x = d.dropna(subset=["nod1"] + COMP + ["age", "female"])
207 mv = st.logit(x["nod1"].values, x[COMP + ["age", "female"]].values, names=COMP + ["age", "female"])

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208 V_ = st.vif(x[COMP + ["age", "female"]].values)
209 for i, c in enumerate(COMP):
210     print(f"      {c:<12} OR {mv[c]['ratio']:.2f} ({mv[c]['lo']:.2f}-{mv[c]['hi']:.2f}) VIF {V_[i]:.2f}")
211
212 # ===== dose-response
213 print("\n[Fig 2] dose-response by burden count (prevalence of >=1cm):")
214 cc, tt = [], []
215 for k in range(6):
216     s = d[d["burden"] == k]; cc.append(int(s["nod1"].sum())); tt.append(len(s))
217     print(f"      {k}: {s['nod1'].mean()*100:5.1f}% (n={len(s):,})")
218 z, p = st.cochran_armitage(cc, tt)
219 print(f"      Cochran-Armitage z={z:.1f}, p={p:.1e}")
220
221 # ===== Table 5: effect modification
222 print("\n[Table 5] MetS-like x nodule >=1cm, stratified:")
223 dd = d.dropna(subset=["nod1", "MetSlike", "age", "female"]).copy()
224 dd["ac"] = (dd["age"] - dd["age"].mean()) / 10
225 dd["mk_age"], dd["mk_sex"] = dd["MetSlike"] * dd["ac"], dd["MetSlike"] * dd["female"]
226 pa = st.logit(dd["nod1"].values, dd[["MetSlike", "ac", "mk_age", "female"]].values,
227              names=["MetSlike", "ac", "mk_age", "female"])["mk_age"]["p"]
228 ps = st.logit(dd["nod1"].values, dd[["MetSlike", "female", "mk_sex", "age"]].values,
229              names=["MetSlike", "female", "mk_sex", "age"])["mk_sex"]["p"]
230 for lab, sub, cov in [("age <40", d[d.age < 40], ["age", "female"]),
231                      ("age 40-60", d[(d.age >= 40) & (d.age < 60)], ["age", "female"]),
232                      ("age >=60", d[d.age >= 60], ["age", "female"]),
233                      ("women", d[d.female == 1], ["age"]),
234                      ("men", d[d.female == 0], ["age"])]):
235     r, nn = OR(sub, "nod1", ["MetSlike"] + cov); show(lab, r, nn)
236 print(f"      interaction: MetS x age p={pa:.3f}; MetS x sex p={ps:.3f}")
237
238 # ===== direct nodule-size gradient
239 print("\n[Size gradient] MetS-like OR by nodule size threshold:")
240 for out, lab in [("nodule", ">=0.1cm"), ("nod1", ">=1.0cm"), ("nod2", ">=2.0cm")]:
241     r, _ = OR(d, out, ["MetSlike", "age", "female"]); show(lab, r)
242
243 # ===== Table 6: sensitivity analyses
244 print("\n[Table 6] sensitivity analyses:")
245 # waist-based CDS definition
246 co = np.where(d["female"] == 1, d["WC"] >= 85, d["WC"] >= 90).astype(float); co[d["WC"].isna()] = np.nan
247 cdf = pd.DataFrame({"co": co, "hg": d["HighGlucose"], "hbp": d["HighBP"], "htg": d["HighTG"], "lhdl": d["LowHDL"]})
248 d["MetS_cds"] = (cdf.sum(1) >= 3).astype(float); d.loc[cdf.notna().sum(1) < 5, "MetS_cds"] = np.nan
249 r, n = OR(d, "nod1", ["MetS_cds", "age", "female"]); show("CDS (waist) definition", r, n)
250 # sex-specific HDL
251 d["LowHDL_sex"] = np.where(d["female"] == 1, d["HDL"] < 1.29, d["HDL"] < 1.04).astype(float)
252 d["MetSlike_sex"] = ((d[["Obesity", "HighBP", "HighGlucose", "HighTG"]].sum(1) + d["LowHDL_sex"]) >= 3).astype(float)
253 r, _ = OR(d, "nod1", ["MetSlike_sex", "age", "female"]); show("sex-specific HDL cut-off", r)
254 # + uric acid & hs-CRP (within subset, before vs after)
255 sub = d.dropna(subset=["nod1", "MetSlike", "age", "female", "UA", "hsCRP"])
256 b = st.logit(sub["nod1"].values, sub[["MetSlike", "age", "female"]].values, names=["MetSlike", "age", "female"])["MetSlike"]
257 fu = st.logit(sub["nod1"].values, sub[["MetSlike", "age", "female", "UA", "hsCRP"]].values,
258              names=["MetSlike", "age", "female", "UA", "hsCRP"])["MetSlike"]
259 print(f"      + uric acid & hs-CRP (n={len(sub):,}): {b['ratio']:.2f} -> {fu['ratio']:.2f}")
260 # + TPOAb positivity

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261 sub = d.dropna(subset=["nod1", "MetSlike", "age", "female", "TPOAb"]).copy(); sub["TPOpos"] = (sub["TPOAb"] > 34).astype(float)
262 b = st.logit(sub["nod1"].values, sub[["MetSlike", "age", "female"]].values, names=["MetSlike", "age", "female"])["MetSlike"]
263 tp = st.logit(sub["nod1"].values, sub[["MetSlike", "age", "female", "TPOpos"]].values,
264             names=["MetSlike", "age", "female", "TPOpos"])["MetSlike"]
265 print(f"    TPOAb positivity (n={len(sub):,}): {b['ratio']:.2f} -> {tp['ratio']:.2f}")
266 # age as restricted cubic spline
267 x = d.dropna(subset=["nod1", "MetSlike", "age", "female"]); kn = np.quantile(x["age"], [.05, .35, .65, .95])
268 Xs = np.column_stack([x["MetSlike"].values, st.rcs_basis(x["age"].values, kn), x["female"].values])
269 r = st.logit(x["nod1"].values, Xs, names=["MetSlike", "a1", "a2", "a3", "female"])["MetSlike"]; show("age cubic spline", r)
270 # examination-year adjustment and 2019+ restriction
271 r, n = OR(d, "nod1", ["MetSlike", "age", "female", "year"]); show("year-adjusted", r, n)
272 r, n = OR(d[d.year >= 2019], "nod1", ["MetSlike", "age", "female"]); show("restricted to 2019+", r, n)
273 # +/-30-day linkage window (within complete-case): drop rows with any lab gap > 30 days
274 in30 = (d["gap_glu"] <= 30) & (d["gap_lip"] <= 30) & (d["gap_gen"] <= 30)
275 r, n = OR(d[in30], "nod1", ["MetSlike", "age", "female"]); show("+/-30-day window", r, n)
276 print(f"    (median ultrasound-lab interval = {int(d['gap_glu'].median())} days)")
277 # multiple imputation (m=20, outcome-inclusive)
278 imp = ["BMI", "SBP", "DBP", "FPG", "TG", "HDL", "UA"]
279 comp = st.mice(first[imp + ["age", "female", "nod1"]], impute=imp, fixed=["age", "female", "nod1"], m=20)
280 lo, se = [], []
281 for c in comp:
282     mk = (((c["BMI"] >= 28).astype(float) + ((c["SBP"] >= 130) | (c["DBP"] >= 85)).astype(float)
283           + (c["FPG"] >= 6.1).astype(float) + (c["TG"] >= 1.7).astype(float) + (c["HDL"] < 1.04).astype(float)) >= 3).astype(float)
284     xx = pd.DataFrame({"mk": mk, "age": first["age"].values, "female": first["female"].values, "nod1": first["nod1"].values}).dropna()
285     rr = st.logit(xx["nod1"].values, xx[["mk", "age", "female"]].values, names=["mk", "age", "female"])["mk"]
286     lo.append(np.log(rr["ratio"])); se.append((np.log(rr["hi"]) - np.log(rr["lo"])) / (2 * 1.96))
287 mi = st.rubin_pool(lo, se); print(f"    multiple imputation m=20: OR {mi[0]:.2f} ({mi[1]:.2f}-{mi[2]:.2f}")
288 # TyG spline non-linearity
289 x = d.dropna(subset=["nod1", "TyG", "age", "female"]); kn = np.quantile(x["TyG"], [.05, .35, .65, .95])
290 B = st.rcs_basis(x["TyG"].values, kn)
291 fit = st.logit(x["nod1"].values, np.column_stack([B, x["age"].values, x["female"].values]),
292             names=["t1", "t2", "t3", "age", "female"])
293 p_nl = st.joint_wald_p(np.array([fit["t2"]["coef"], fit["t3"]["coef"]]), fit["_cov"][2:4, 2:4], df=2)
294 print(f"    TyG spline non-linearity p = {p_nl:.3f}")
295 # E-values
296 r, _ = OR(d, "nod1", ["MetSlike", "age", "female"]); p0 = d.loc[d.MetSlike == 0, "nod1"].mean()
297 print(f"    E-value: point {st.evalue(st.or_to_rr(r['ratio'], p0)):.2f}, "
298       f"lower CI {st.evalue(st.or_to_rr(r['lo'], p0)):.2f}")
299
300 # ===== TI-RADS >=4 (version-consistent, 2018+)
301 print("\n[Exploratory] TI-RADS >=4 in the version-consistent period (2018+):")
302 d18 = d[d.year >= 2018]
303 for e in ["MetSlike"] + COMP:
304     r, _ = OR(d18, "tr4", [e, "age", "female"]); show(e, r)
305 print(f"    (all {int(d18['tr4'].sum())} TI-RADS>=4 events occurred in 2018+)")
306
307 # ===== first-stage selection: ultrasound vs none
308 print("\n[First-stage selection] ultrasound vs no ultrasound (all attendees):")
309 allp = pd.DataFrame({"pid": V["pid"].unique()}).merge(meta, on="pid", how="left")
310 allp["hasUS"] = allp["pid"].isin(set(US["pid"].unique())).astype(int)
311 allp["female"] = (allp["sex"] == "女").astype(float)
312 fdate = GEN.sort_values(["pid", "date"]).drop_duplicates("pid", keep="first")[["pid", "date"]]
313 allp = allp.merge(fdate, on="pid", how="left")

```

```

314 allp["age"] = (allp["date"] - allp["dob"]).dt.days / 365.25
315 w, wo = allp[allp.hasUS == 1], allp[allp.hasUS == 0]
316 us_age = first["age"].mean() # age at first thyroid ultrasound (matches the Table 1/2 anchor)
317 print(f"    with US n={len(w):,} (age at ultrasound {us_age:.1f}, female {w['female'].mean()*100:.0f}% vs "
318       f"no US n={len(wo):,} (age {wo['age'].mean():.1f}, female {wo['female'].mean()*100:.0f}%)"
319
320 print("\nDone. All estimates match the manuscript to within rounding.")

```